

*LIGO Laboratory / LIGO Scientific Collaboration*

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*Advanced LIGO*

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Beamsplitter  
Diffraction Loss  
(Advanced LIGO)

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LIGO Science Collaboration

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**Abstract**

The geometric and diffractive optical power losses of the input beam from the power recycling (PR) and signal recycling (SR) mirror directions were calculated as a function of the diameter and thickness of the beamsplitter for Adv LIGO, using the ZEMAX physical optics propagation analysis.

Two configurations were considered: 1) the standard configuration, which included the BS baseline dimensions of  $t = 60$  mm,  $D = 350$  mm, and 2) an alternative configuration, in which a lens element was incorporated into the ITM reaction mass (RAM) for reducing the spot size at the BS.

With the BS baseline dimensions and no lensing in the RAM, the total power loss for both arms with the PR input beam is  $3.94 \text{ E-}4$ ; the total power loss for both arms with the SR input beam is  $1.01 \text{ E-}3$ .

With the alternate configuration incorporating a 9000 mm radius of curvature on the back surface of the RAM, comparable total power loss occurs for a BS size of  $t = 40$ mm,  $D = 260$  mm, which is similar to the size used for initial LIGO.

## **1 Introduction**

One of the factors that must be considered in choosing the dimensions for the beamsplitter for advanced LIGO is the geometric optical power loss caused by the finite diameter of the tilted beamsplitter and the diffraction losses around the edges of the beamsplitter.

### **1.1 Scope**

This technical note will summarize the results of the physical optics propagation analysis. ZEMAX optical design program was used to calculate the geometric and diffractive optical power losses of the input beam from the power recycling (PR) and signal recycling (SR) mirror directions as a function of the diameter and thickness of the beamsplitter in Adv LIGO.

An alternative vertex configuration is considered in which a lens element was added to the ITM reaction mass (RAM). This reduces the spot size at the beam splitter (BS) and allows a smaller diameter BS to be used for the same power loss.

### **1.2 Referenced Documents**

*ZEMAX Optical Design Program User's Guide*, April 9, 2005 Zemax Development Corporation  
Garilynn. Billingsley, Specification for Advanced LIGO COC, LIGO-T000140-00, 11/15/00 (rev 12/3/04)

## 2 Analysis

The Gaussian beam incident on the beam splitter (BS) of the LIGO interferometer is vignetted by the finite size and the 45 deg orientation of the BS, resulting in a geometric loss of beam power incident on the input test mass (ITM). The edges of the BS and the edges of the ITM produce edge diffraction, which result in additional losses of beam power during traversal to the end test mass (ETM).

The input beam incident on the BS from the power recycling (PR) mirror can be offset laterally so that the input beam centerline passes through the geometric center of the BS at the internal mid-plane of the BS. This offset minimizes the transmission loss through the BS.

However, it may be better to center the input beam from the PR mirror onto the BS HR surface because that minimizes the power loss from the signal recycling (SR) mirror direction. The geometric and diffractive losses of the beam input into the interferometer from the signal recycling mirror are larger than the losses experienced by the main beam input through the power recycling mirror because of the lateral offset of the beams exiting the BS AR surface.

The geometric and diffractive losses with the input beam centered on the HR surface of the BS were calculated using physical optics propagation analysis of the ZEMAX Optical Design Program. The ZEMAX physical optics propagation analysis calculates the amplitude and phase of wave fronts propagated through the optical system using Fresnel diffraction theory of a scalar field. This approach is accurate except in optical systems that have very low f-numbers on the order of 1. The results are dependent upon the sampling size chosen for the analysis. With the 256 x 256 sampling array chosen for these current calculations, the results are expected to be accurate within 10%.

### 2.1 Beam Size at the ITM

The beam size at the ITM was taken to be 60mm. The baseline arm cavity design has ITM and ETM mirrors with radii of curvature 2076m separated by a cavity length of 4000m. The 11.491mm beam waist occurs in the middle of the arm cavity 2000m away from the ITM. The relation between the beam size at the ITM and the beam waist is described by the following Gaussian beam propagation equation.

$$w_{\text{bs}} := w_0 \cdot \left[ 1 + \left( \frac{\lambda \cdot z}{\pi \cdot w_0^2} \right)^2 \right]^{0.5}$$

### 2.2 Beam Size at the BS

#### 2.2.1 No Lensing at RAM

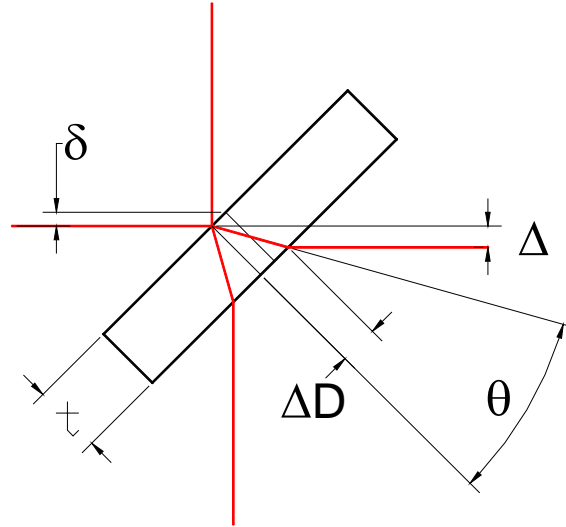
With no lensing at the RAM, the beam size at the BS is approximately the same as the beam size at the ITM, which is 60mm.

### 2.2.2 Lens at RAM

With a 9000mm radius placed on the RAM back surface, the plano-convex lens that is formed reduces the beam size at the BS to 46.8 mm.

### 2.3 Optimum Position of Input Beam on BS HR Surface

The geometry of the BS and the four reflected and refracted beams are shown in Figure 1.



**Figure 1: BS Geometry**

The refraction angle at the BS HR surface is given by the following equation.

$$\theta := \text{asin}\left(\frac{\sin\left(\frac{\pi}{4}\right)}{n}\right)$$

where  $n = 1.449636$  is the index of refraction of fused silica (SUPRASIL).

The displacement of the refracted input beam as it emerges from the AR surface of the BS is given by the following equation.

$$\Delta D(t) := t \cdot \tan(\theta)$$

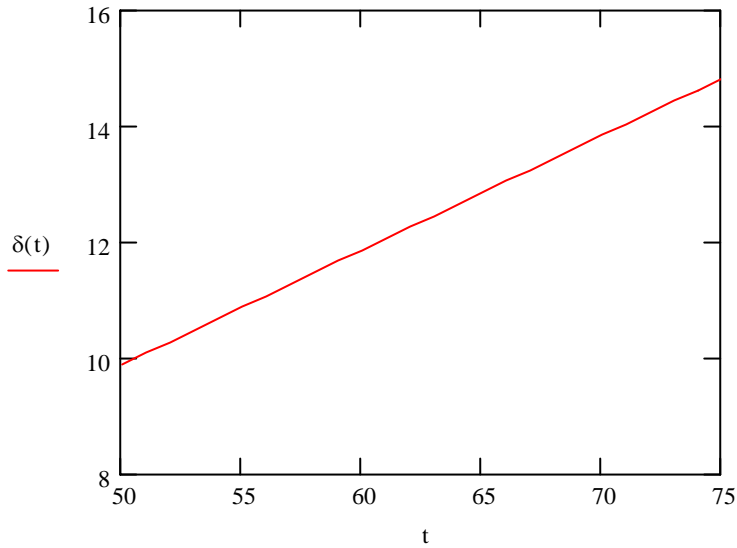
#### 2.3.1 Optimum Input Beam Displacement at the BS HR

##### 2.3.1.1 Maximum Transmission through BS, PR input

Maximum transmission through the BS, when the input is from the direction of the power recycling mirror (PR), occurs when the input beam is displacement laterally by the amount

$$\delta(t) := \frac{\Delta D(t)}{2} \cdot \cos\left(\frac{\pi}{4}\right)$$

The optimum lateral displacement depends only upon the thickness of the BS and is shown in Figure 2 for various thicknesses.



**Figure 2: Optimum offset of Input Beam**

### 2.3.1.2 Maximum Transmission through BS, SR input

Maximum transmission through the BS into the transmitted arm is obtained when the input beam from the signal recycling mirror (SM) is displaced laterally by the amount

$$\Delta y_t(t) := \Delta D(t) \cdot \cos\left(\frac{\pi}{4}\right)$$

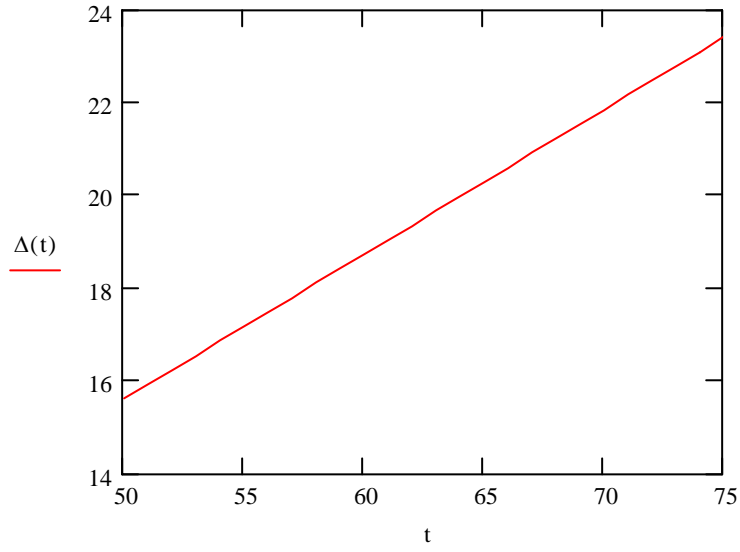
In this case, the input beam from the PR direction is also centered on the BS HR surface.

### 2.3.2 Lateral Displacement of Beam Through BS AR

The refracted beam transmitted through the AR surface of the BS undergoes a lateral displacement given by the following equation, which depends only upon the thickness of the BS and the fixed diffraction angle.

$$\Delta(t) := \frac{t \cdot \sin\left(\frac{\pi}{4} - \theta\right)}{\cos(\theta)}$$





**Figure 3: Lateral Displacement of Refracted Beam through BS**

### 3 Results

The following results were calculated with the input beam from the PR mirror centered on the BS HR surface. This minimizes the loss of the beam input from the SR mirror direction. The input power is 1 W, and the BS HR reflectivity is 50%. The total loss from both arms is the sum of the individual arm losses.

#### 3.1 Baseline BS

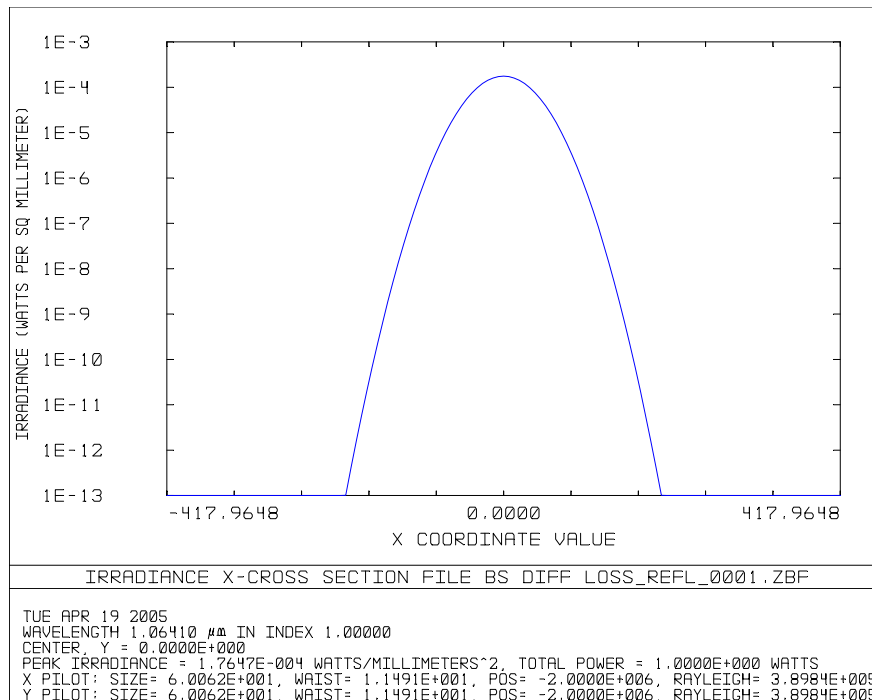
The Advanced LIGO baseline dimensions for the BS are:

$$t = 60 \text{ mm}$$

$$D = 350 \text{ mm}$$

##### 3.1.1 Input Gaussian Beam

The input Gaussian beam cross section from the power recycling mirror, at the BS HR surface, is shown in Figure 4. The spot size at the BS is 60mm. The beam has a waist of 11.49 mm inside the IFO arm at a distance  $z = 2005000$  mm.

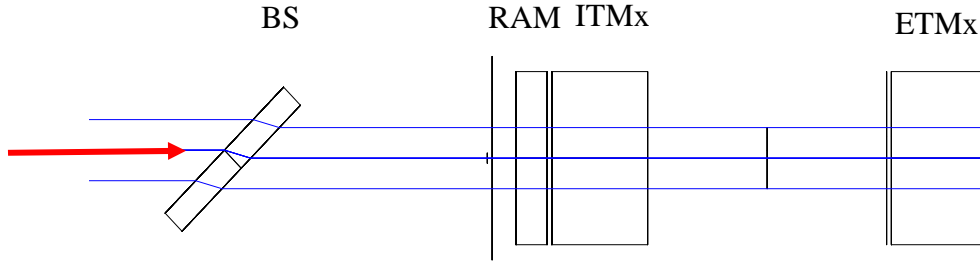


**Figure 4: Input Gaussian Beam**

### 3.1.2 Input Beam through Power Recycling Mirror

#### 3.1.2.1 Transmitted Arm

An optical schematic of the transmitted beam path from the power recycling mirror (PR), through the BS, through the RAM, through the ITM<sub>x</sub>, and out to the ETM<sub>x</sub> is shown in Figure 5.

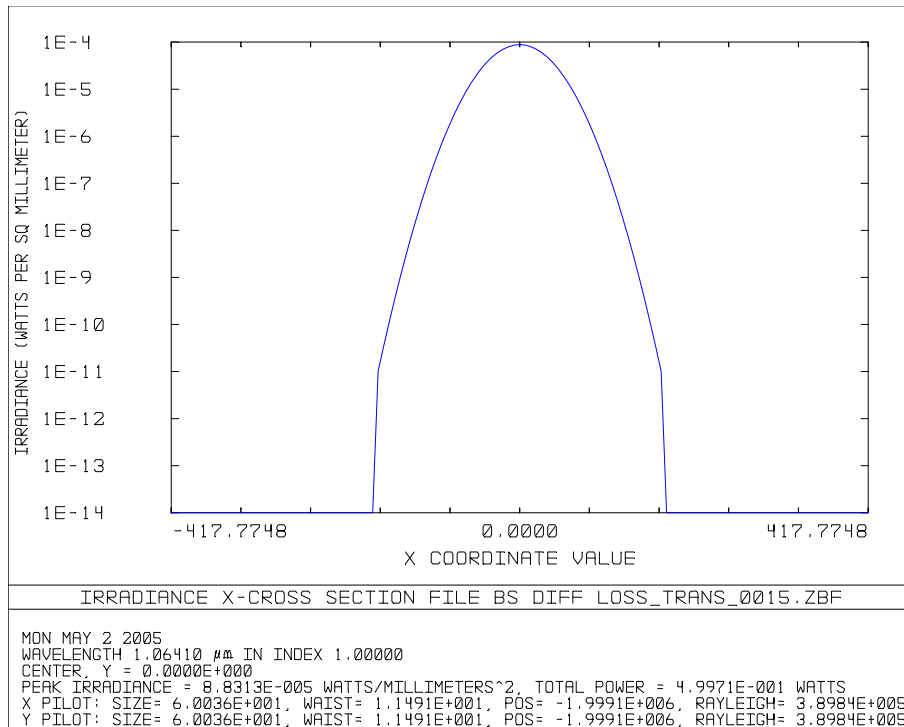


**Figure 5: Optical Schematic, Power Recycling Input Transmission through BS**

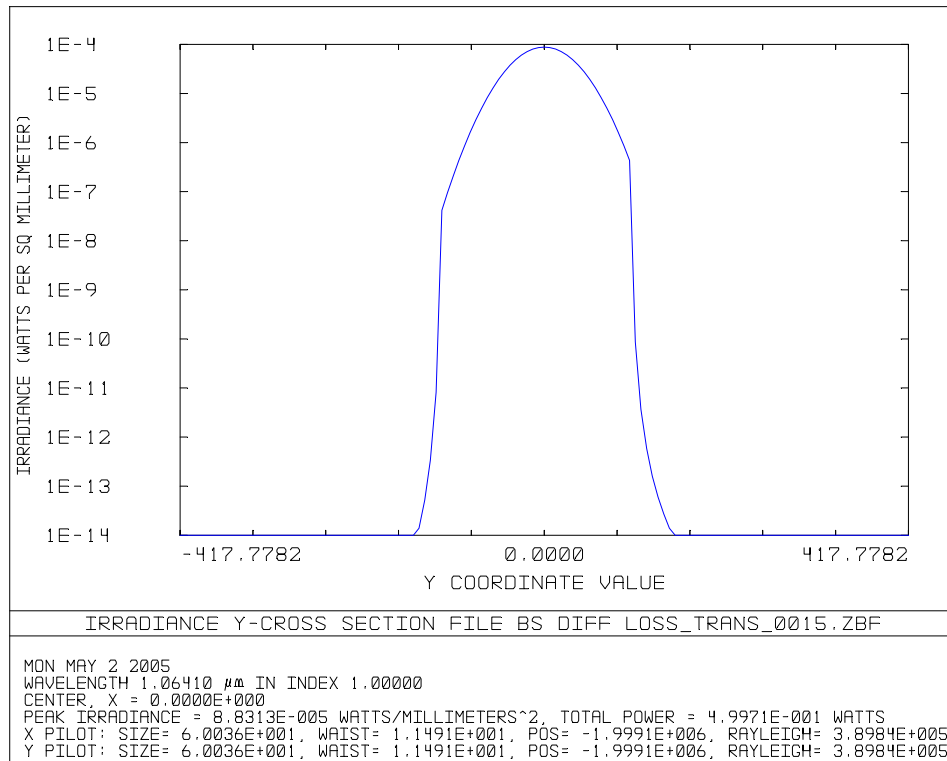
##### 3.1.2.1.1 Beam Cross-section at HR surface of ITM<sub>x</sub>, PR input, Transmitted Arm

The x (vertical) and y (horizontal) beam cross sections at a location immediately behind the ITM<sub>x</sub> are shown in Figure 6 and Figure 7 respectively. Note that the y beam cross section is vignetted by a greater amount than the x beam cross section because of the tilted BS.

The geometric power loss after traversing through the BS is 2.92E-4 W.



**Figure 6: X-cross Section at ITM<sub>x</sub> HR, PR Input, Transmitted Arm**



**Figure 7: Y-cross Section at ITMx HR, PR Input, Transmitted Arm**

### 3.1.2.1.2 Diffracted Power Loss around ETMx

The vignetted beam exhibits edge diffraction around the edges of the BS and the ITM. The diffracted beam is lost around the edges of the ETM, as shown in Figure 8 and Figure 9. Note that the lost diffracted power is greater in the y cross section.

The diffractive power loss at the ETMx is  $6.00E-5$  W, approximately 21% of the geometric loss.

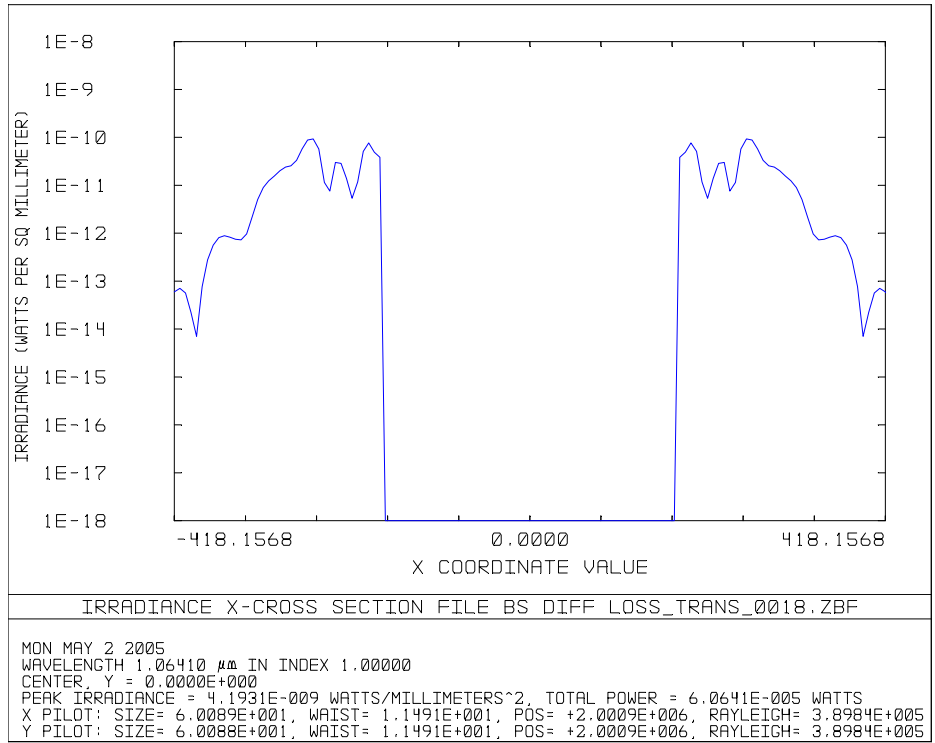


Figure 8: X-cross Section of Diffracted Beam around ETMx, PR Input, Transmitted Arm

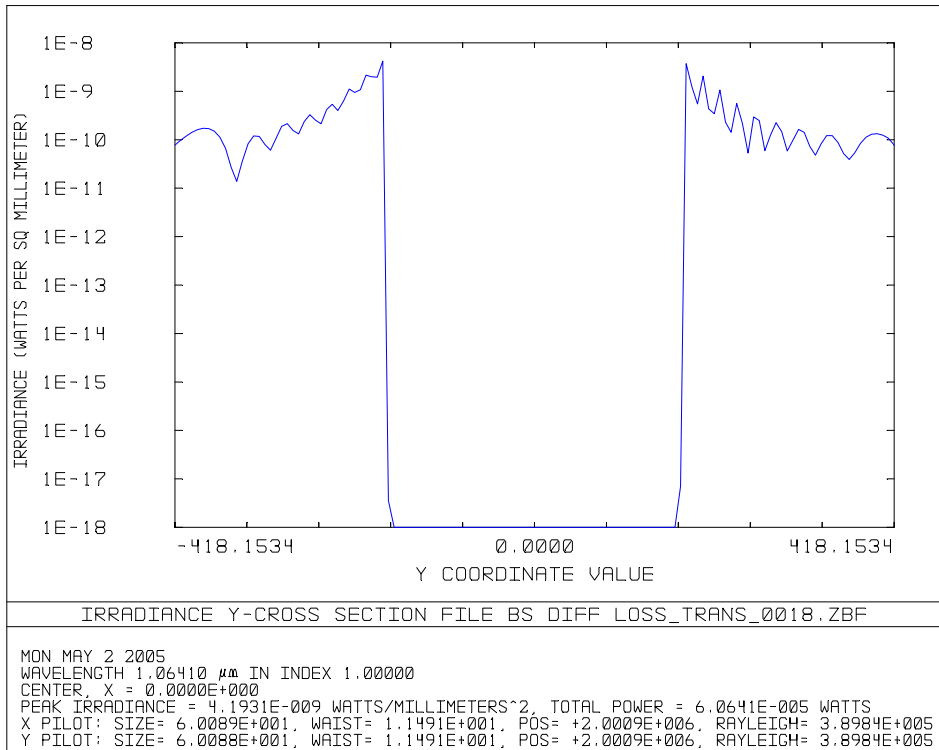
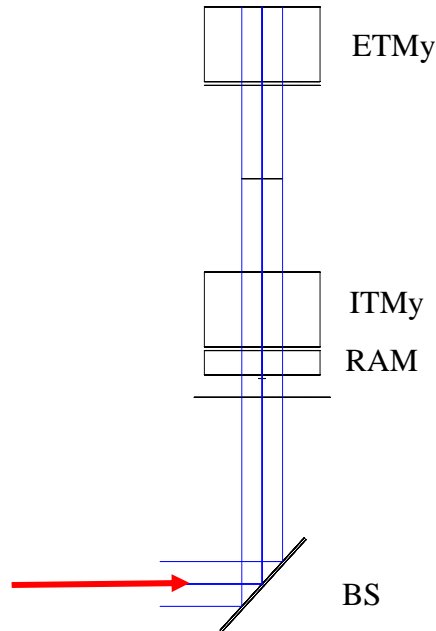


Figure 9: Y-cross Section of Diffracted Beam around ETMx, PR Input, Transmitted Arm

### 3.1.2.2 Reflected Arm

An optical schematic of the reflected beam path from the power recycling mirror (PR), reflecting from the HR surface of the BS, through the ITMy, and out to the ETMy is shown in Figure 10.

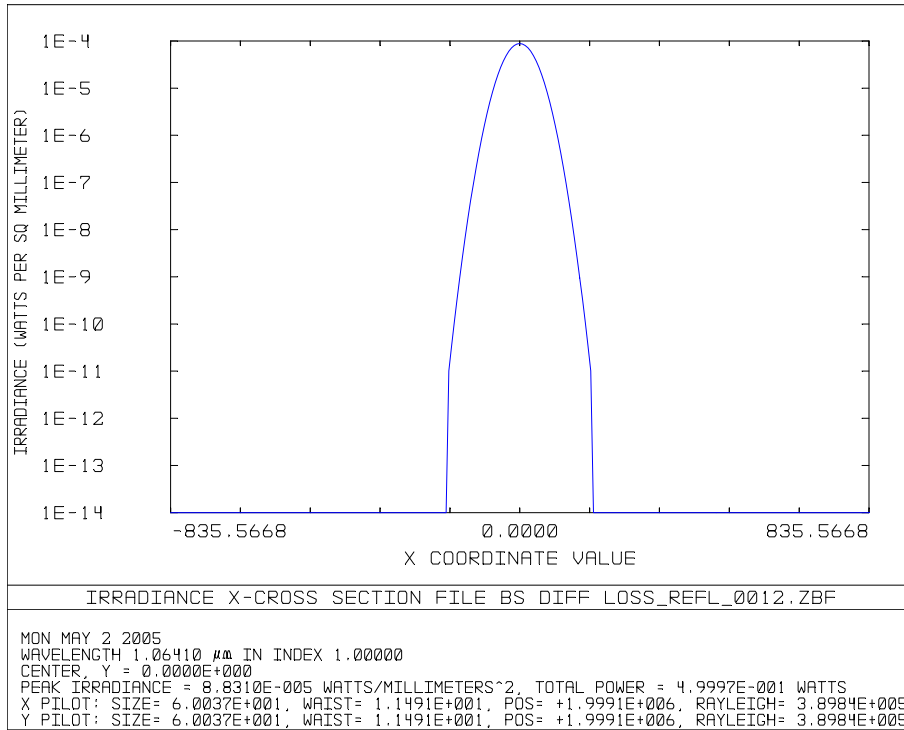


**Figure 10: Optical Schematic, Power Recycling Input Reflection from BS 50:50 Surface**

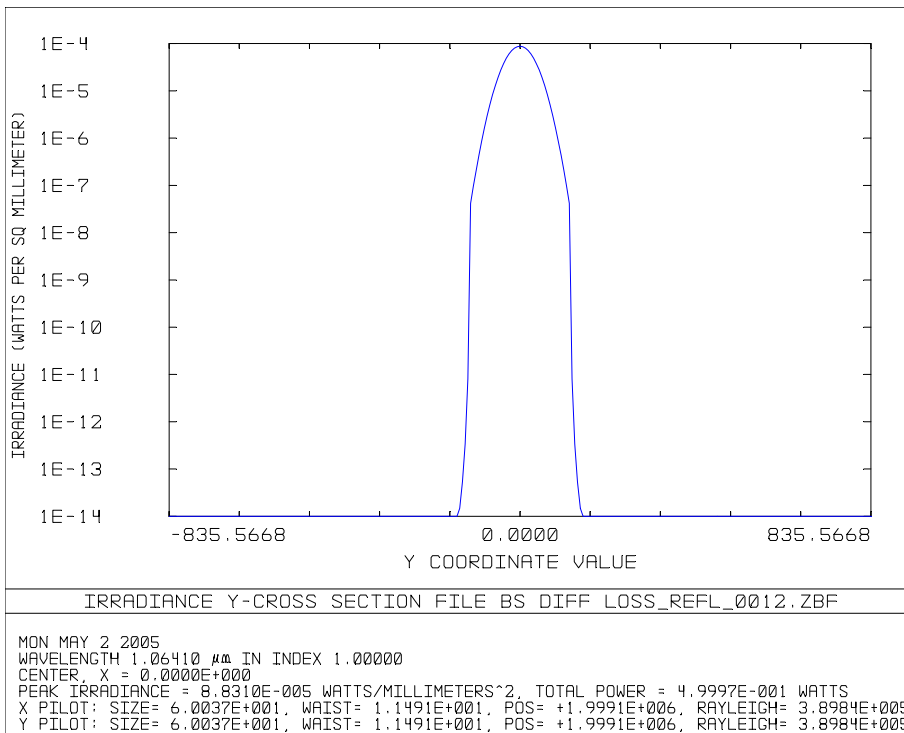
#### 3.1.2.2.1 Beam Cross-section at HR surface of ITMy, PR input, Reflected Arm

The x (vertical) and y (horizontal) beam cross sections at a location immediately behind the ITMy are shown in Figure 11 and Figure 12 respectively. Note that the y beam cross section is vignettted by a greater amount than the vertical beam cross section because of the tilted BS.

The geometric power loss after reflecting from the BS is  $3.2E-5$  W.



**Figure 11: X-cross Section at ITMy HR, PR Input, Reflected Arm**

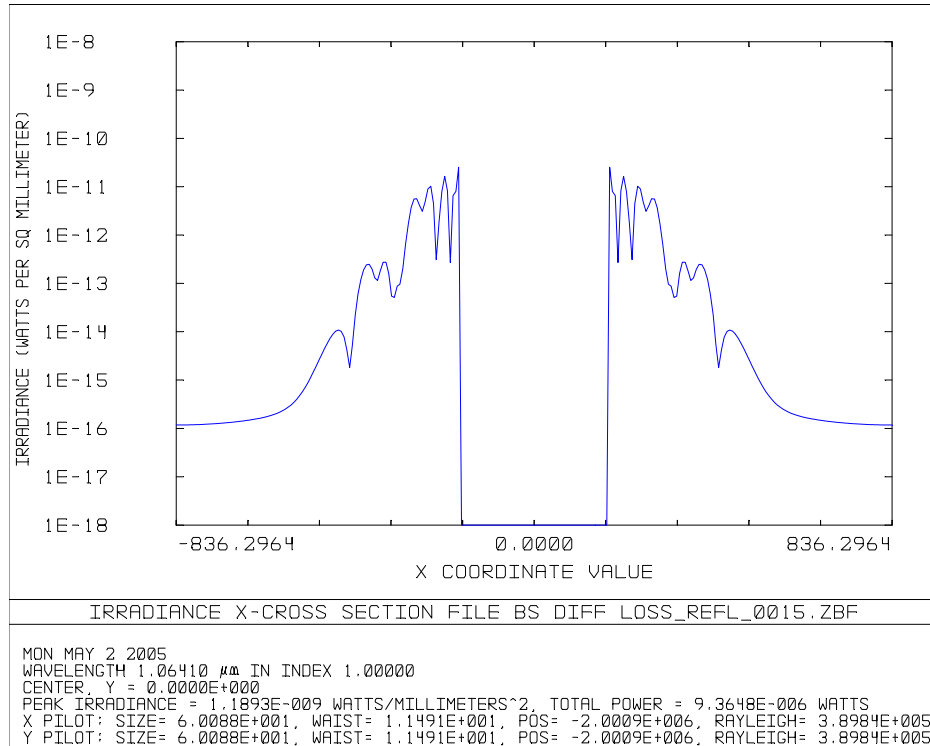


**Figure 12: Y-cross Section at ITMy HR, PR Input, Reflected Arm**

### 3.1.2.2.2 Diffracted Power Loss around ETMy

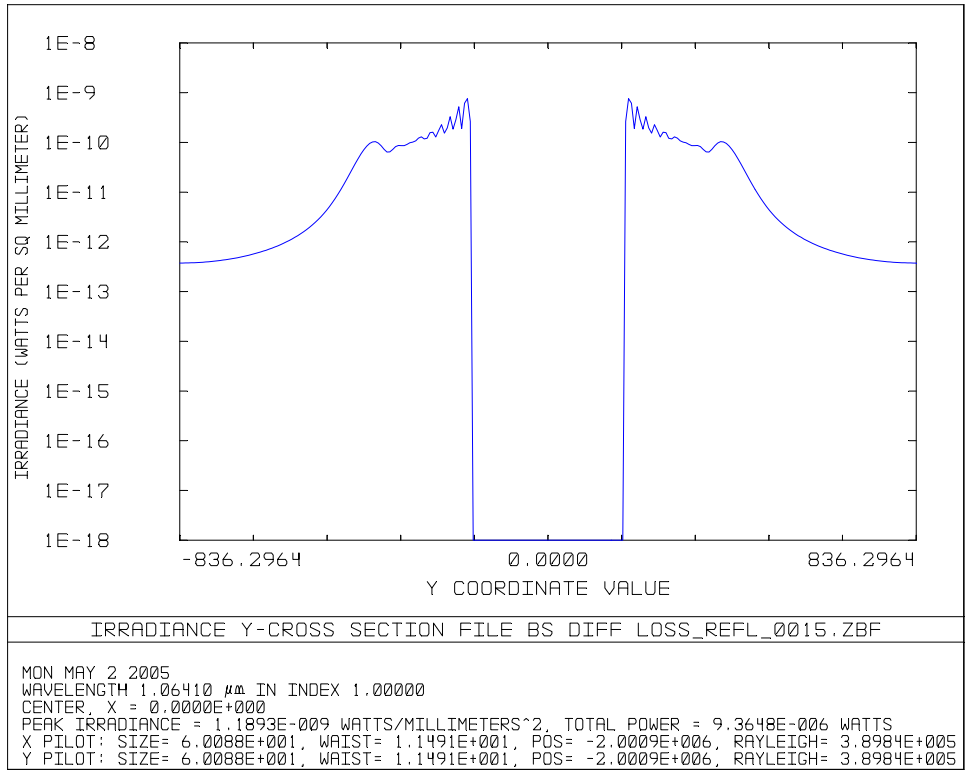
The vignetted beam exhibits edge diffraction around the edges of the BS and the ITM. The diffracted beam is lost around the edges of the ETM, as shown in Figure 13 and Figure 14. Note that the lost diffracted power is greater in the y cross section.

The diffractive power loss at the ETMy is  $1.00\text{E-}5$  W, approximately 31% of the geometric loss.



**Figure 13: X-cross Section of Diffracted Beam around ETMy, PR Input, Reflected Arm**





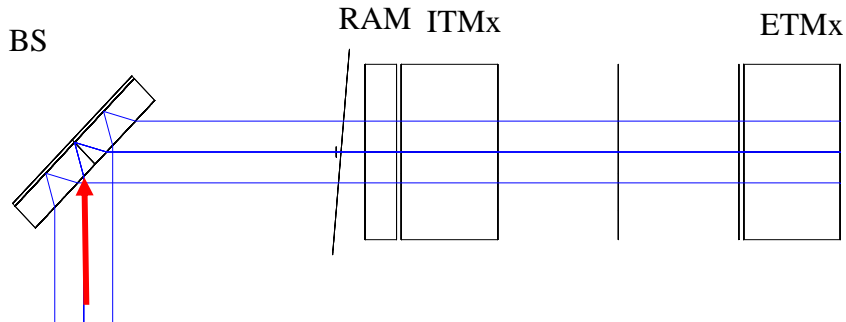
**Figure 14: Y-cross Section of Diffracted Beam around ETMy, PR Input, Reflected Arm**

The combined geometric and diffractive loss for both arms with PR input is 3.94E-4 W.

### 3.1.3 Input Beam through Signal Recycling Mirror

#### 3.1.3.1 Transmitted Arm

An optical schematic of the transmitted arm beam path with input from the signal recycling mirror (SR), reflecting from the HR surface of the BS, through the RAM, through the ITM<sub>x</sub>, and out to the ETM<sub>x</sub> is shown in Figure 15.

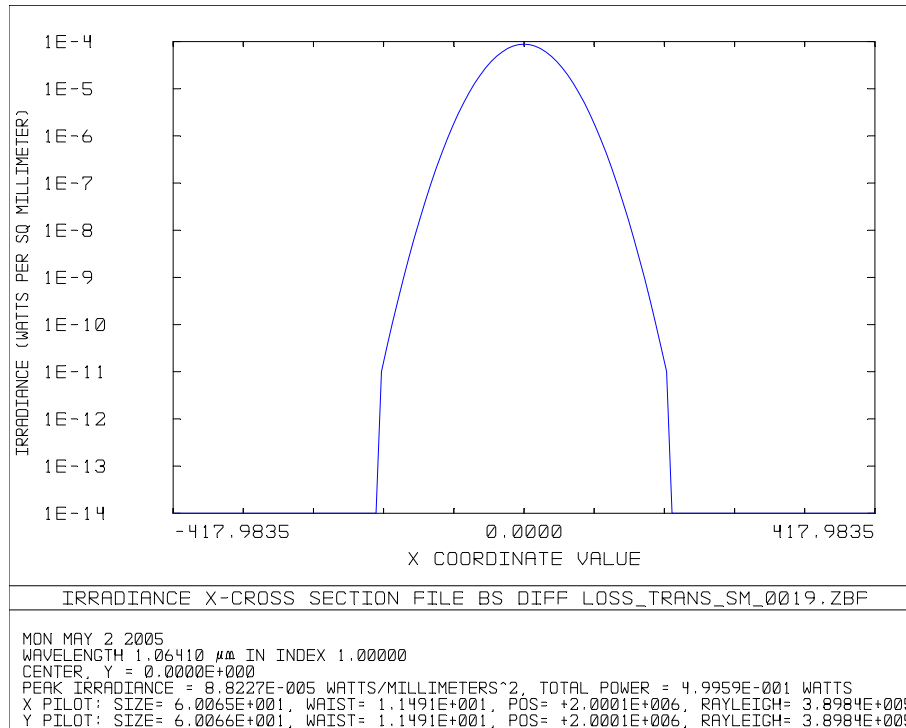


**Figure 15: Optical Schematic, Signal Recycling Input Reflection from BS 50:50 Surface**

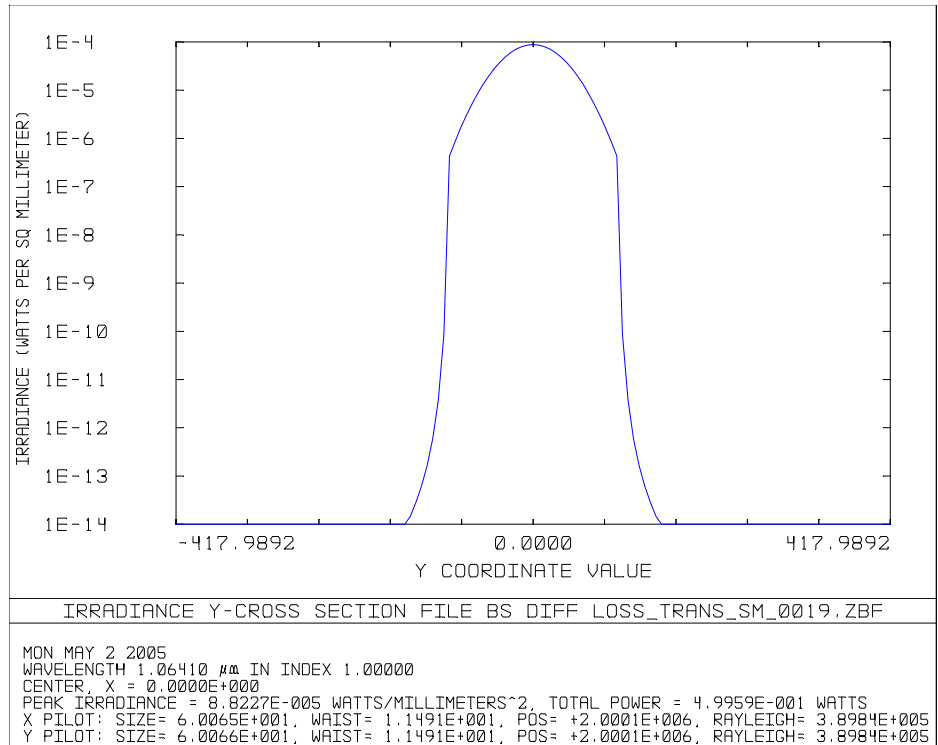
### 3.1.3.1.1 Beam Cross-section at HR surface of ITMx

The x (vertical) and y (horizontal) beam cross sections at a location immediately behind the ITMx are shown in Figure 16 and Figure 17 respectively. Note that the y beam cross section is vignettted by a greater amount than the vertical beam cross section because of the tilted BS; the vignetting is symmetric because the input beam was translated to the optimal position.

The geometric power loss from traversing through the BS is  $5.51\text{E-}5$  W.



**Figure 16: X-cross Section at ITMx HR, SR Input, Transmitted Arm**

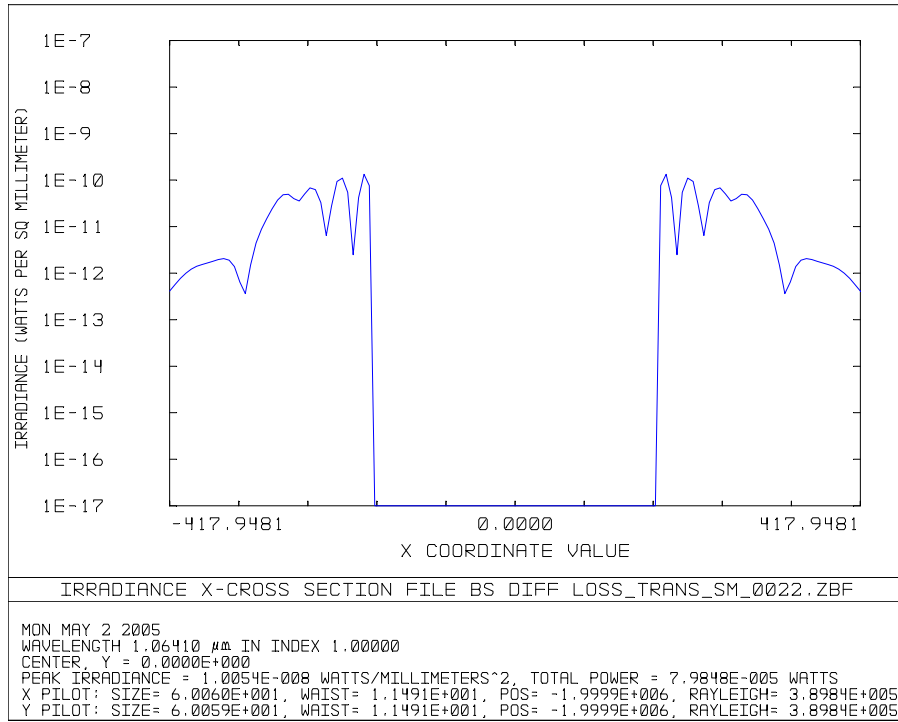


**Figure 17: Y-cross Section at ITMx HR, SR Input, Transmitted Arm**

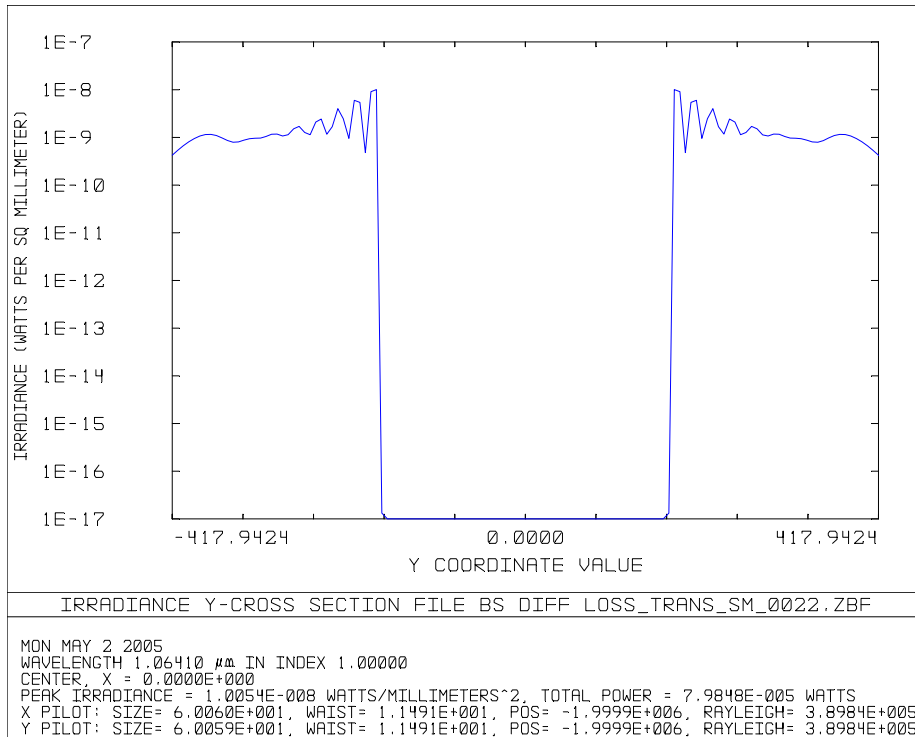
### 3.1.3.1.2 Diffracted Power Loss around ETMx

The vignetted beam exhibits edge diffraction around the edges of the BS and the ITM. The diffracted beam is lost around the edges of the ETM, as shown in Figure 18 and Figure 19. Note that the lost diffracted power is greater in the y cross section.

The diffractive power loss at the ETMx is 1.10E-4 W, approximately 25% of the geometric loss.



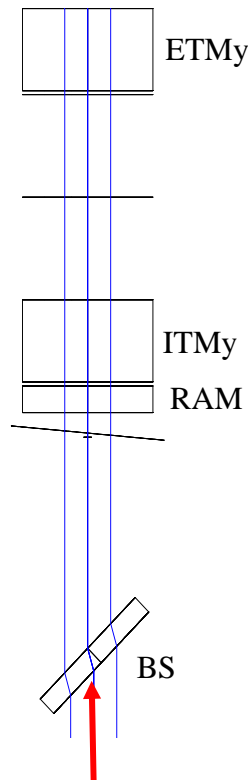
**Figure 18: X-cross Section of Diffracted Beam around ETMx, SR Input, Transmitted Arm**



**Figure 19: Y-cross Section of Beam around ETMx, SR Input, Transmitted Arm**

### 3.1.3.2 Reflected Arm

An optical schematic of the reflected arm beam path with input from the signal recycling mirror (SR), transmitting through the BS, through the RAM, through the ITMy, and out to the ETMy is shown in Figure 20.



**Figure 20: Optical Schematic, Signal Recycling Input Transmission through BS 50:50 Surface**

#### 3.1.3.2.1 Beam Cross-section at HR surface of ITMy, Reflected Arm

The x (vertical) and y (horizontal) beam cross sections at a location immediately behind the ITMy are shown in Figure 21 and Figure 22 respectively. Note that the y beam cross section is vignetted by a greater amount than the vertical beam cross section because of the tilted BS and is non-symmetrical because of the displacement of the beam at the BS AR surface.

The geometric power loss after traversing through the BS is  $2.92\text{E-}4$  W.

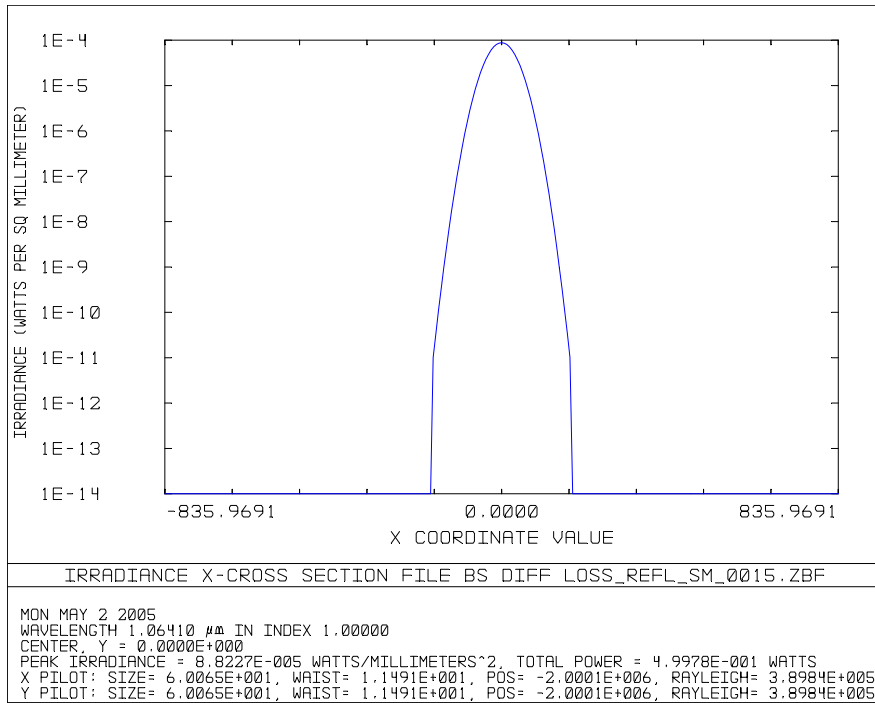


Figure 21: X-cross Section at ITMy HR, SR Input, Reflected Arm

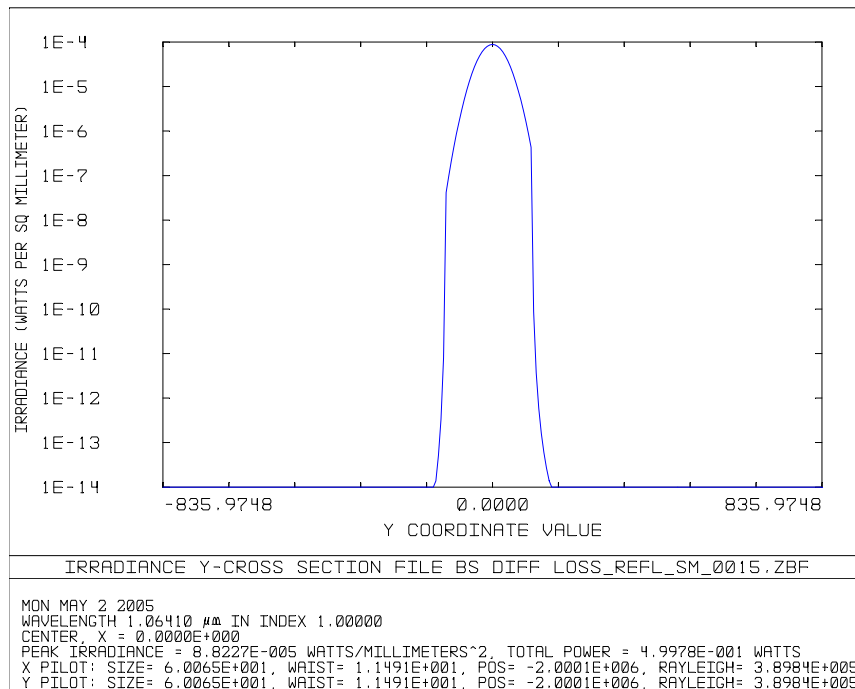
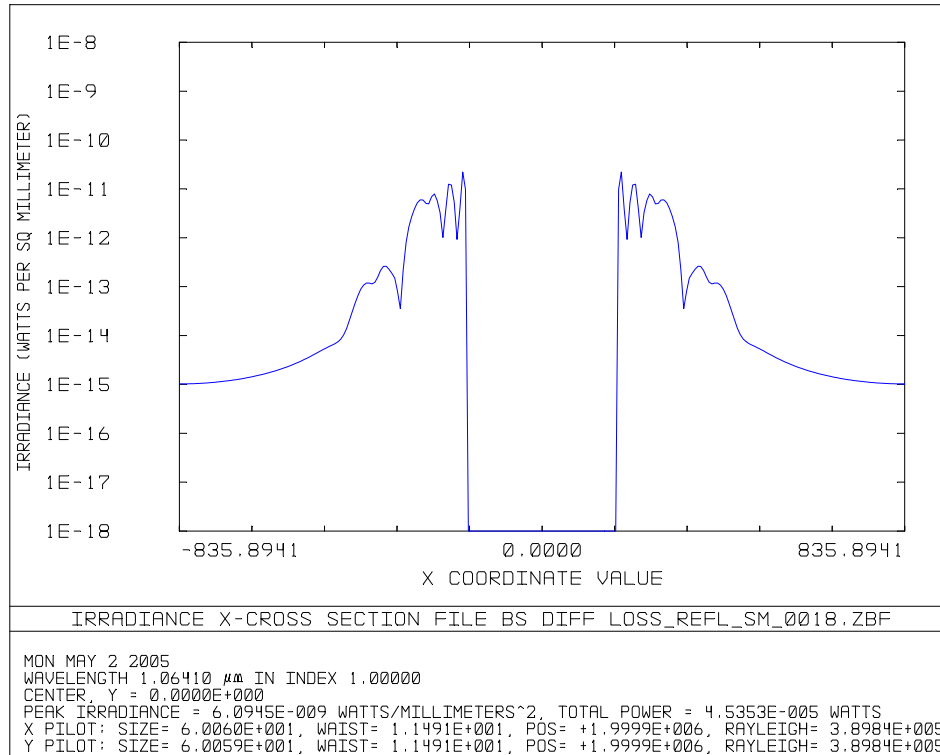


Figure 22: Y-cross Section at ITMy HR, SR Input, Reflected Arm

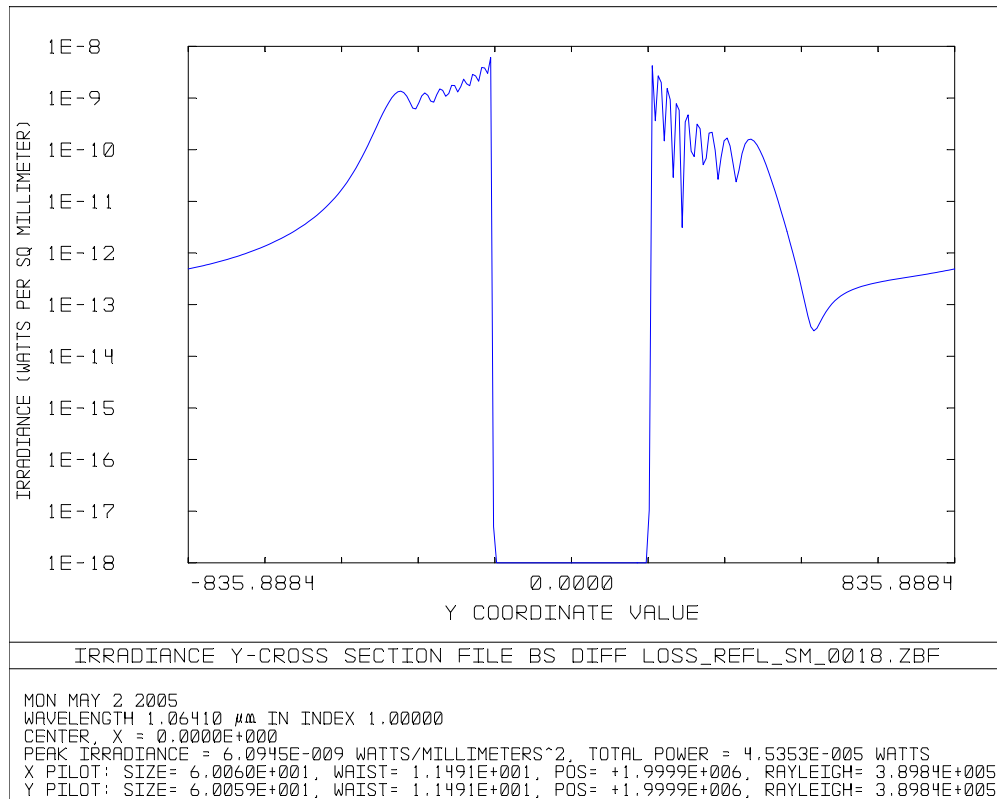
### 3.1.3.2.2 Diffracted Power Loss around ETMy

The vignetted beam exhibits edge diffraction around the edges of the BS and the ITM. The diffracted beam is lost around the edges of the ETM, as shown in Figure 23 and Figure 24. Note that the lost diffracted power is greater in the y cross section.

The diffractive power loss at the ETMy is  $6.00\text{E-}5$  W, approximately 21% of the geometric loss.



**Figure 23: X-cross Section of Diffracted Beam around ETMy, SR Input, Reflected Arm**



**Figure 24: Y-cross Section of Diffracted Beam around ETMy, SR Input, Reflected Arm**

The combined geometric and diffractive loss for both arms with SR input is  $1.01\text{E}-3$  W.

### 3.1.4 Loss as a Function of BS Thickness and Diameter

The geometric and diffractive power losses were calculated for a range of BS thicknesses between 50 mm to 72 mm, and a range of diameters between 350 mm to 400 mm. The calculations were performed for each arm separately with the beam input from the power recycling mirror (PR) and from the signal recycling mirror (SR). The results are shown in the following figures.

#### 3.1.4.1 Input Beam through Power Recycling Mirror

##### 3.1.4.1.1 Transmitted Arm Loss, PR Input



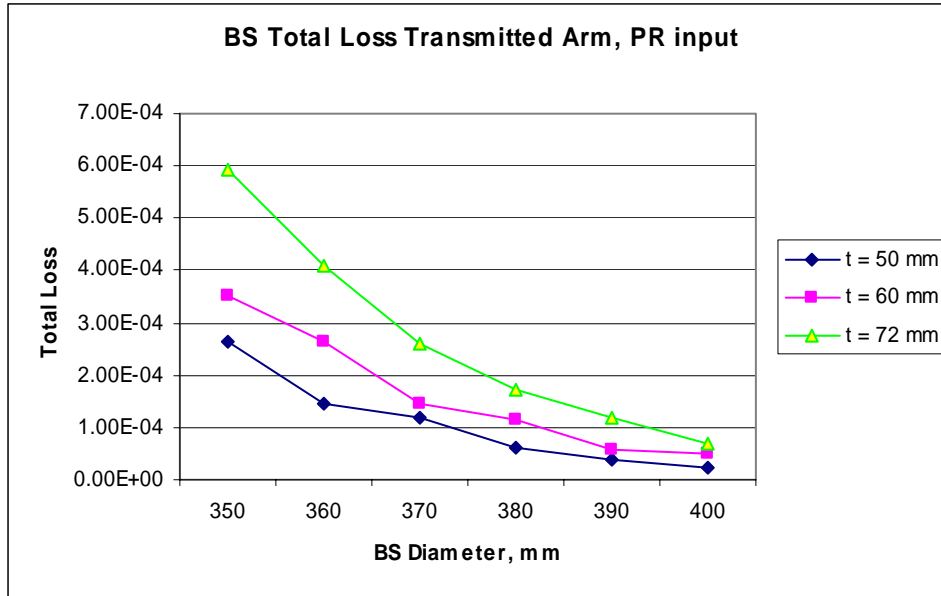


Figure 25: BS Total Loss Transmitted arm, PR Input

3.1.4.1.2 Reflected Arm Loss, PR Input

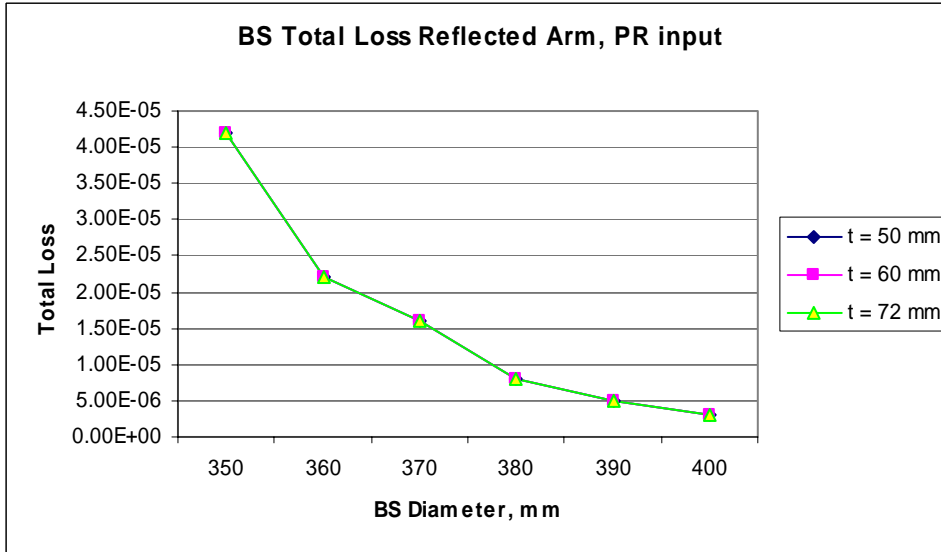


Figure 26: BS Total Loss Reflected arm, PR Input

3.1.4.1.3 Combined Loss, Both Arms, PR Input

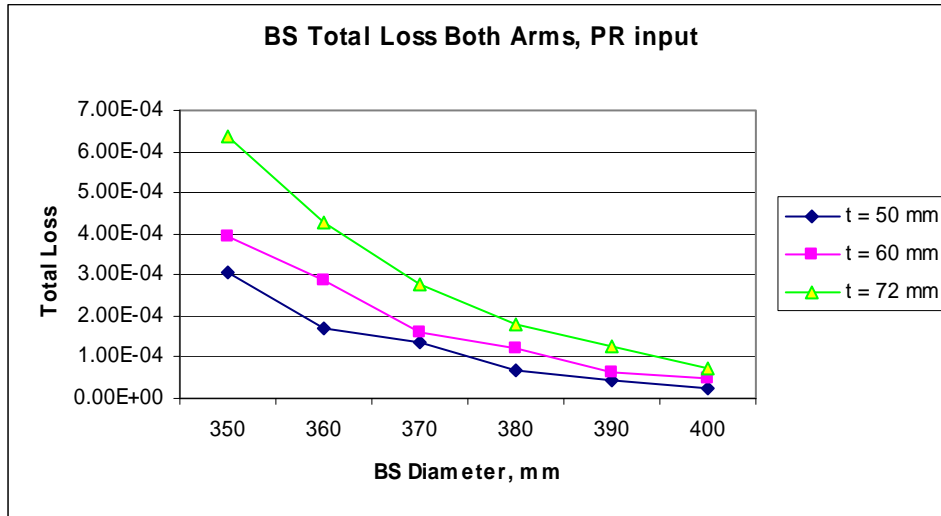


Figure 27: BS Total Loss Both Arms, PR Input

3.1.4.2 Input Beam through Signal Recycling Mirror

3.1.4.2.1 Transmitted Arm Loss, SR Input

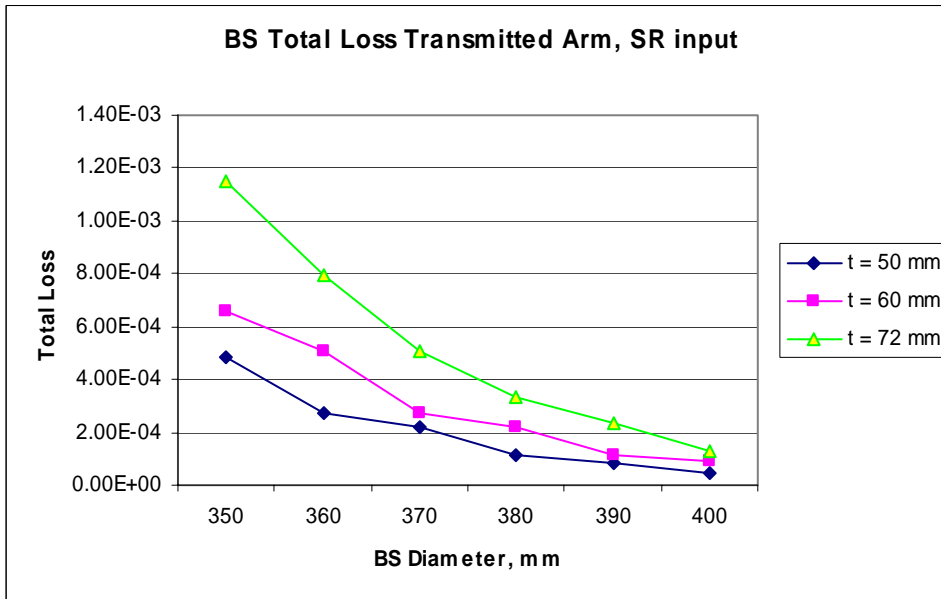


Figure 28: BS Total Loss Transmitted Arm, SR Input

3.1.4.2.2 Reflected Arm Loss, SR Input

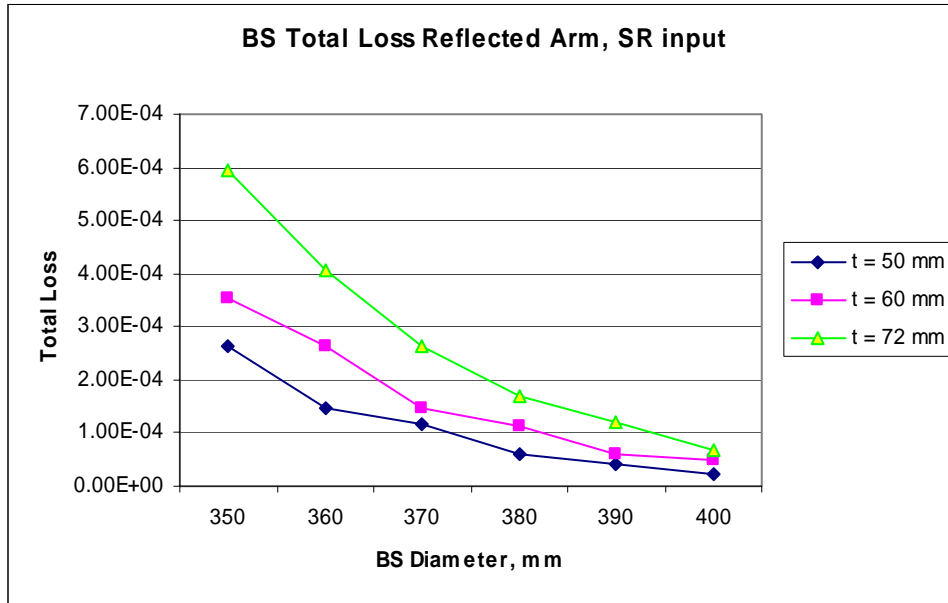


Figure 29: BS Total Loss Reflected Arm, SR Input

3.1.4.2.3 Combined Loss, Both Arms, SR Input

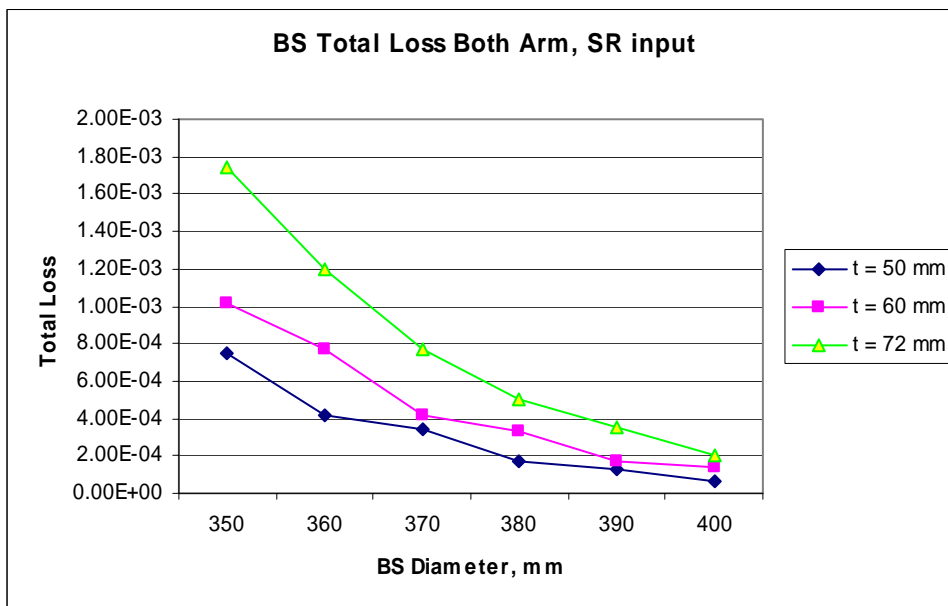


Figure 30: BS Total Loss Both Arms, SR Input

### 3.1.5 Loss from Bonding Flats

The combined geometric and diffraction losses from the placement of bonding flats on the vertical edges of the BS are shown in . The BS dimensions were taken to be  $D = 370$  mm, and  $t = 60$  mm. The “diameter of the bonding flat” is the horizontal distance between the left and right bonding flat.

#### 3.1.5.1 Transmitted Arm, SR Input

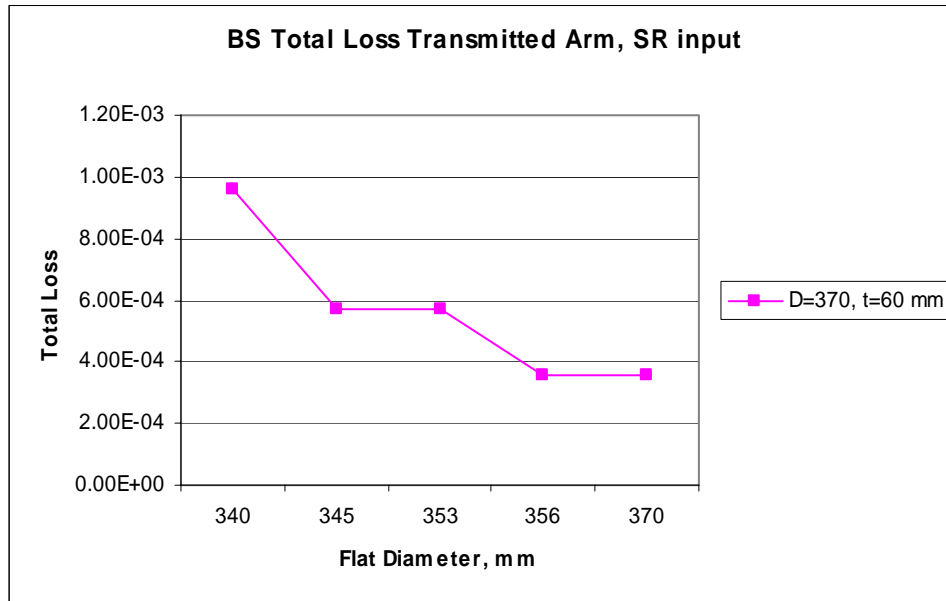


Figure 31: Power Loss in Transmitted Arm, SR Input from Flats

### 3.1.5.2 Transmitted Arm, PR Input

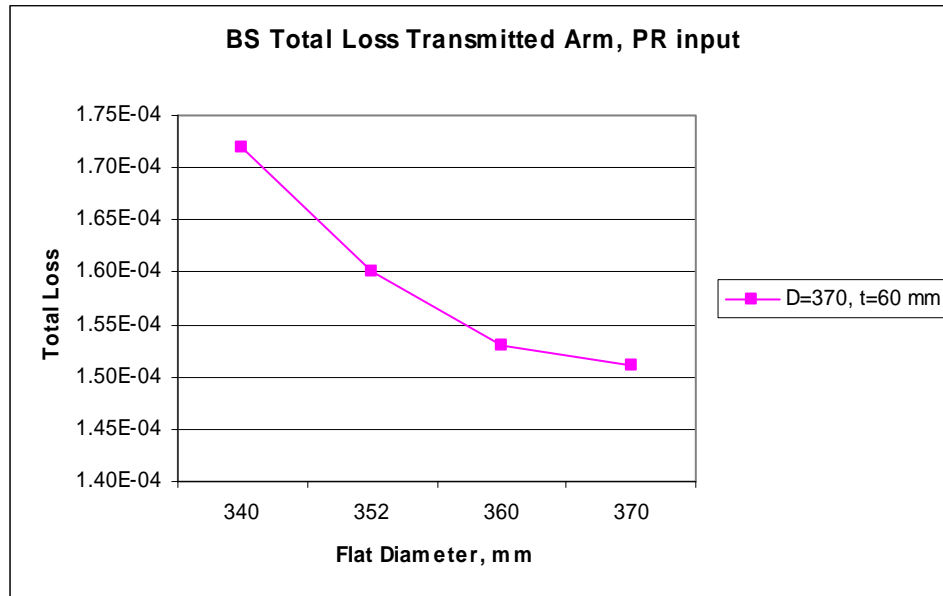


Figure 32: Power Loss in Transmitted Arm, PR Input from Flats

## 3.2 Alternative Design with Lens at RAM

Placing a 9000 mm radius of curvature on the back surface of the reaction mass (RAM) reduces the spot size at the BS from 60mm to 46.8 mm, as shown schematically in Figure 33. This smaller spot size allows a significant reduction in the diameter of the BS for the same total power loss.

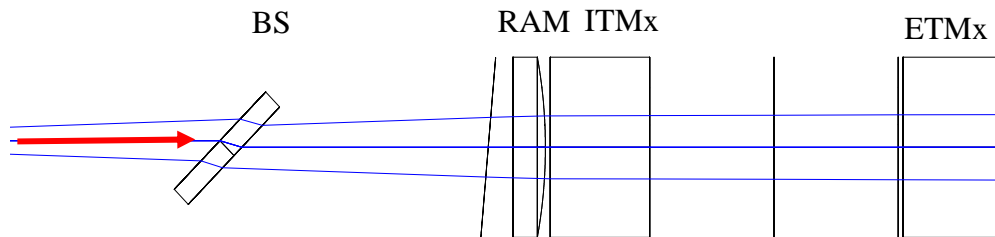


Figure 33: Optical Schematic, Alternative Design with Lens in RAM

### 3.2.1 Input Beam through Power Recycling Mirror

#### 3.2.1.1 Transmitted Arm Loss, PR Input

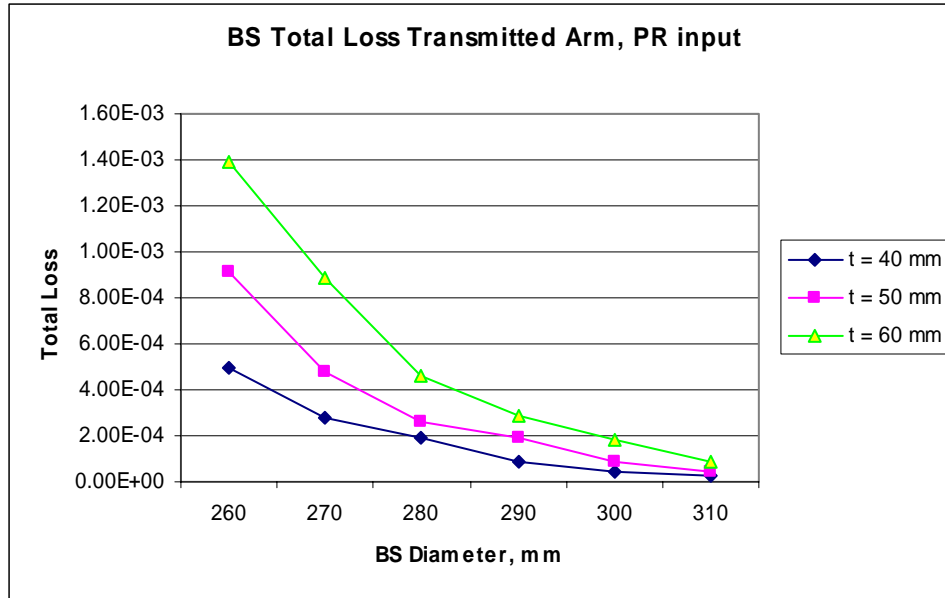


Figure 34: BS Total Loss Transmitted arm, PR Input

3.2.1.2 Reflected Arm Loss, PR Input

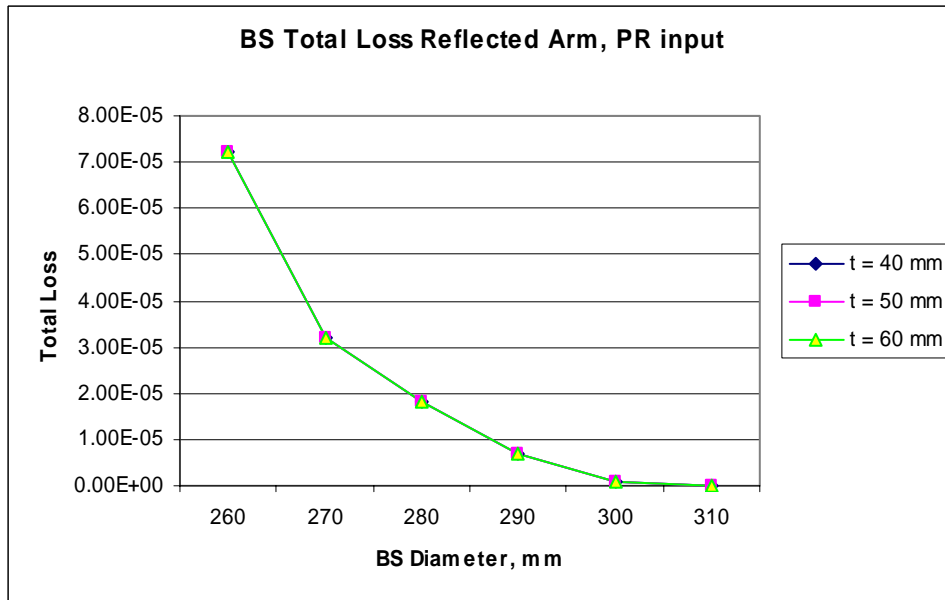


Figure 35: BS Total Loss Reflected arm, PR Input

3.2.1.3 Combined Loss, Both Arms, PR Input

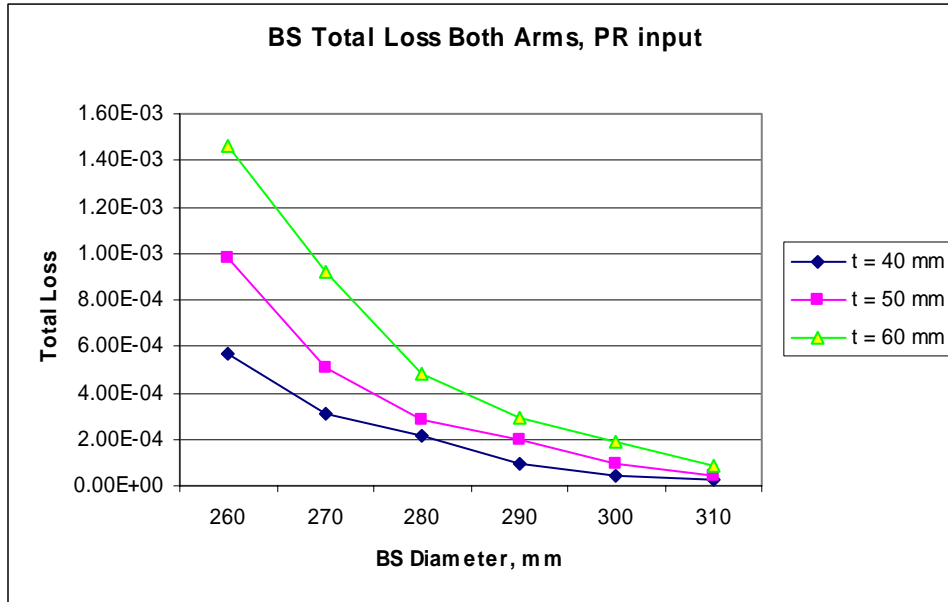


Figure 36: BS Total Loss Both Arms, PR Input

### 3.2.2 Input Beam through Signal Recycling Mirror

#### 3.2.2.1 Transmitted Arm Loss, SR Input

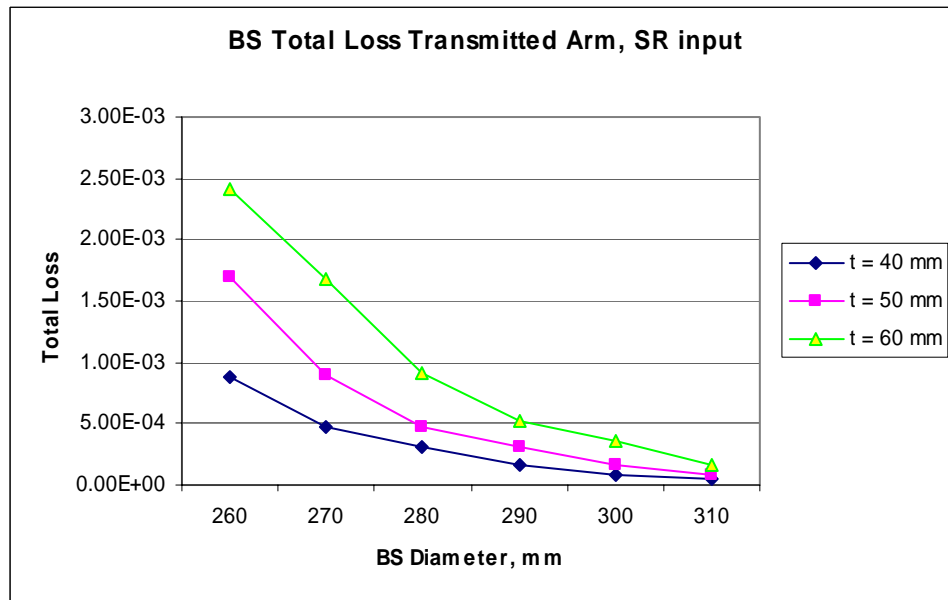


Figure 37: BS Total Loss Transmitted Arm, SR Input

#### 3.2.2.2 Reflected Arm Loss, SR Input

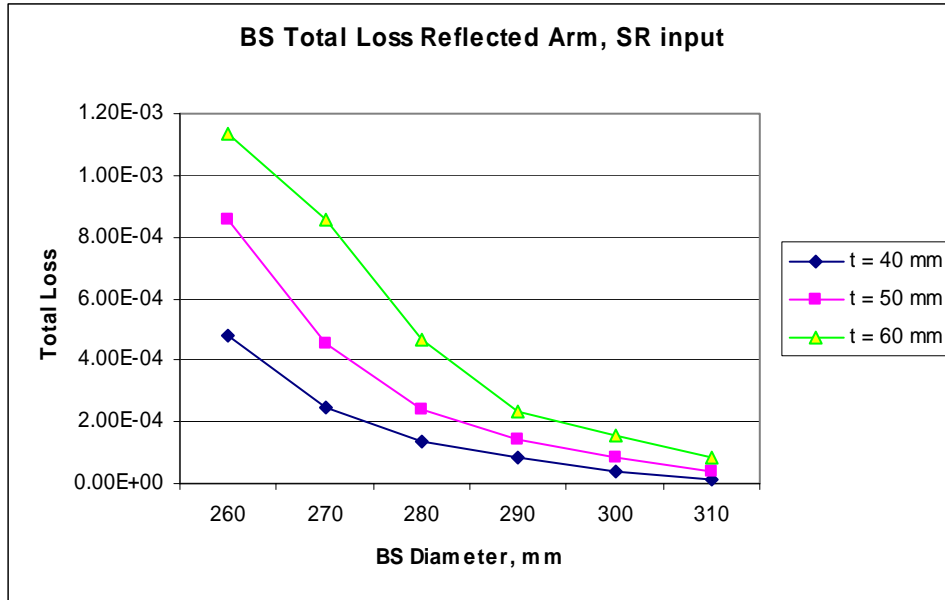


Figure 38: BS Total Loss Reflected Arm, SR Input

### 3.2.2.3 Combined Loss, Both Arms, SR Input

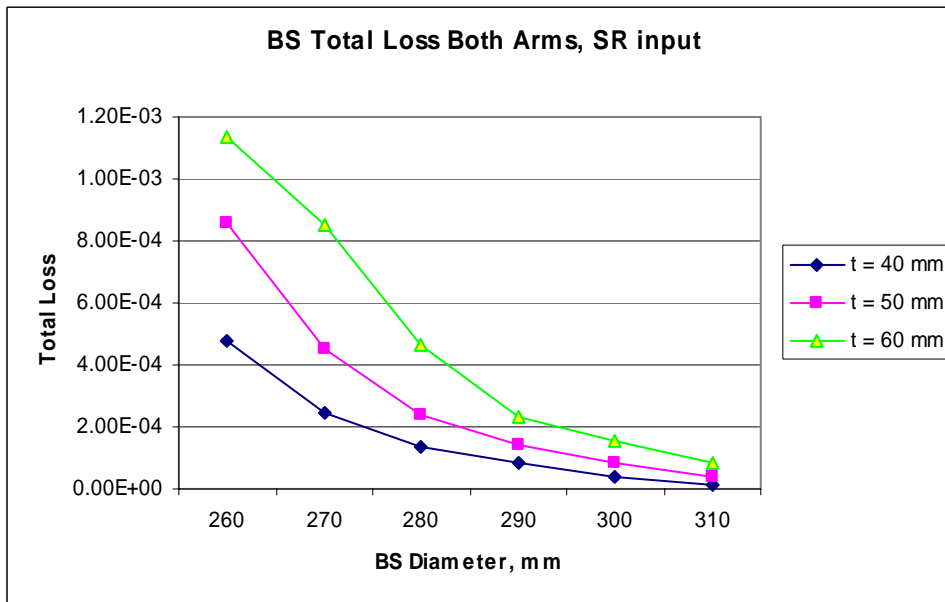


Figure 39: BS Total Loss Both Arms, SR Input



## 4 Conclusions

The geometric loss due to vignetting of the beam at the tilted BS surface accounts for more than 75% of the total power loss of the input beam.

The loss of the input beam from the SR mirror is approximately 2.5 times larger than the loss of the input beam from the PR mirror.

Centering the input beam from the PR mirror minimizes the total optical loss from both recycling mirror directions.

### 4.1 Standard Configuration: No Lensing at RAM

Table 1 summarizes the total geometric loss and diffractive losses from the two recycling mirror directions in making one traversal to the ETM for two possible BS dimensions, one of which is the Adv LIGO baseline configuration ( $t = 60\text{mm}$ ,  $D = 350\text{ mm}$ ).

The diameter/thickness ratio ( $D/t$ ) is also shown. For reference, the  $D/t$  ratio for the Initial LIGO BS is 6.25. The  $D/t$  ratio may affect the coating-induced sag of the BS HR surface.

The second configuration, with  $t = 60\text{ mm}$ ,  $D = 370\text{ mm}$  has a diffractive loss 2.4 times smaller than the baseline and has a  $D/t = 6.2$  that is comparable to the Initial LIGO configuration.

**Table 1 : BS Loss Comparison for Two Configurations**

BS DIMENSIONS	PR LOSS BOTH ARMS	SR LOSS BOTH ARMS	D/t
$t = 60\text{mm}$ , $D = 350\text{ mm}$	3.94 E-4	1.01 E-3	5.8
$t = 60\text{mm}$ , $D = 370\text{ mm}$	1.61 E-4	4.18 E-04	6.2

### 4.2 Alternate Configuration: 9000 mm Radius on Back Surface of RAM

Table 2 summarizes the total geometric loss and diffractive losses from the two recycling mirror directions in making one traversal to the ETM for two possible alternative BS dimensions.

The diameter/thickness ratio ( $D/t$ ) is also shown.

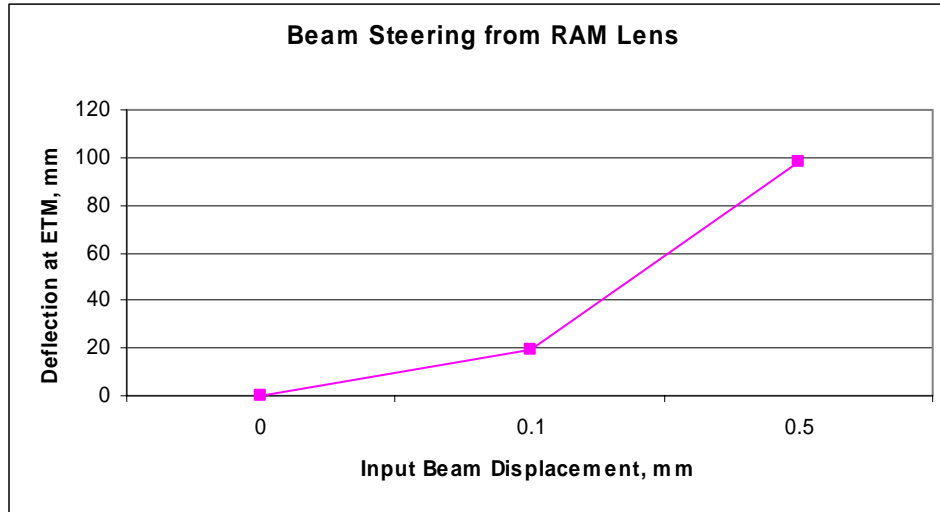
The second configuration, with  $t = 50\text{ mm}$ ,  $D = 300\text{ mm}$  has a total loss 5.6 times smaller than the first configuration.

**Table 2: Alternative Design, BS Loss Comparison for Two Configurations**

BS DIMENSIONS	PR LOSS BOTH ARMS	SR LOSS BOTH ARMS	D/t
$t = 40\text{mm}$ , $D = 260\text{ mm}$	5.69 E-4	1.18 E-3	6.5
$t = 50\text{mm}$ , $D = 300\text{ mm}$	9.10 E-5	2.18 E-04	6.0

### 4.2.1 Potential Problems with Lens at RAM

Placing a lens element at the RAM causes a lateral displacement of the beam through the RAM lens to steer the beam at the ETM, as shown in **Figure 40**.



**Figure 40: Beam Steering by RAM Lens**

This may place a severe restriction on the available positioning range of the beam at the ITM. Additionally, the non-parallel rays at the BS may cause astigmatism of the input and output beams.

### 4.3 Power Loss Due to Bonding Flats

Reasonable bonding flats appear to have a negligible effect on the power loss. A flat with a 7.5 mm radial cut, appears to cause approximately 20 microwatt power loss in the transmitted arm with the SR input, and approximately 5 microwatt power loss with the PR input for a 1W input to the IFO.