

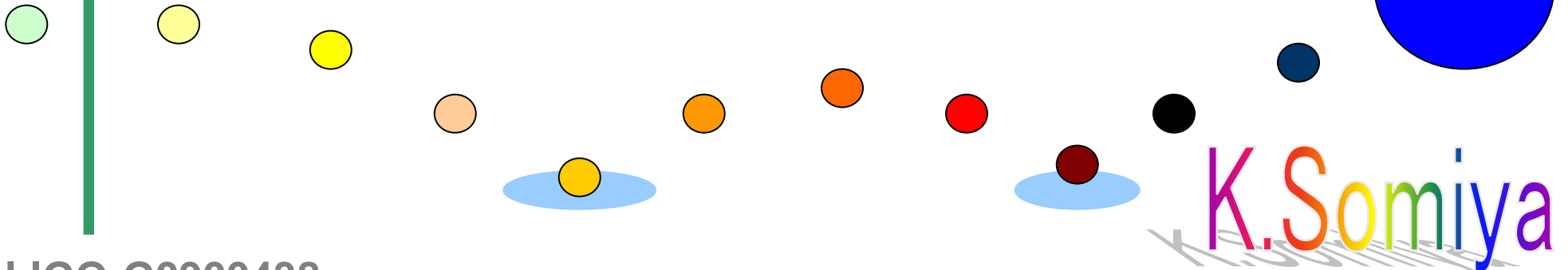
Conceptual Design of the Hannover 10m Interferometer for sub SQL measurement

K. Somiya

for Hannover-10m team

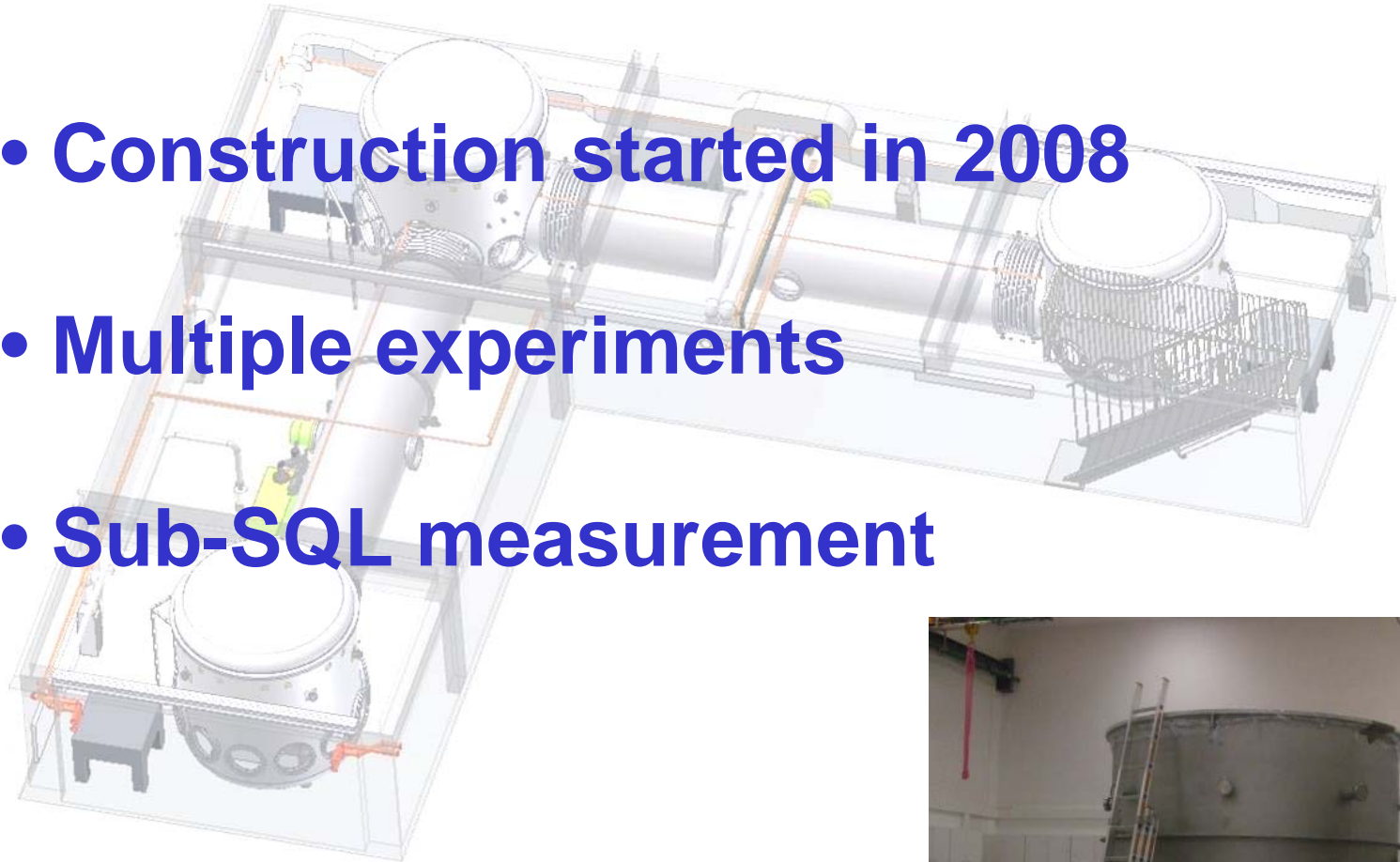
GWADW at Ft Lauderdale

May 2009



Hannover 10m

- Construction started in 2008
- Multiple experiments
- Sub-SQL measurement



vacuum chamber
 $\phi=3\text{m}$, $h=3.2\text{m}$



Today's talks for the 10m

1. Noise analysis and IFO design (K.Somiya)

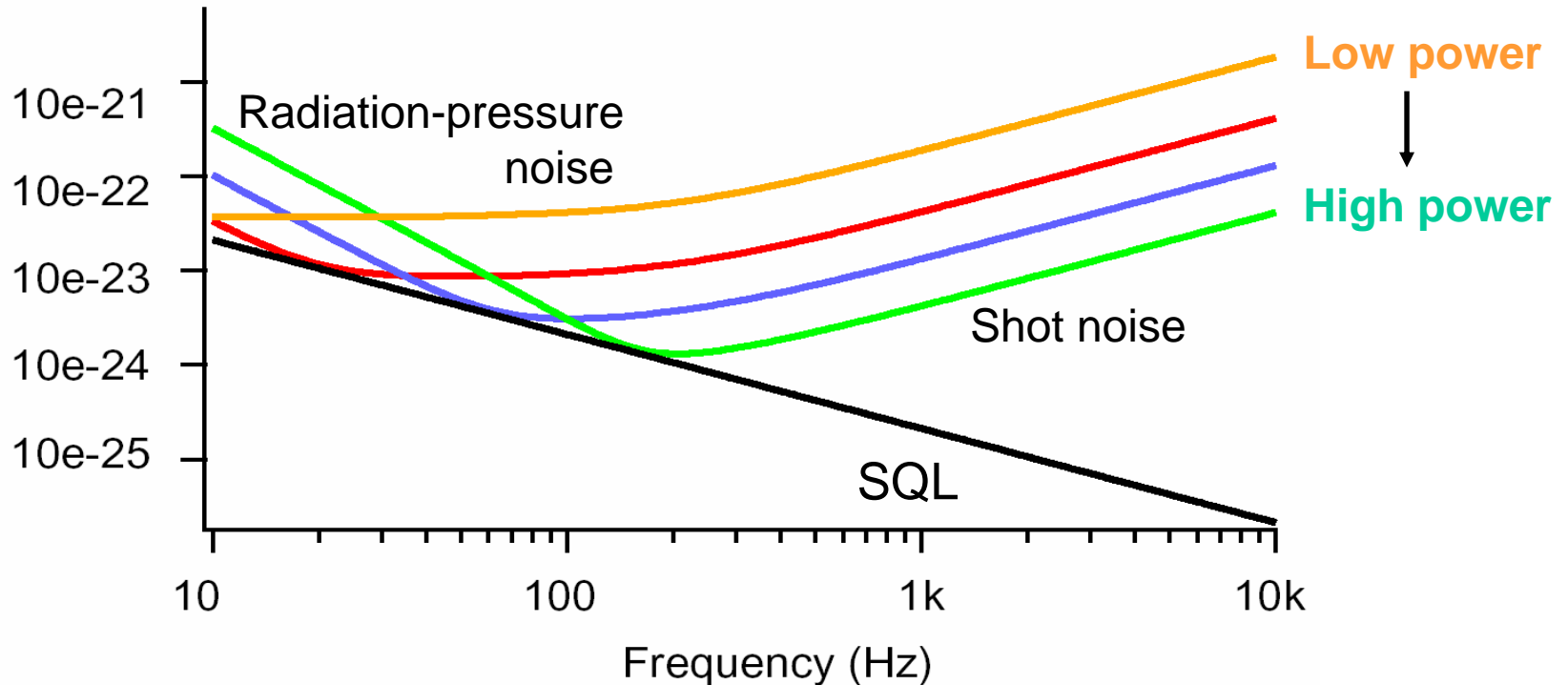
- SQL
- Reduction of thermal noise
- Parameter optimization

2. Discussion of various configurations (F.Kawazoe)

3. Overview and status of the experiment (S.Gossler)

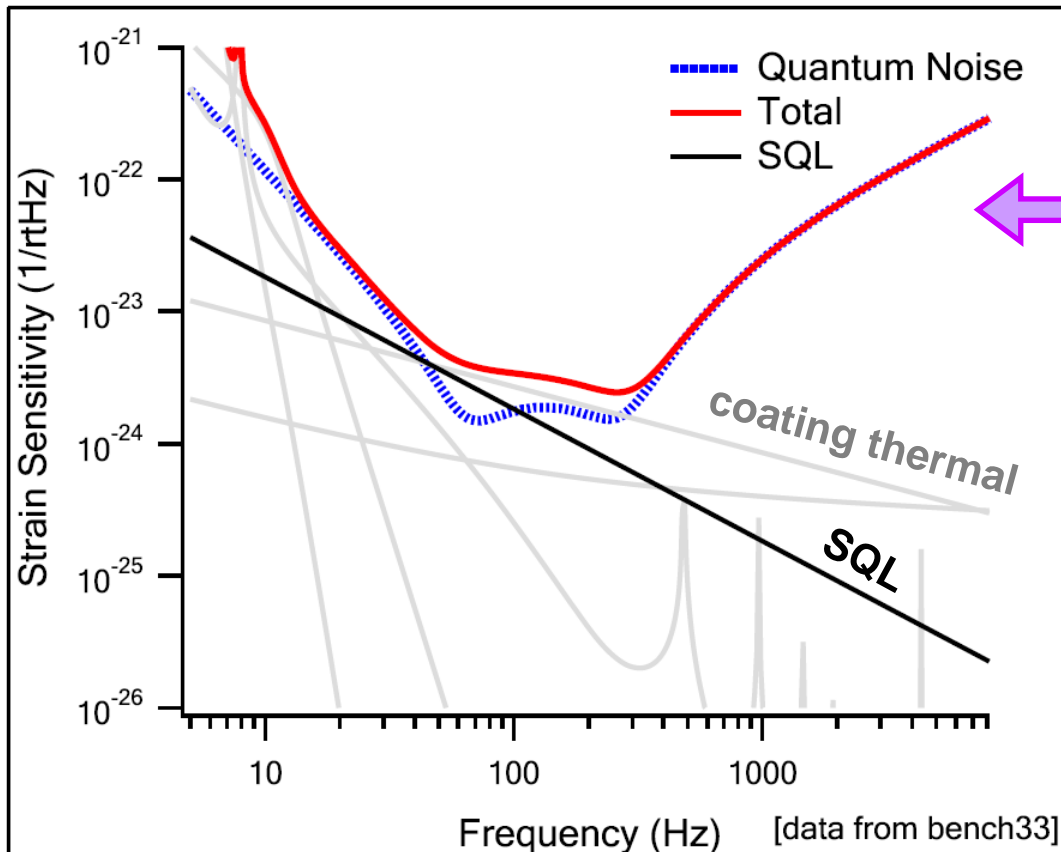
Standard Quantum Limit (SQL)

Noise Spectrum (1/r²Hz)



- **Quantum limit of conventional measurement** (FPMI w/RF)
- **Ideas to overcome the limit**
(squeezing, homodyne detection, speed-meter, opt-spring, ... etc.)
- **Essential to test quantum mechanics**

Can we reach the SQL?



AdLIGO's sensitivity
will be close to the SQL

40kg masses are almost in
the quantum superposition!!

$$h_{SQL} = \sqrt{\frac{8\hbar}{m\Omega^2 L^2}}$$

- What if we reduce the mass?
- Can we reduce thermal noise?

Mass-dependence of thermal noise

1. SQL and coating Brownian TN

$$\text{SQL} \propto 1/\sqrt{m}$$

$$\text{coating TN} \propto 1/w_0 \propto 1/m^{1/3} \quad \text{[fixed aspect-ratio]}$$

➡ Gain is only by $m^{1/6}$

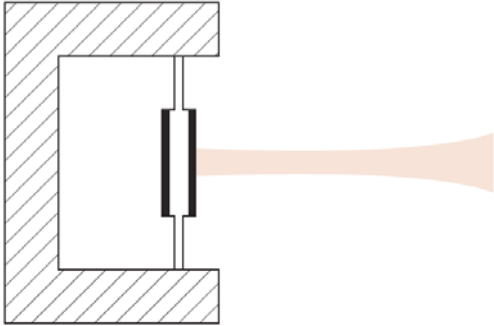
2. SQL and suspension TN

$$\text{susp TN} \propto \begin{cases} 1/m^{3/4} \text{ (LF)} \\ 1/m^{5/4} \text{ (HF)} \end{cases} \quad \text{[fixed wire-thickness]}$$

➡ Susp TN increases faster than SQL

Low-mass regime and high-mass regime

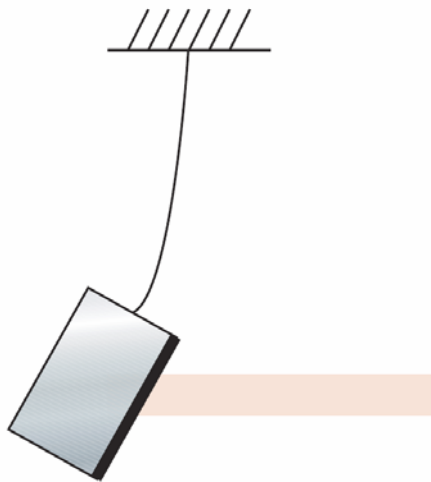
[Low-mass regime]



- high SQL
- high frequency
- low Q, but easy to cool down

300K → 4K

[High-mass regime]



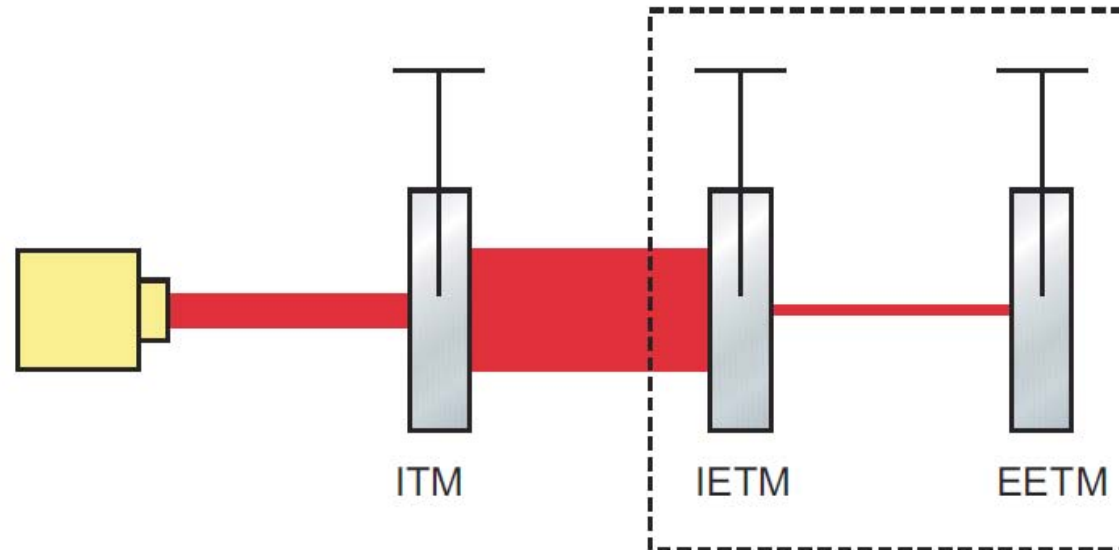
- high-Q pendulum with dilution by gravity
- $$Q = \frac{\text{resonance}}{\text{loss}}$$
- ← restoring force: gravity
- ← loss of silica fiber

dilution factor >> 1000

- knowledge from GW detectors
- need to do something to reduce coating TN

Reduction of coating TN with end-mirror cavity

[Khalili PLA 05]



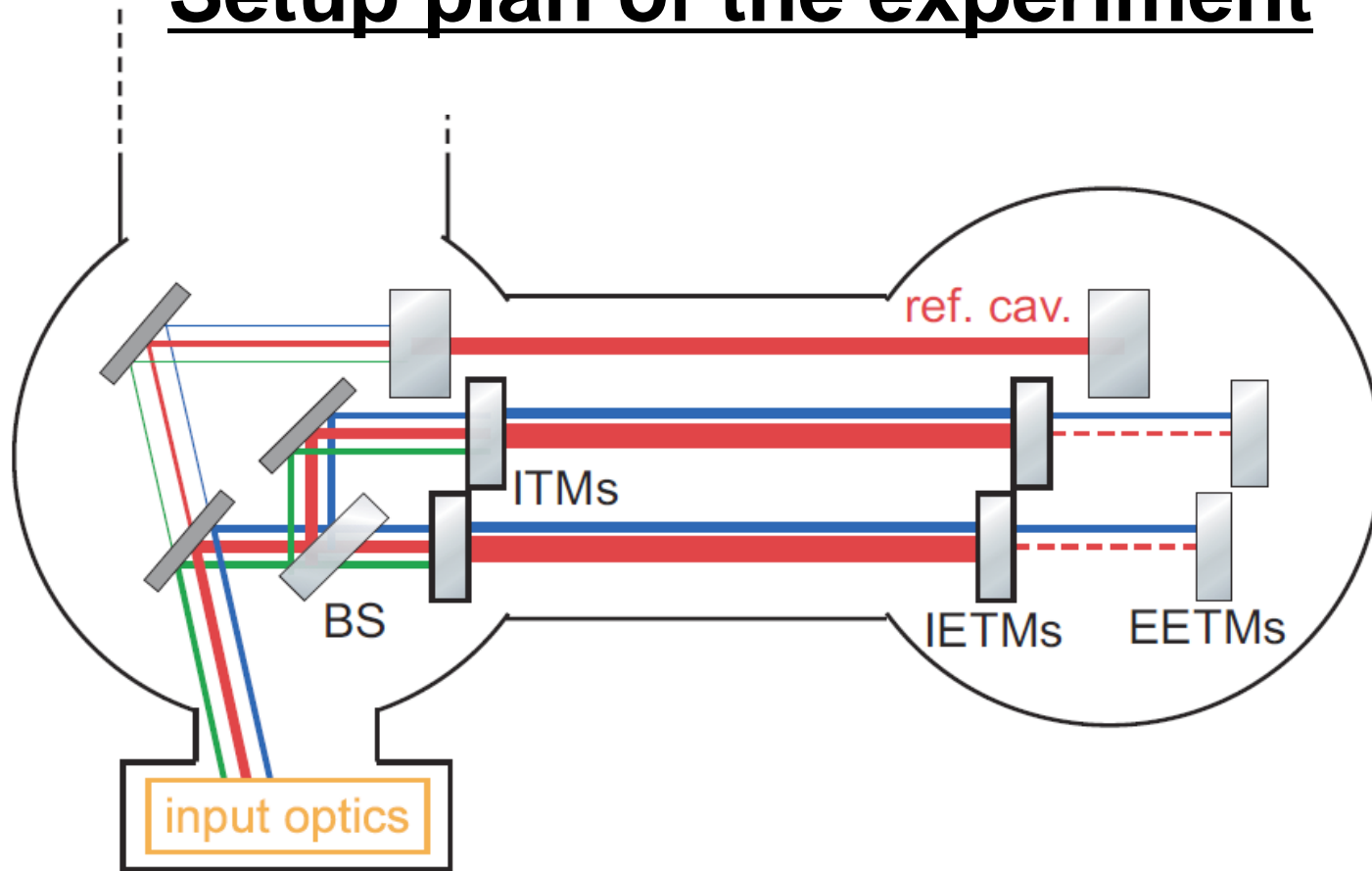
Replacing ETM to an anti-resonant cavity

→ { less coating on IETM
little noise coupling from EETM

~20% TN reduction with $r_{\text{IETM}} = r_{\text{ITM}}$

→ can be better with lower r_{IETM}

Setup plan of the experiment



- **Folded FPMI with end-mirror cavities**
- **Ref. cavity with heavy mirrors for freq-stabilization**
- **Seismic isolation with SAS and SPI**

Parameters to be optimized

1. Mass

- Trade-off of susp-TN/SQL vs coat-TN/SQL

2. Aspect ratio of a mirror

- Finite-size analysis

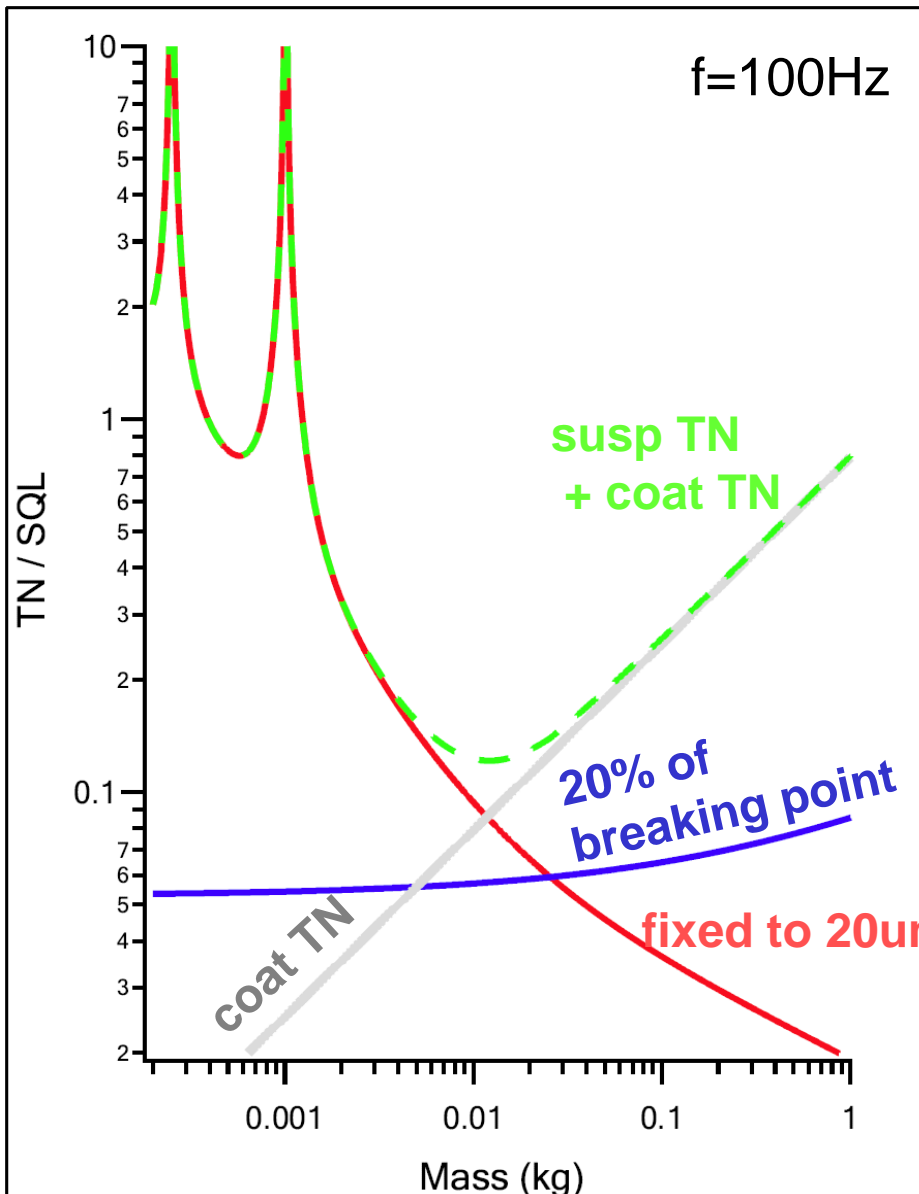
3. Reflectivity of each mirror

- Trade-off of IETM TN vs EETM TN (+ IETM TR noise)

4. Arm length

- Trade-off of freq noise vs cavity stability

(1) Mass optimization



- **Manufacture limit ~ 20um**
- **Breaking point ~ 2GPa**
- **2 fibers on each side**
- **30cm length**
(1st violin mode = 500Hz w/ m=100g)



Optimal mass: m=12g

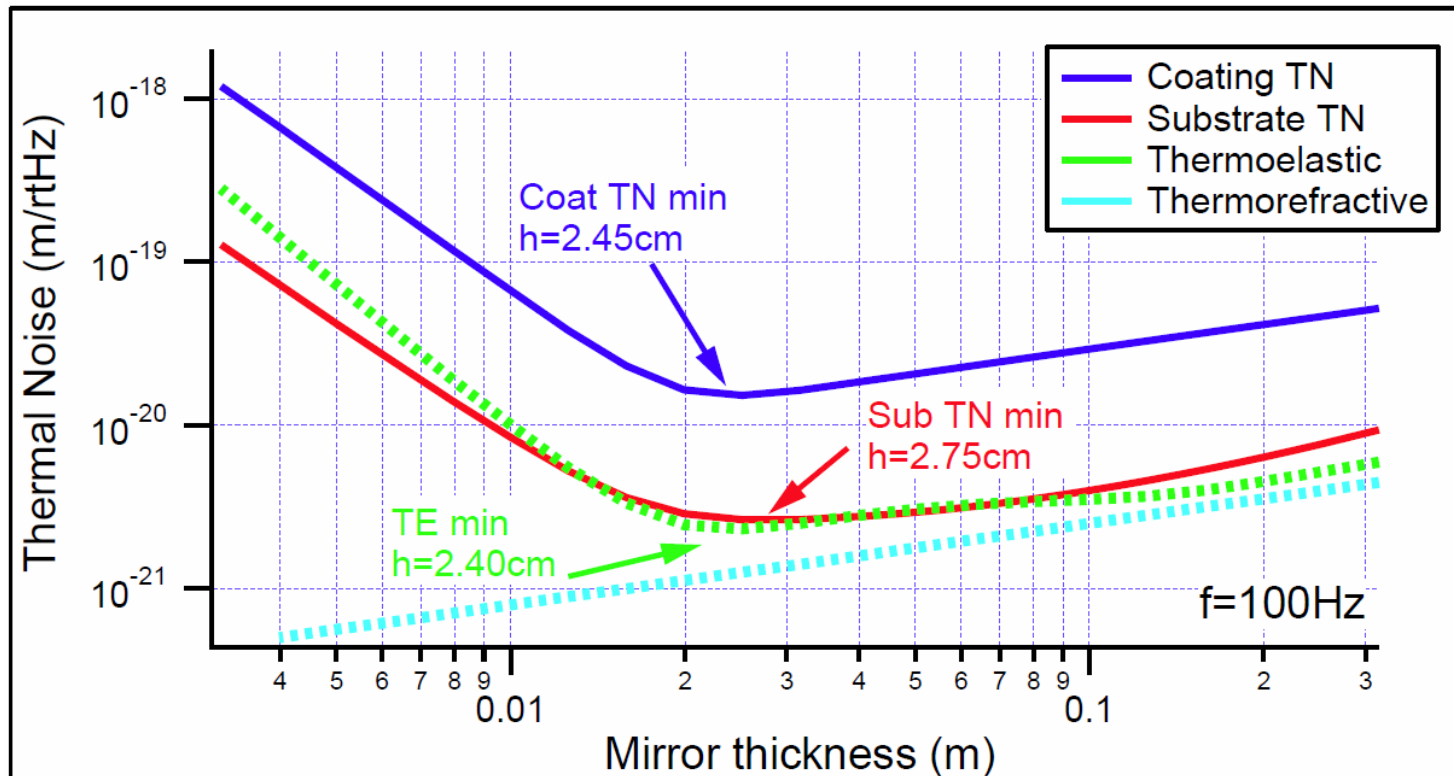


The smaller, the harder.

Our choice: m=100g

(2) Aspect ratio

[Somiya PRD 09]

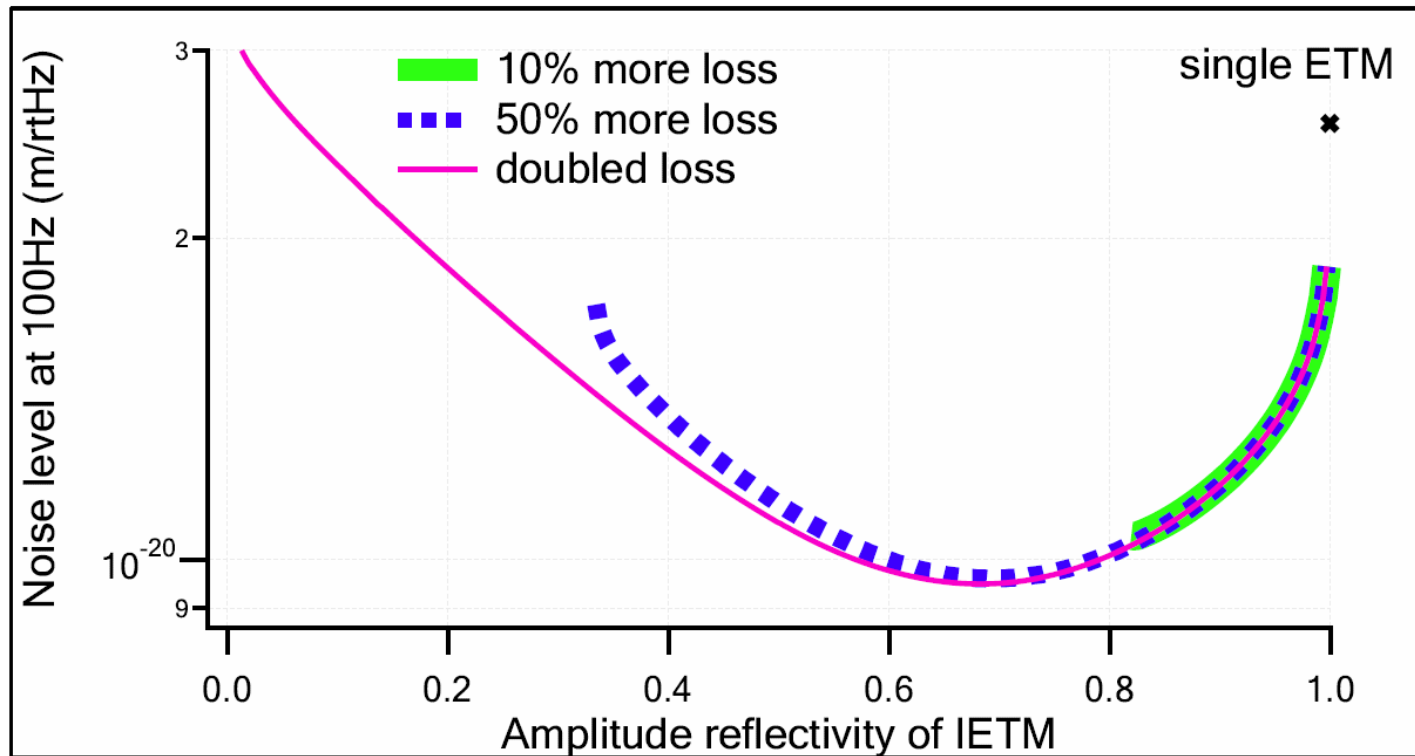


Mass is fixed to 100g. Beam radius is mirror radius/2.5.

- big h \rightarrow small beam radius \rightarrow noise increases
- small h \rightarrow high susceptibility \rightarrow noise increases

Our choice: $h=2.45\text{cm}$, $a=2.43\text{cm}$

(3) Reflectivity optimization

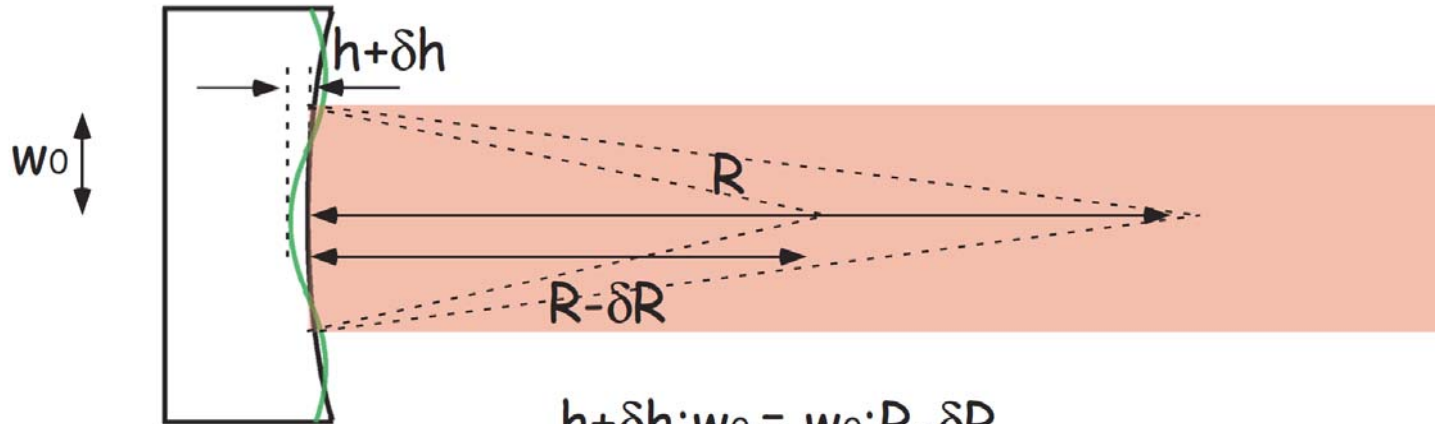


- high IETM-ref → more coat TN on IETM
- low IETM-ref → more coat TN from EETM
(also IETM's substrate thermorefractive)

Our choice: N=2 (r=0.72) for IETM

[N=15 for EETM]

(4) Arm length and cavity stability



$$h + \delta h : w_0 = w_0 : R - \delta R$$

$$\Rightarrow \delta h = (w_0/R)^2 \times \delta R$$

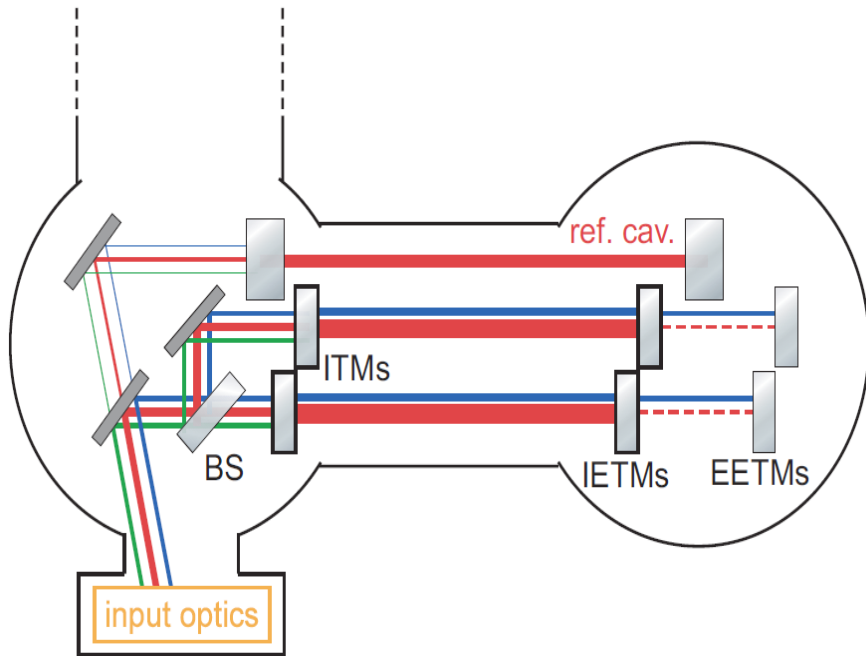
Cavity stability :

$$w_0 < \frac{\lambda}{\pi} \sqrt{\frac{L}{2\delta h}} \Rightarrow L > 2\delta h \left(\frac{w_0 \pi}{\lambda} \right)^2$$

- mirror radius / 2.5 = 9.7mm
 - $\delta h \sim 2\text{nm}$
- $\} \Rightarrow L > 3.3\text{m}$

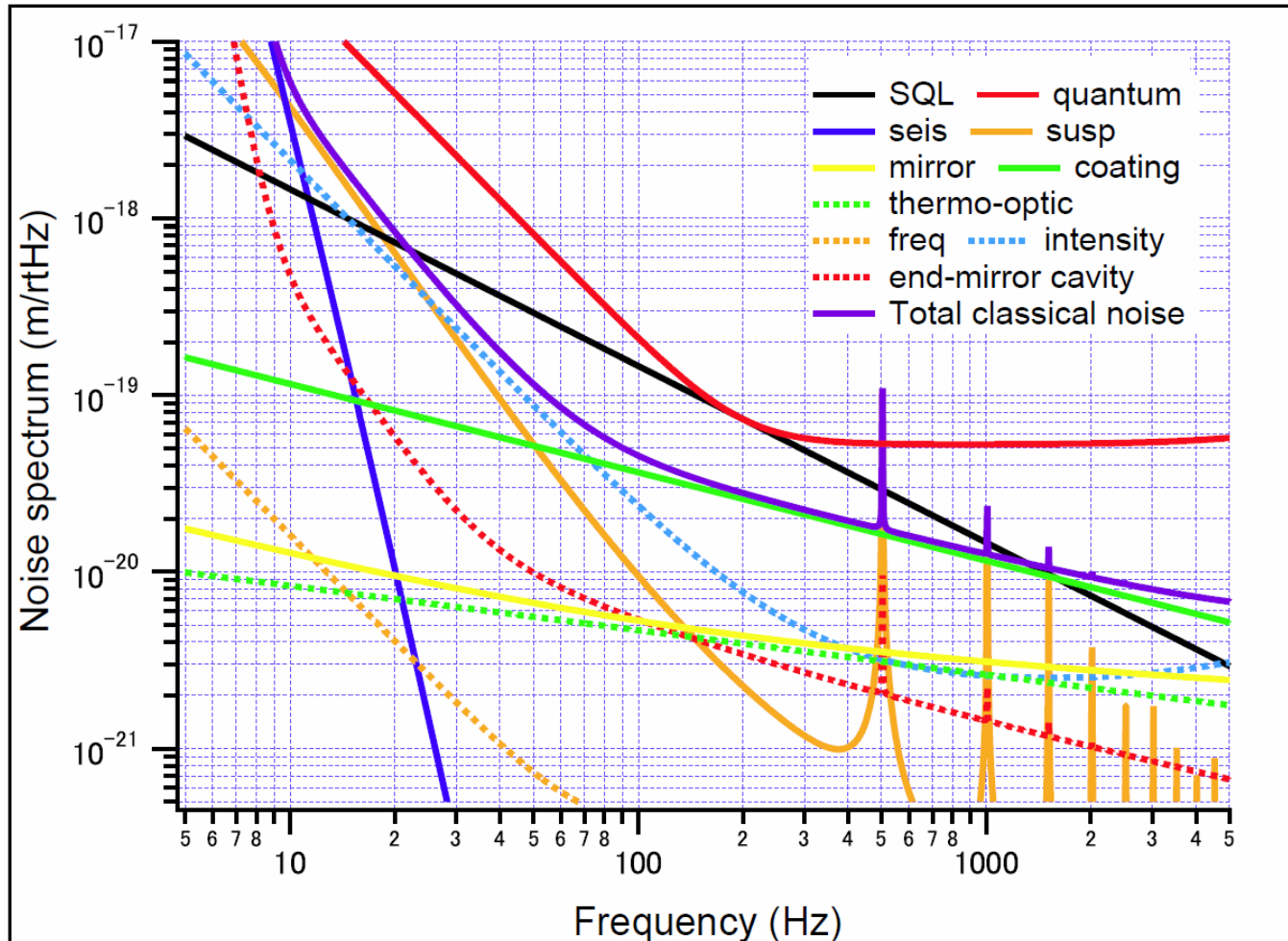
Our choice: L=10m (1.5m chamber + 10m pipe)

Parameters are determined



- number of coating layers
 $N=8$ (ITM), 2 (IETM), 15 (EETM)
finesse = 600
- **$L=10\text{m}$**
- **$m=100\text{g}$ ($\phi 2.45\text{cm} \times 2.43\text{cm}$)**
- input power = 5.5W
(touching SQL at 200Hz)
- suspension **$l=30\text{cm}$, $d=28\mu\text{m}$, $N=4$**
- mechanical losses (at 100Hz)
susp: $6\text{e-}7$, subs: $5\text{e-}10$,
coat (silica): **$1\text{e-}4$** , coat (tantala): **$4\text{e-}4$**
- ISS: 100mW PD
- FSS: reference cavity
($F=6000$, $l=100\text{mW}$, $m=860\text{g}$)

Estimated noise curve



- SQL is a factor ~ 3.2 above classical noise (100Hz)!
- Coat TN (ITM) and intensity noise limit the margin

Discussion to increase the margin

Coating TN reduction

- ITM cavity (or power-recycling)
- doped tantala
- non-quarter-wave-length coatings

Intensity noise reduction

- stabilization with L+
- stabilization with squeezing

Mass reduction

- ribbon suspension
- magnetic levitation

End of the slides