



**An additional  
Low Frequency  
Gravitational Wave  
Interferometric Detector  
for Advanced LIGO?**

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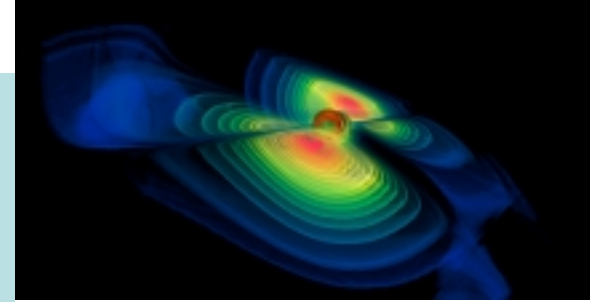
La Biodola 28<sup>th</sup> May 2003

LIGO-G030292-00-R

- In memory of Gianni
  - »  $\Omega$  20th of May 2003
- We conceived this idea together.

# New Scientific motivations

## Intermediate Mass Black Holes

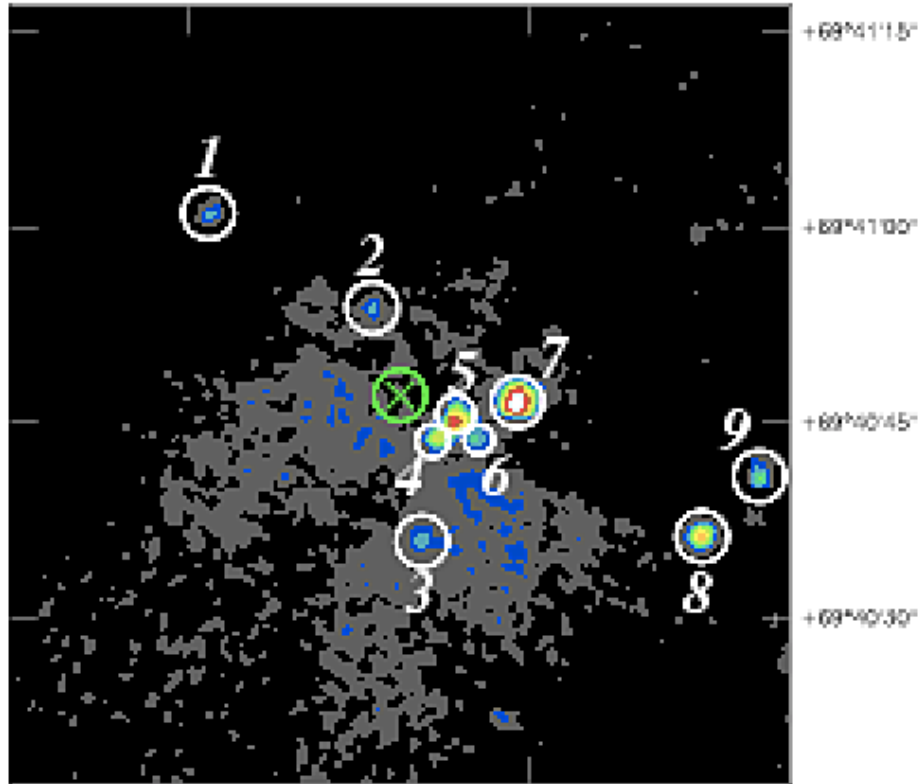


- Advanced LIGO was designed to detect ns-ns inspirals, mergers and inspirals
- New X-ray and optical observations performed after the design of Adv-LIGO indicate the presence of
- **new Lower Frequency GW sources**
- Data summary from Cole's Miller, based observations of galaxies and globular clusters
- <http://www.astro.umd.edu/~miller/IMBH/>
- [http://online.kitp.ucsb.edu/online/bhole\\_c02/miller/oh/05.html](http://online.kitp.ucsb.edu/online/bhole_c02/miller/oh/05.html)

# Chandra's observations of M82

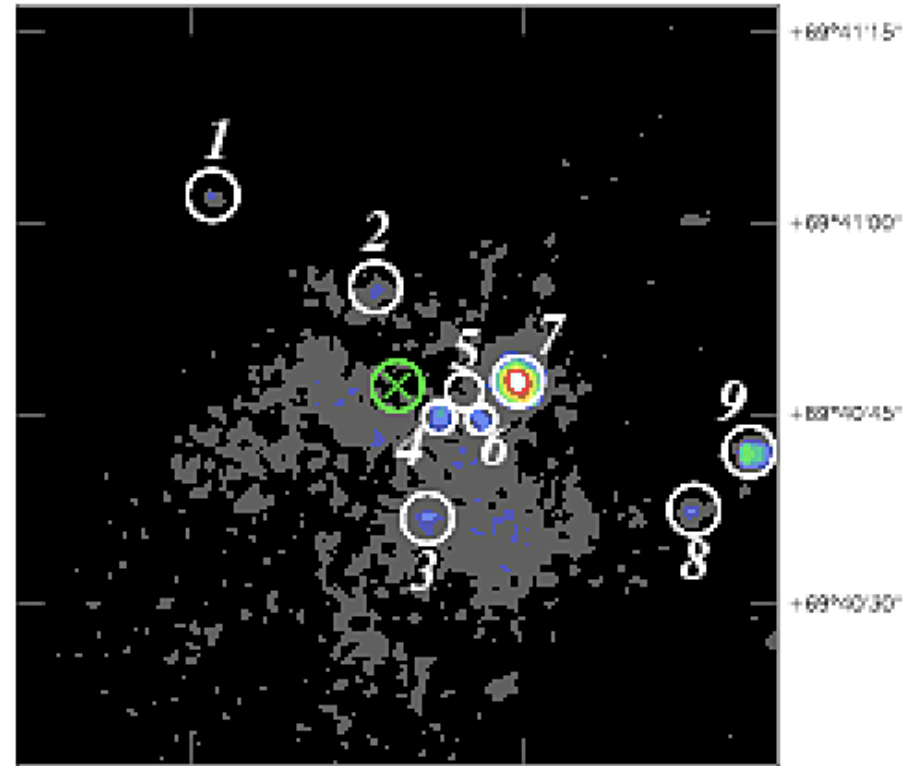
Matsumoto et al.

M82  
CHANDRA HRC HRC-I Exposure: 2788 s  
09°55'55" 09°55'50"



28 October 1999

M82  
CHANDRA HRC HRC-I Exposure: 17684 s  
09°55'55" 09°55'50"



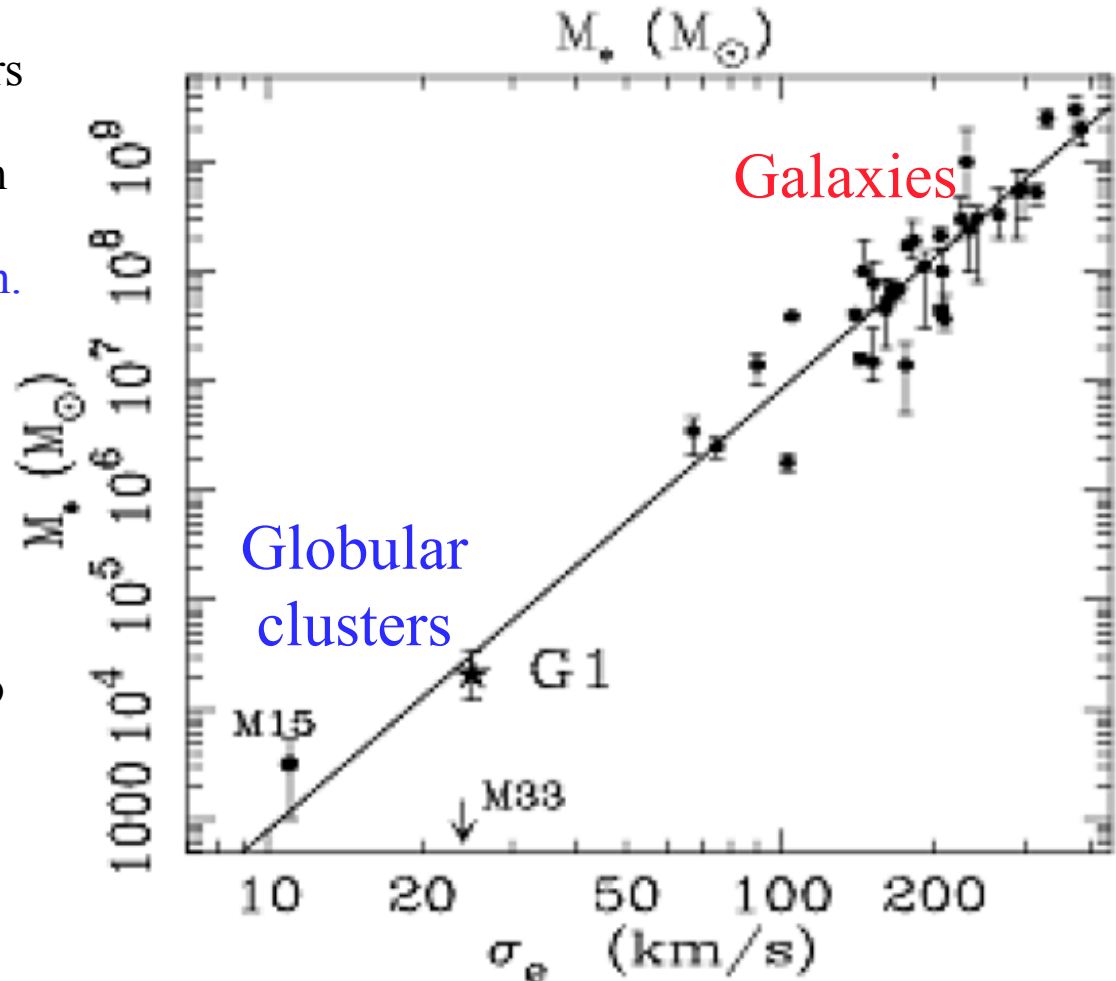
20 January 2000



# Concurring evidence of IMBH

## Central mass $M - \sigma$ relation

- In some Globular clusters the speed distribution of stars is compatible with central concentrated and invisible mass  $\sim 10^3$  s.m.
- Either a single, a binary or a cluster of BH must be at the center
- (Note: Statistics increased with respect to this figure)



# Observational facts

- Observed x-ray sources in globular clusters
- Eddington mass of sources  $30 \sim 10^3$  s.m.
- Emission implies a feeding companion
- So many couples imply high density in globular clusters (optically observed  $10^6$  stars/pc<sup>3</sup>)

# Optical observations:

inspirals may be occurring at a catalyzed pace

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- Systems high high mass slow down by dynamical friction ( $\tau=10\sim 50\text{My}$ ) and sink to the center of the cluster where they are induced to merge
  1. Density of  $\sim$  million stars per cubic parsec optically observed
  2. Encounters tend to equalize kinetic energy, heavy masses get slowed
  3. Mass segregation occurs
- Smaller stars collect kinetic energy and angular momentum and export them to the periphery or out of the cluster
- Encounters of binaries with singles tend to tie and tighten up the bigger guy and fling out the smaller of the three

# Optical observations: Swirl in clusters

- Swirl is observed in the core stars around central hidden mass
- But
- Frictional braking would rapidly eliminate the observed swirl!
- Explanation (controversial but growing evidence)
- Core stars around central BH cluster can soak angular momentum while hardening massive BH binaries or clusters at the center
- Is swirl a catalyzed inspiral Smoking gun?
- Coalesce may ensue at rapid rate!  $\sim 10\text{My}$  not Gy !!!!





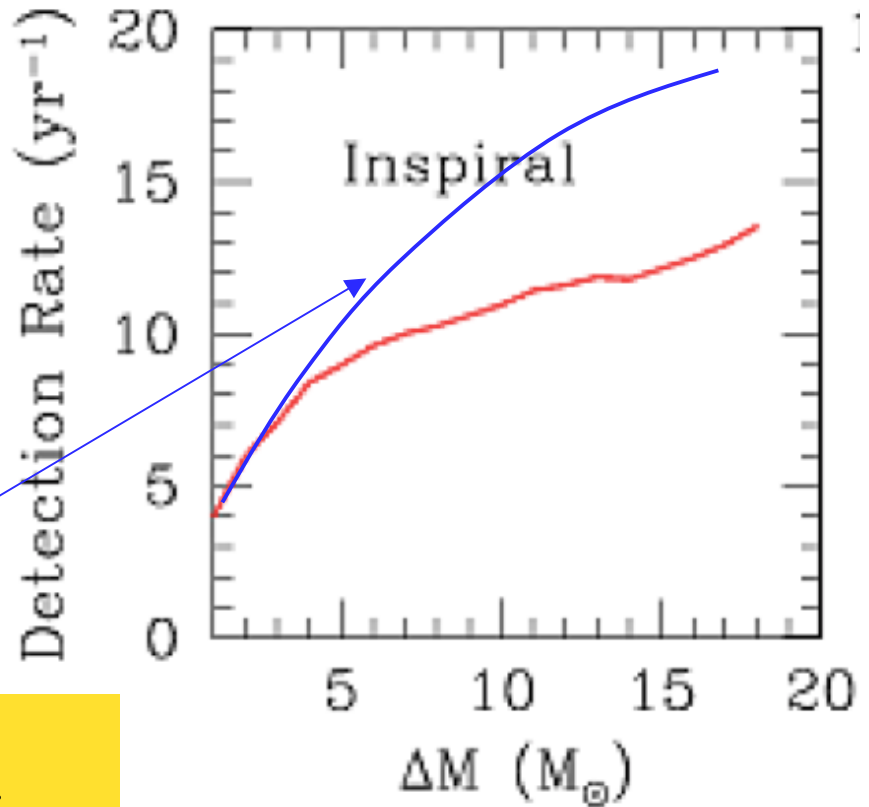
# Signal Detection



- The **G W signal** from the above mentioned and other sources will be **detected** with **Interferometric Detectors**
- Study of Full Relativistic regimes (BH merger and ringdown) require **sensitivity in the 100 Hz region.**
- **Detection** of the signal in **the inspiral phase** require **sensitivity in the 10 Hz region.**

# Predicted inspiral rate

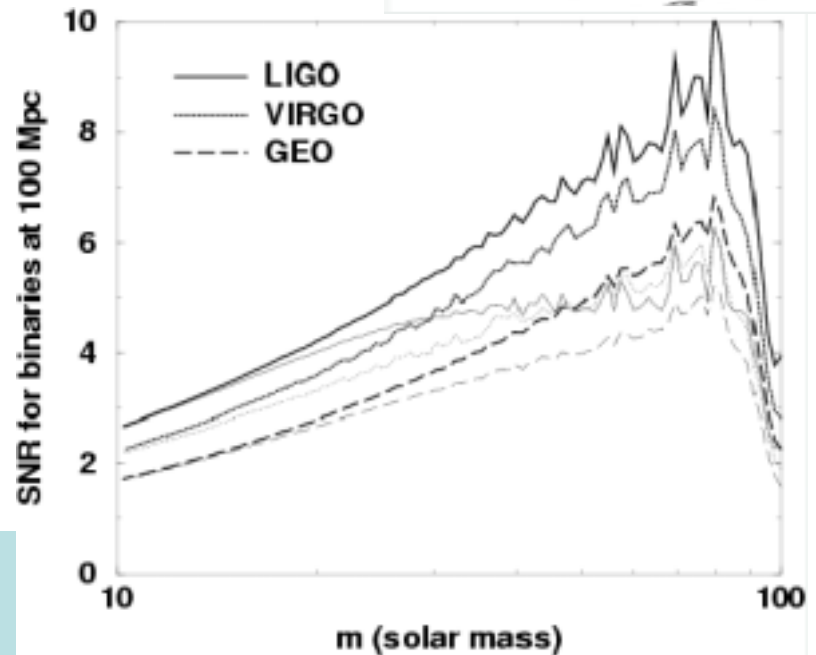
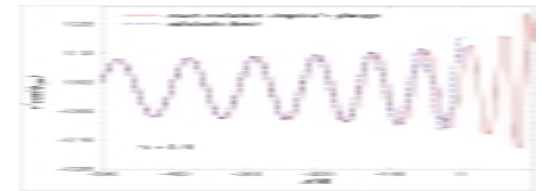
- Assuming accretion of objects starting from a  $10 M_{\text{sun}}$  BH
- Estimation for Adv-LIGO
- Adv-LIGO would preferentially see the initial accretions
- LF-GWID would see many more of these because of smaller effect of the merger frequency cutoff



•Cole Miller  
•Very preliminary

# Template difficulties

- Templates allow optimized filter matching only up to a certain frequency
- **Templates fail close to mergers thus strongly reducing the S/N ratio**
- **The higher the inspiral mass, the lower the cutoff frequency thus reducing the template effectiveness and the effective detection range**
- Number of templates must **grow from 25 to 10,000** (not counting BH spins) to recover the S/N from the last few orbits
- **Unfeasible without triggering**
- LF-GWID can **trigger at LF**
- Can apply all templates on **follow-up at HF** measurements of mergers and ringdowns

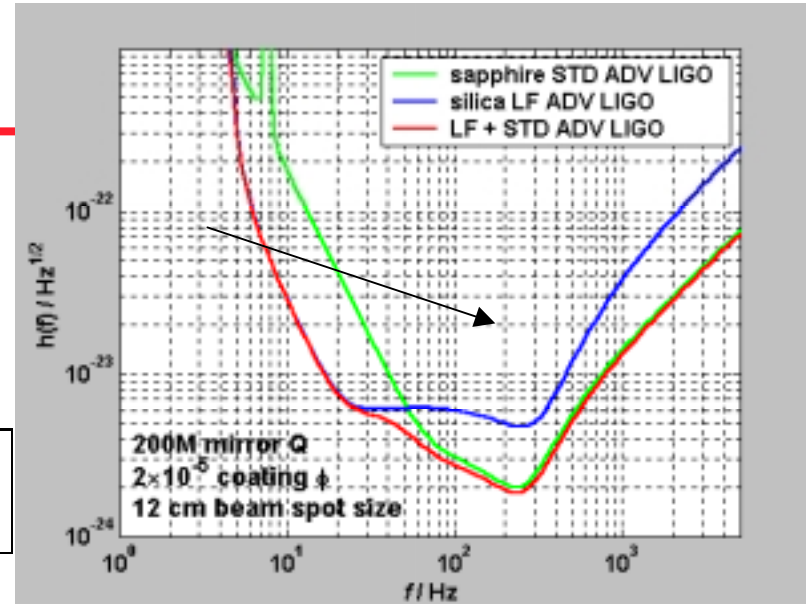




# In numbers

Integrating signal to noise with template,  
on full spectral range

up to  $f_{\max} = 99 \text{ Hz} / (1+z) * (20 M_{\text{sol}} / M)$  Lost S/N



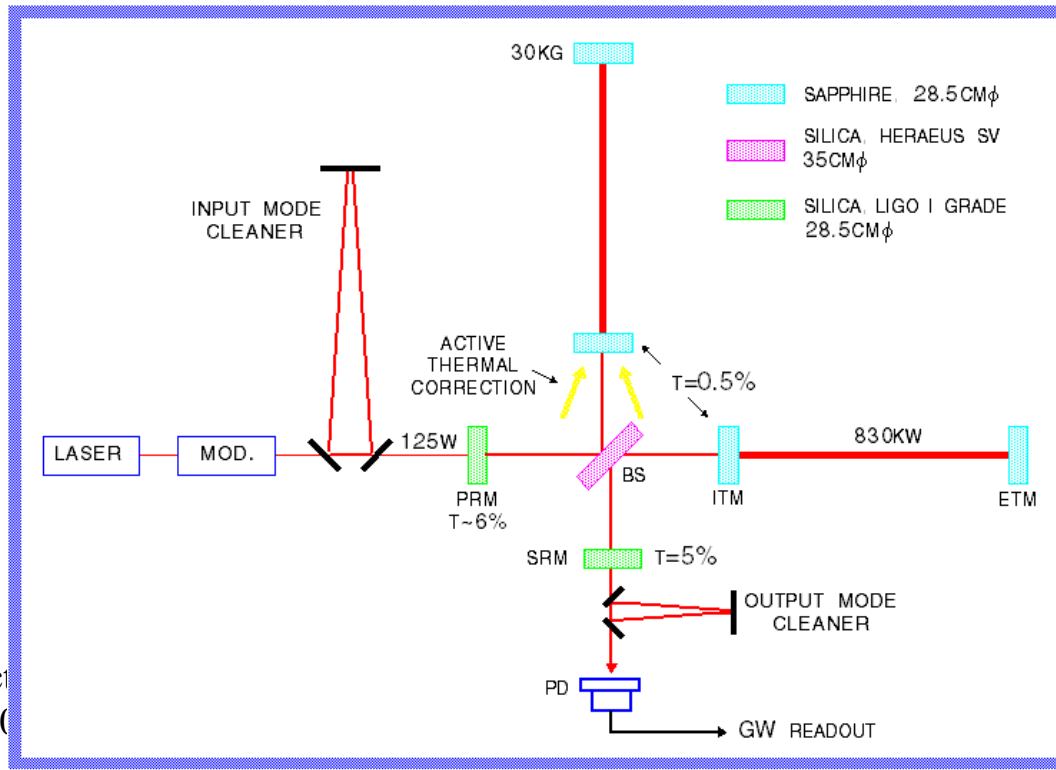
Inspirational mass	ADV-LIGO HF		LF GWID (w. SR)	
1.4+1.4	4.3	0 %	4.5	0 %
	4.4		4.6	
10+10	21.8	20 %	22.8	0 %
	17.5		22.9	
30+30	54.6	80 %	57.1	14%
	10.7		49	
50+50	83.5	95 %	87.4	31 %
	4.1		60	

# Technical feasibility

- Low frequency GW sensitivity is of great **astrophysical interest**
- Advanced LIGO is foreseen and optimized to cover **HF** signals should not be diverted
- Cannot be optimized for LF without some significant changes
  - Reduce beam power and different finesse (rad. Pressure)
  - Use Fused Silica instead of Sapphire mirrors (bulk TN)
  - Use Supersized, double weight, mirrors (coating TN, rad. Pr)
  - Use Double length suspensions (susp. TN)
- Need separate and specialized **Low and High Frequency** interferometers

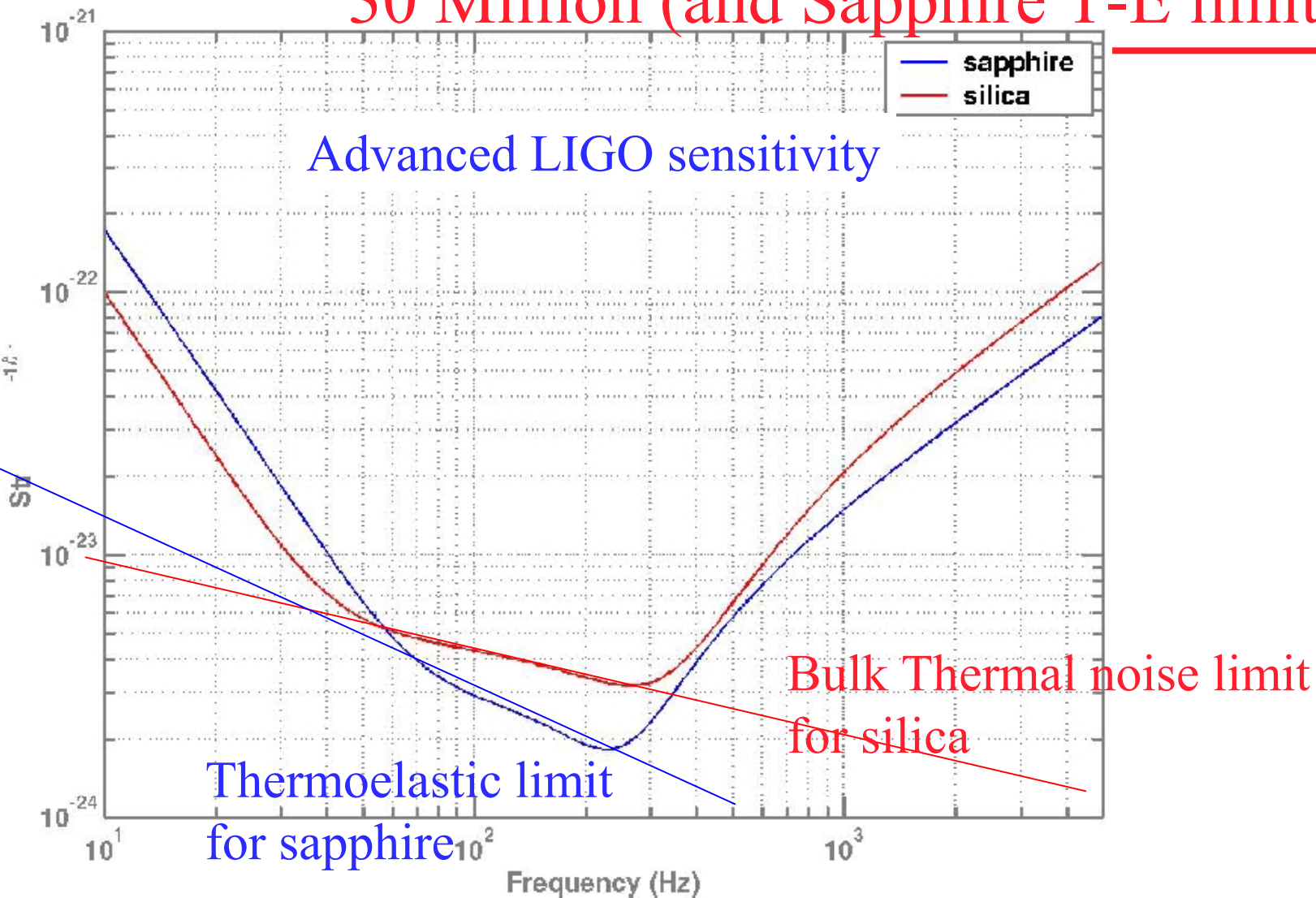
# Building a LF optimized interferometer

- Choice of materials and technologies





This curve was drawn when Fused silica was believed to have a Q-factor of 30 Million (and Sapphire T-E limited)



# The new TN situation

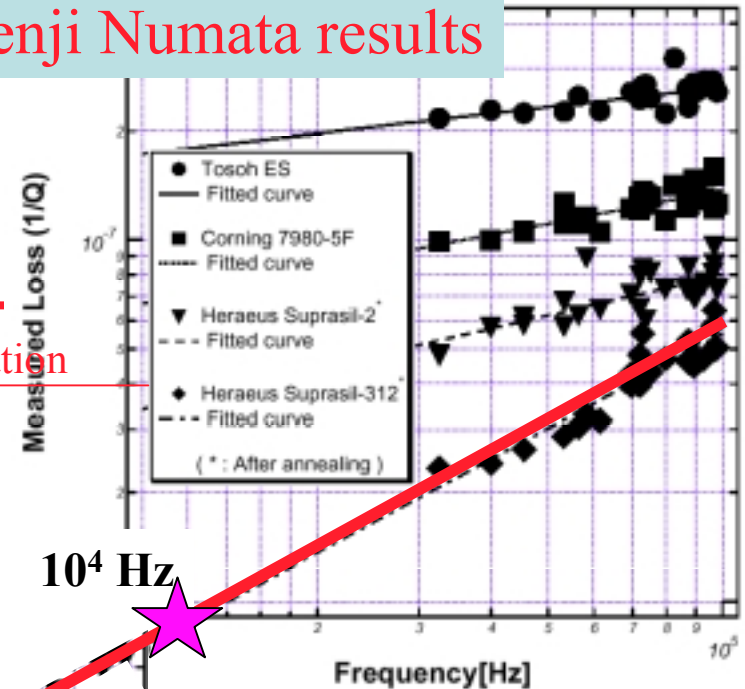
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- Now the bulk F.S. TN floor is crumbling.
- Three new measurements:
- Kenji's Q- factor measurements
- Gregg Harry, Steve Penn observed Fused Silica Q factors at and above 200 Million
  - Note: Sapphire show equally high Q factors but, unfortunately, the fact is irrelevant because of the thermo-elastic effect
- Phil's measurement of old LIGO test mass



Where are the substrate losses at  $f \sim 100$  Hz?

### Kenji Numata results



Original estimation  
 $3 \times 10^{-7}$

Steve Penn and Gregg Harry's result



Extrapolated to test mass shape



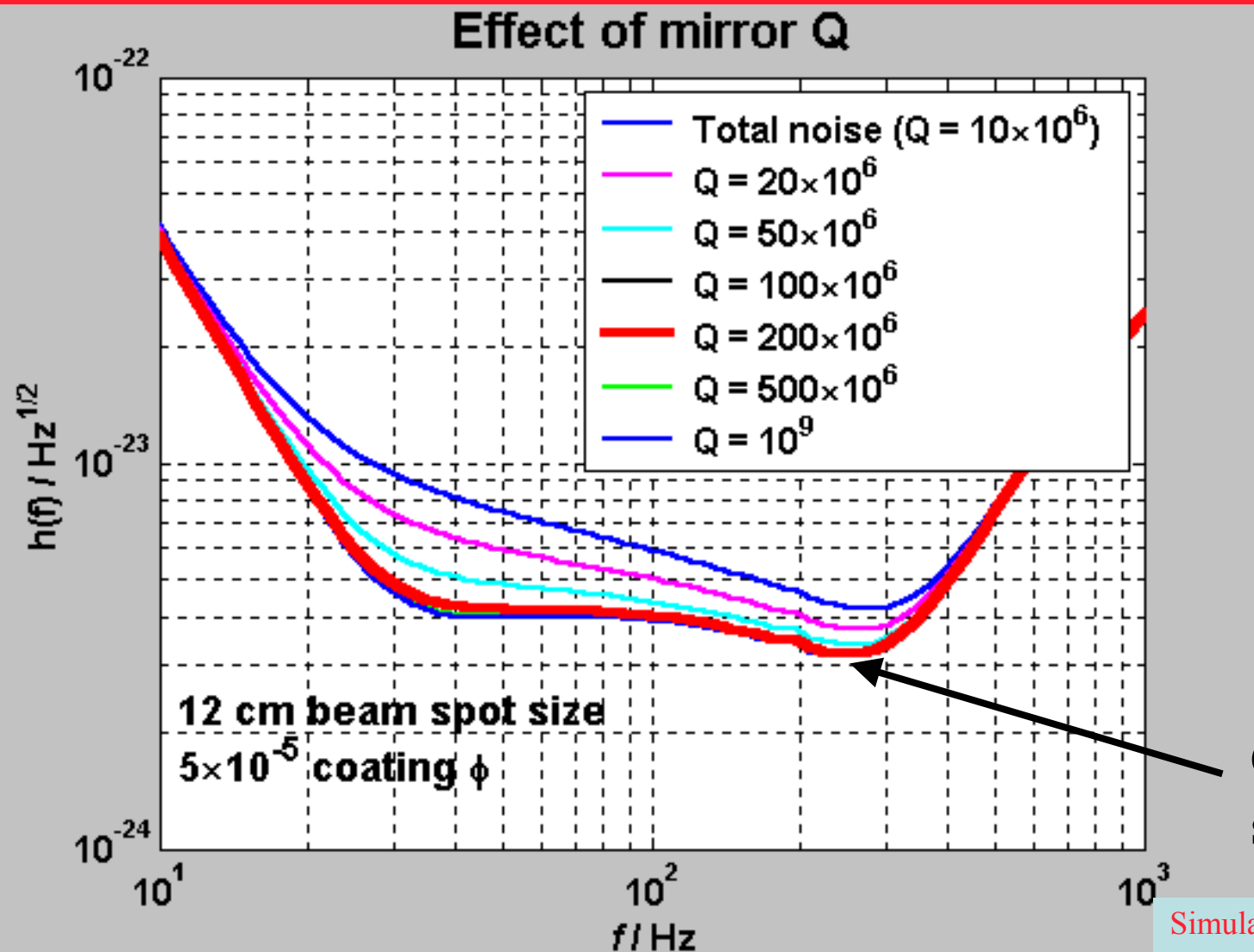
Phil Willems' result on LIGO I mass

At what point Surface and Coating losses spoil the performance?



# What can we expect?

## Effect of substrate's Q factor.



Note:  
large beam size  
used to depress  
coating ill effects

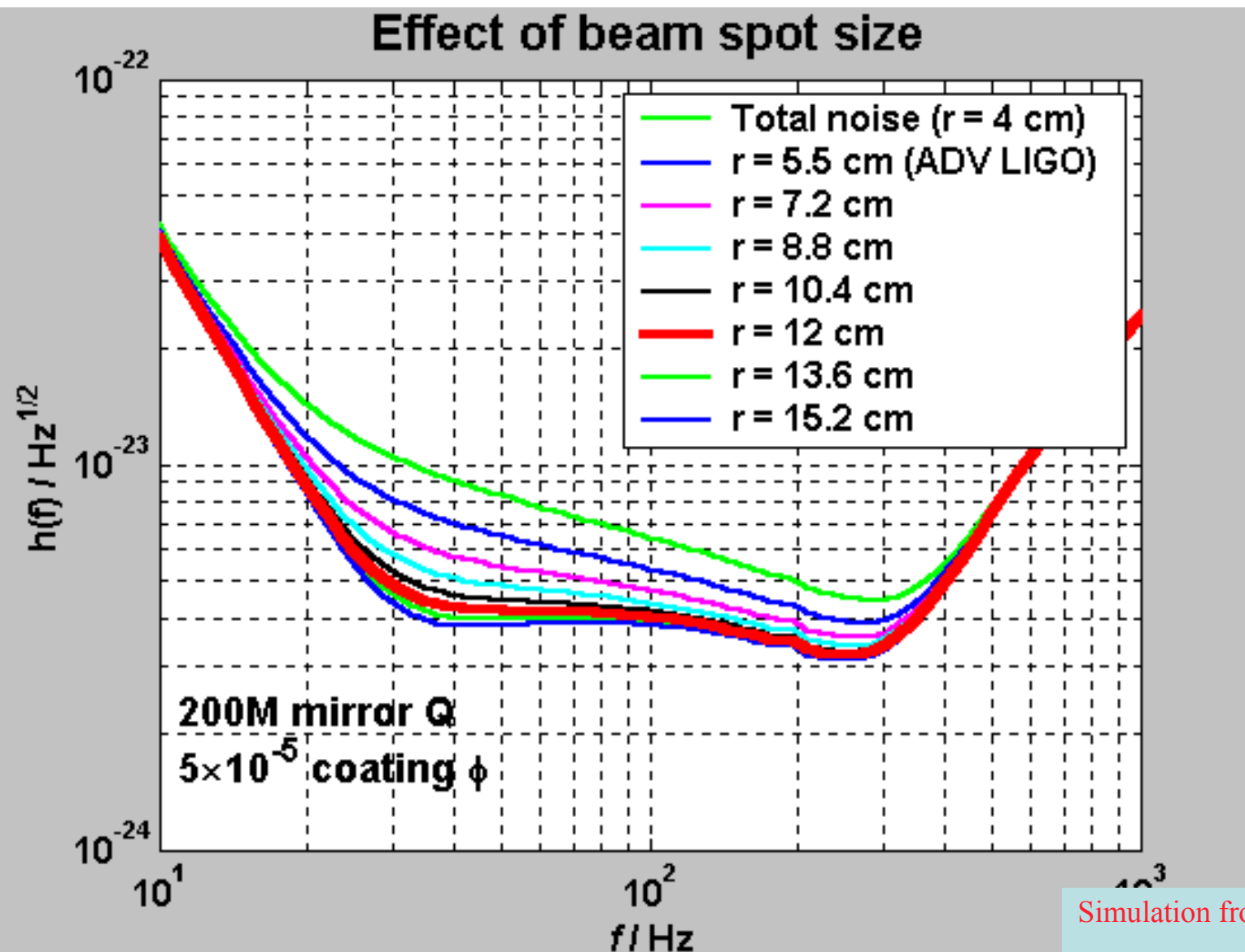
Coating  
saturation

# Implications at L.F.

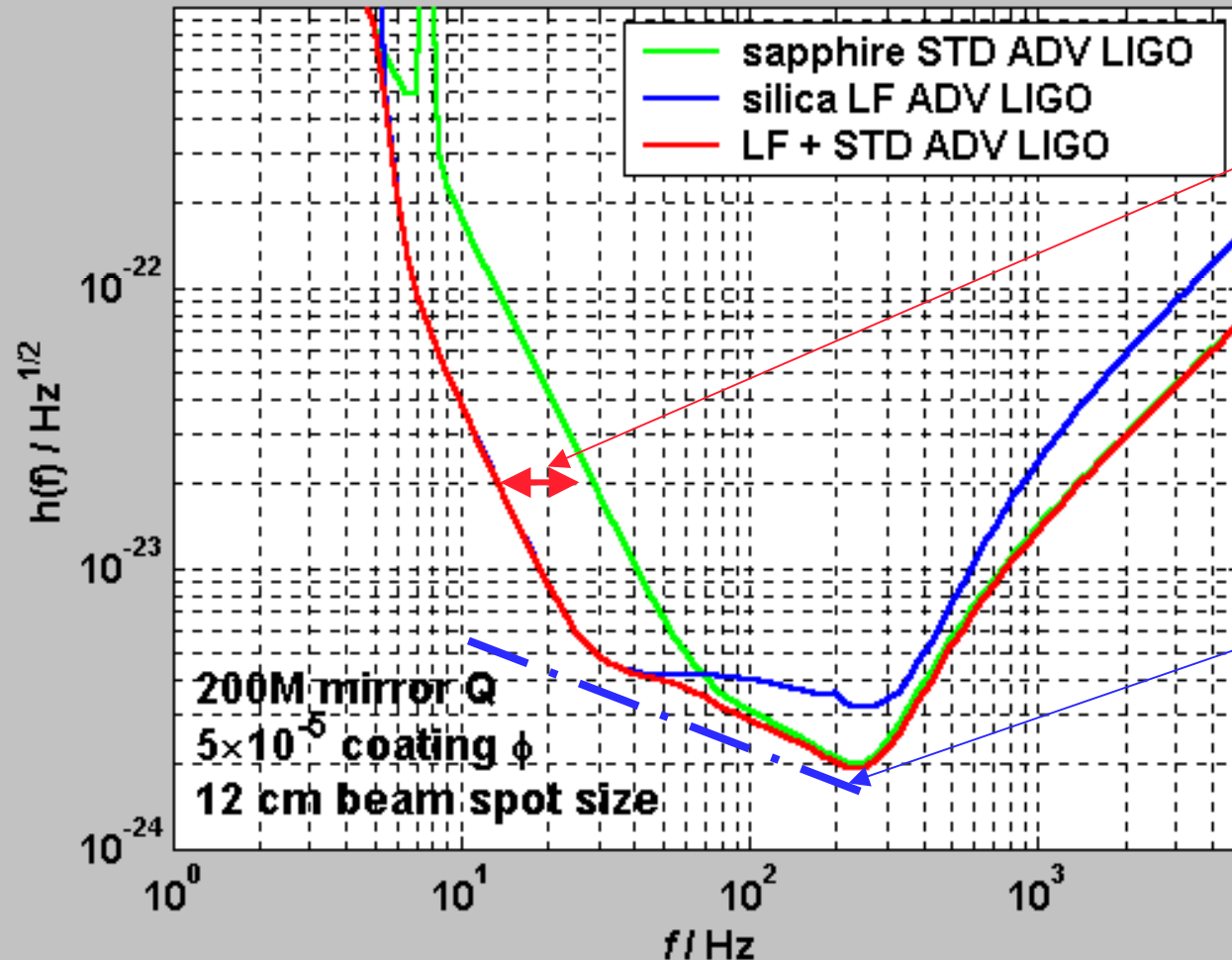
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- **Fused silica is the ideal choice for LF interferometers**
- The thermal noise limit **from coating thermal noise.**
- **Solutions**
- **Advanced coatings**                      **may be in future**
- **Large spot sizes**                      **possible now**
  - **Spot size effects:**
  - Bulk thermal noise  $\sim$  (spot diameter)<sup>-1/2</sup>
  - Coating thermal noise  $\sim$  (spot diameter)<sup>-1</sup>
  - Thermo-elastic noise  $\sim$  (spot diameter)<sup>-3/2</sup>
- **Large spot sizes are required**

# Effect of spot size



# Bench and Kenji's estimations



x 2 gain from longer Suspensions, higher mass, and lower stored beam power

in solid Gregg and Enrico's Simulations on Bench

In blue dashes Kenji's "complete" TN simulation on Ansys ( $10^{-4}$  coating  $\phi$ )

# Signal to noise at 200 MPc

Inspiral mass	AdvLIGO S/N	LF LIGO S/N	Tandem S/N
1.4+1.4	4	4.4	>6
30+30	51.5 ★	57.1 ★	>80
50+50	78.9 ★	87.4 ★	>120

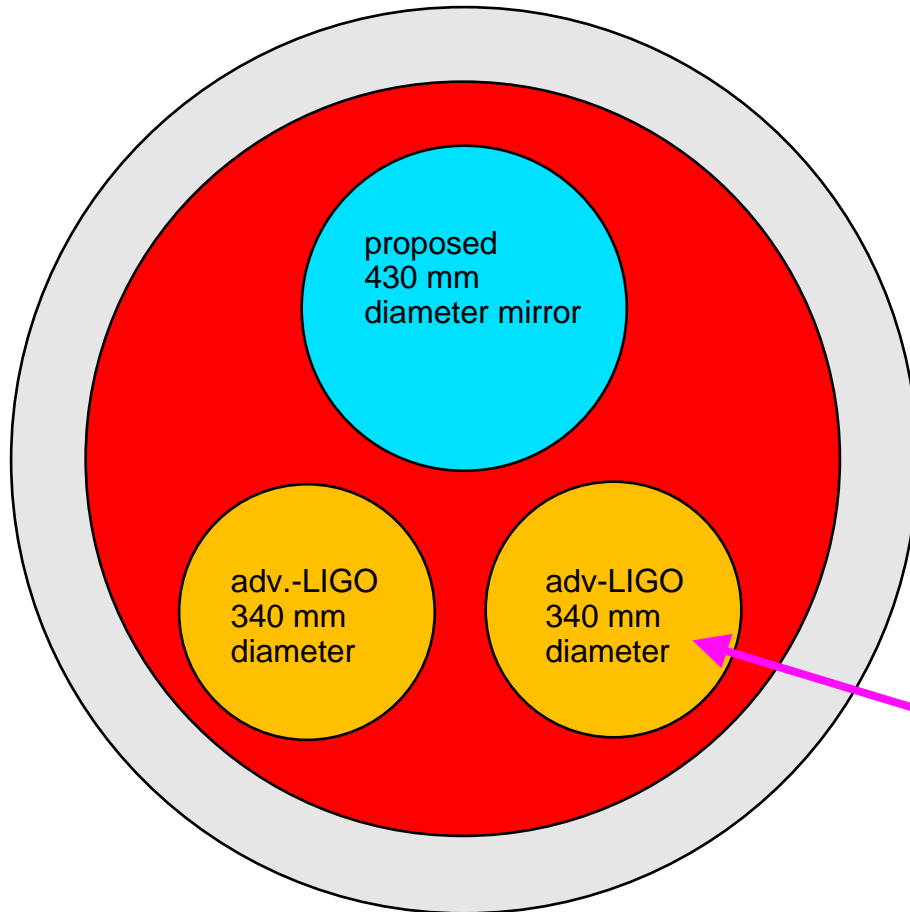
**Tandem configuration allows much larger S/N (between  $\sqrt{2}$  [equal range IFO] and 2 [fully separated f ranges]) !!**

★ Assuming templates applicable throughout the frequency range, see Iyer et al. **after LF trigger and follow up at HF to recover full S/N for high mass objects merging in Adv-LIGO bandwidth**

**At LF twice or more the effective signal to noise =>**

**=> ~1 order of magnitude in observed volume for high mass obj.s**

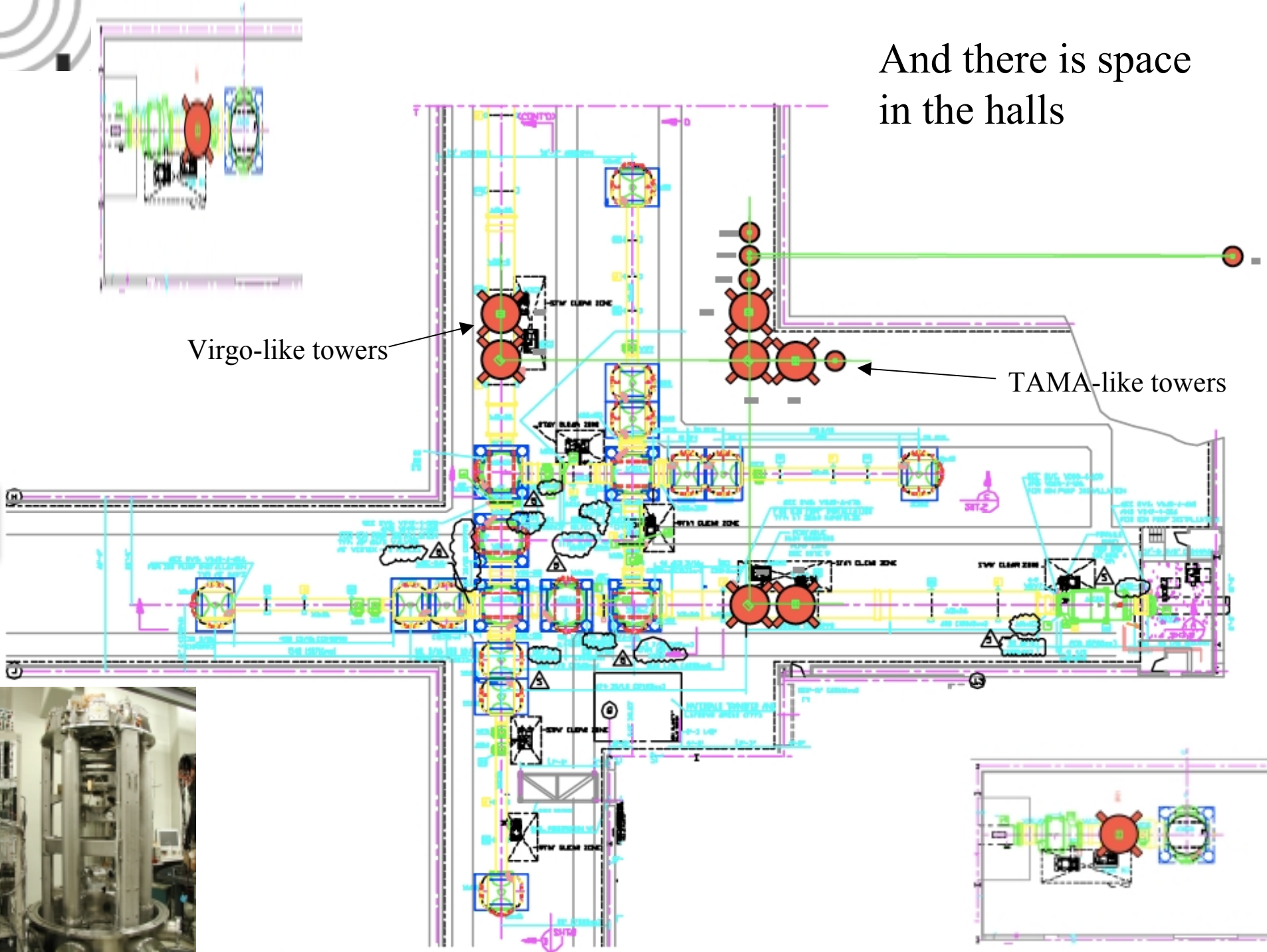
# Can we accommodate a LF interferometer next to Adv-LIGO



- There is space in the beam pipe just above and forwards of the Adv-LIGO mirrors

• Advanced LIGO nominal beam positions

And there is space  
in the halls





# Resuming

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- A Virgo-like interferometer to cover the low frequency region at LIGO would be greatly desirable
- Advantages
- Lower frequency region is better covered (Explored volume  $> *3$ )
- Splitting up the frequency range between two different interferometers eases lots of design constraints and allows better performance from each
- Advanced LIGOs are free to be narrow banded
- For heavy massers, Adv.LIGO would be “triggered” by the LF optimal filter detection and allow disentangling final inspiral and merge signals and recover S/N

# Can we afford **not to** introduce a LF brother for Adv-LIGO

- Clearly the newly observed BH are important and compelling potential GW sources for a LF interferometer
- Optimized LF sensitivity allows
  - study of the genesis of the large galactic BH believed to be central to the dynamics of galaxies and
  - mapping the globular clusters in our neighborhood
  - Enhancement of the performance of both Virgo and LIGO
- At LIGO with roughly a 10% increase of the projected costs the explored volume in the Universe can be increased by at least a factor of 3 for ns-ns inspirals, and much more for heavier mass objects.
- Similarly, but at a higher cost, at Virgo

# The End !

- Frequently Asked Questions (for offline discussions)
  - Comments for LIGO
  - Comments for Virgo
  - Are wide beams feasible?
  - Is gravity gradient a problem
  - Do we need a new design?
  - When and where to implement LF-GWIDs?
  - Can we afford LF-GWID?
  - LF-GWID Characteristics
  - How big a mirror can we make?
  - Is Virgo an optimized LF-GWID?
  - Is there space in Virgo for a HF companion?
  - What would be the interest for Virgo in LF companions?
    - Are LF interferometers in the LIGO facilities adequate LF companions for Virgo
    - Should EGO push to build Low Frequency companion(s) for LF coincidence detection in the LIGO facilities?
  - Effect of spot size and better catings
  - More on event rates

# Comments for LIGO

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- Adv-LIGO is designed for broadband over a different set of possible sources and consequently does not cover well the Low Frequency range as well as an IFO exclusively targeted at this range
- Ignoring the LF range could be dangerous because it contains many juicy, and observed, GW signal generator candidates
- Redesigning Adv-LIGO to cover it would be awkward and take too long and it would uncover the equally important High Frequency range
- Adding a simple Low Frequency interferometer is the simplest and best choice!

# Comments for Virgo

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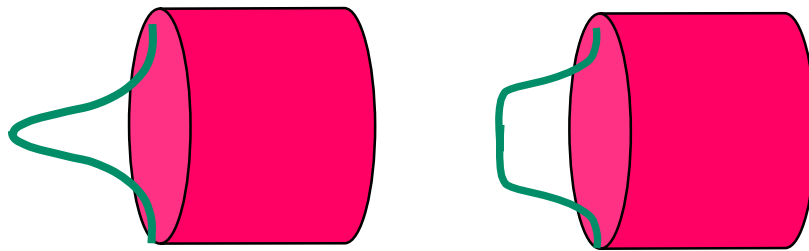
- Virgo needs matching LF coincidence partner(s) to optimize its science goals
- Adv-LIGO is unlikely to be optimized for the low frequency range and would profit greatly both in reach and scientific scope from LF companions
- Building the LF GWIDs in the LIGO vacuum pipes is cost effective
- The relative orientations makes that two Virgo-likes in the LIGO pipes allow **both** coincidence detection **and** coverage of both emission polarizations.

# How to reduce the coating noise problem

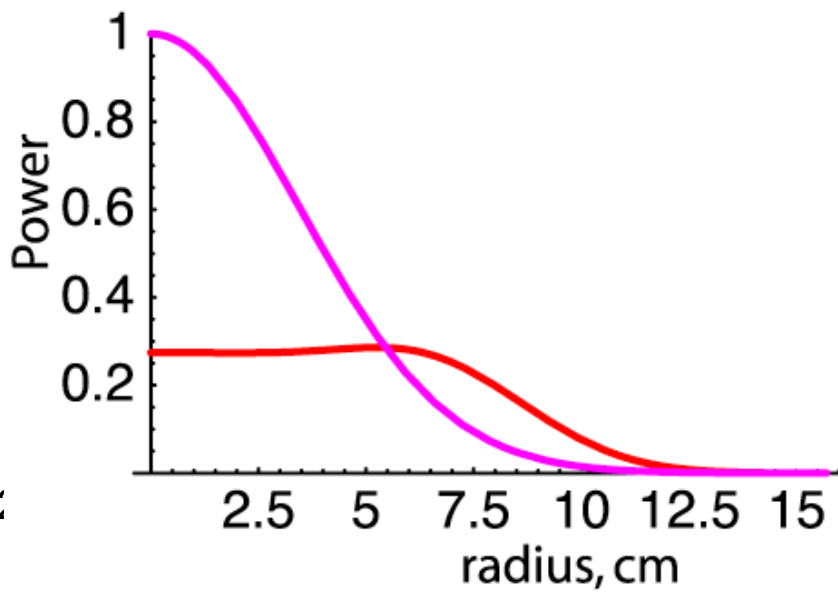
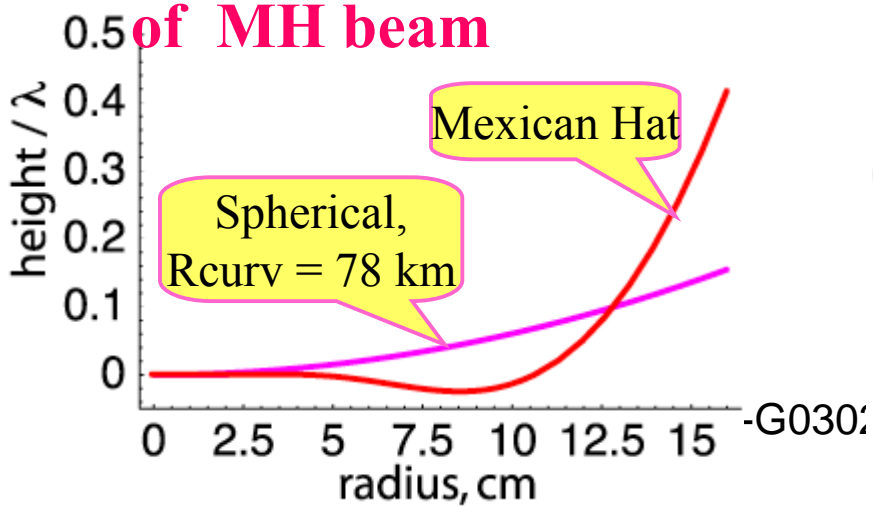
Mexican hats proposed by Kip Thorne et al. are a solution

<http://www.ligo.caltech.edu/docs/G/G030137-00/>

- A Flat-topped beam averages over bumps much more effectively than a Gaussian beam.



- MH mirror shape:**  
**matches phase fronts**  
**of MH beam**

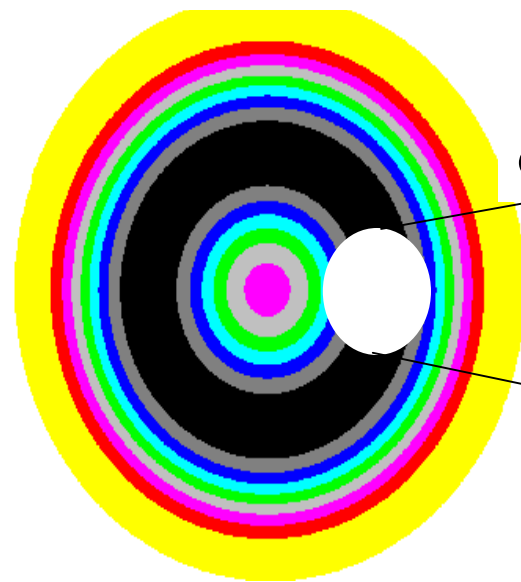


## Mexican hats are feasible

And J.M. Mackowsky shows that they are relatively easy to make

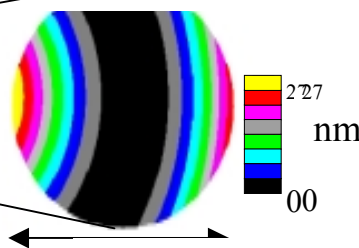
<http://www.ligo.caltech.edu/docs/G/G030115-00/>

Top view of a Mexican hat



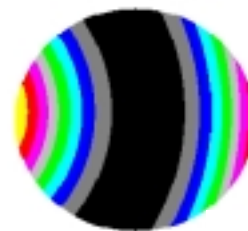
Frontier 350 mm  
28th of May

Studied area of Mexican hat

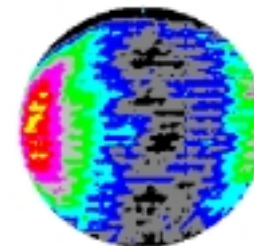


80 mm

LIGO-G0302

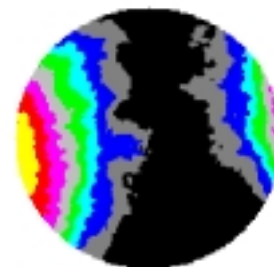
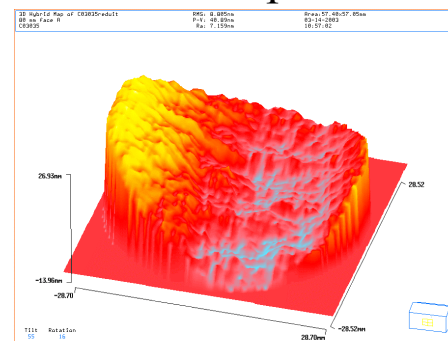


Theoretical mexican hat



Simulation of the corrective coating

Experimental mexican hat



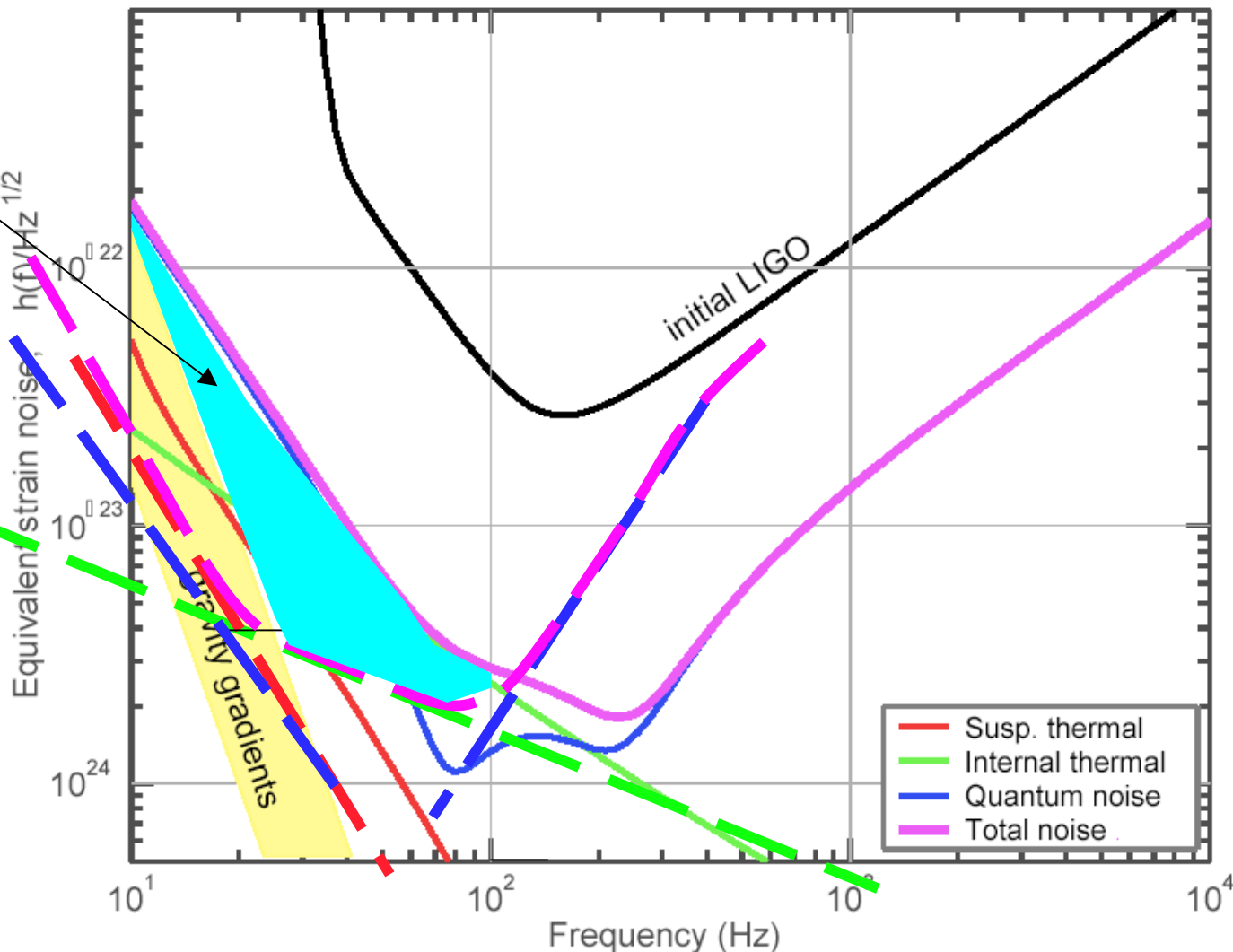


# Is gravity gradient going to stop us?

Minimal  
Additional  
Phase space

Dashed =  
LF-LIGO

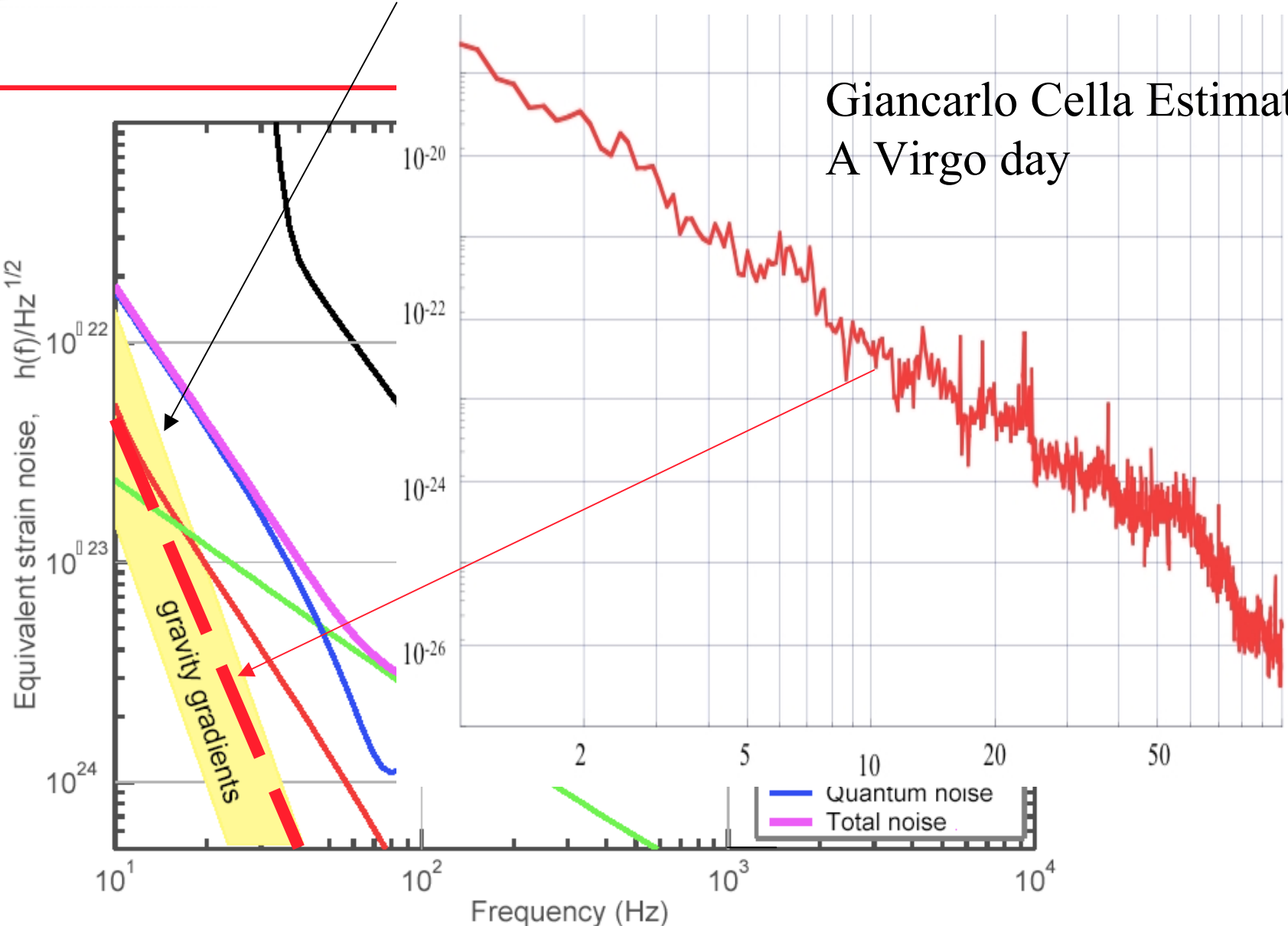
Solid =  
Adv-LIGO







Adv-LIGO estimation based on worse of best 90%  
Of data stretches, including transients!



Giancarlo Cella Estimation  
A Virgo day

# Comments on GG

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- G.C. Cella evaluations give similar results
- Even if the GG was to be low only in windless nights, it would be worth having the listening capability 50% of the time
- LF-LIGO would give us the opportunity to test GG subtraction techniques

## Does gravity gradient negate the advantages?

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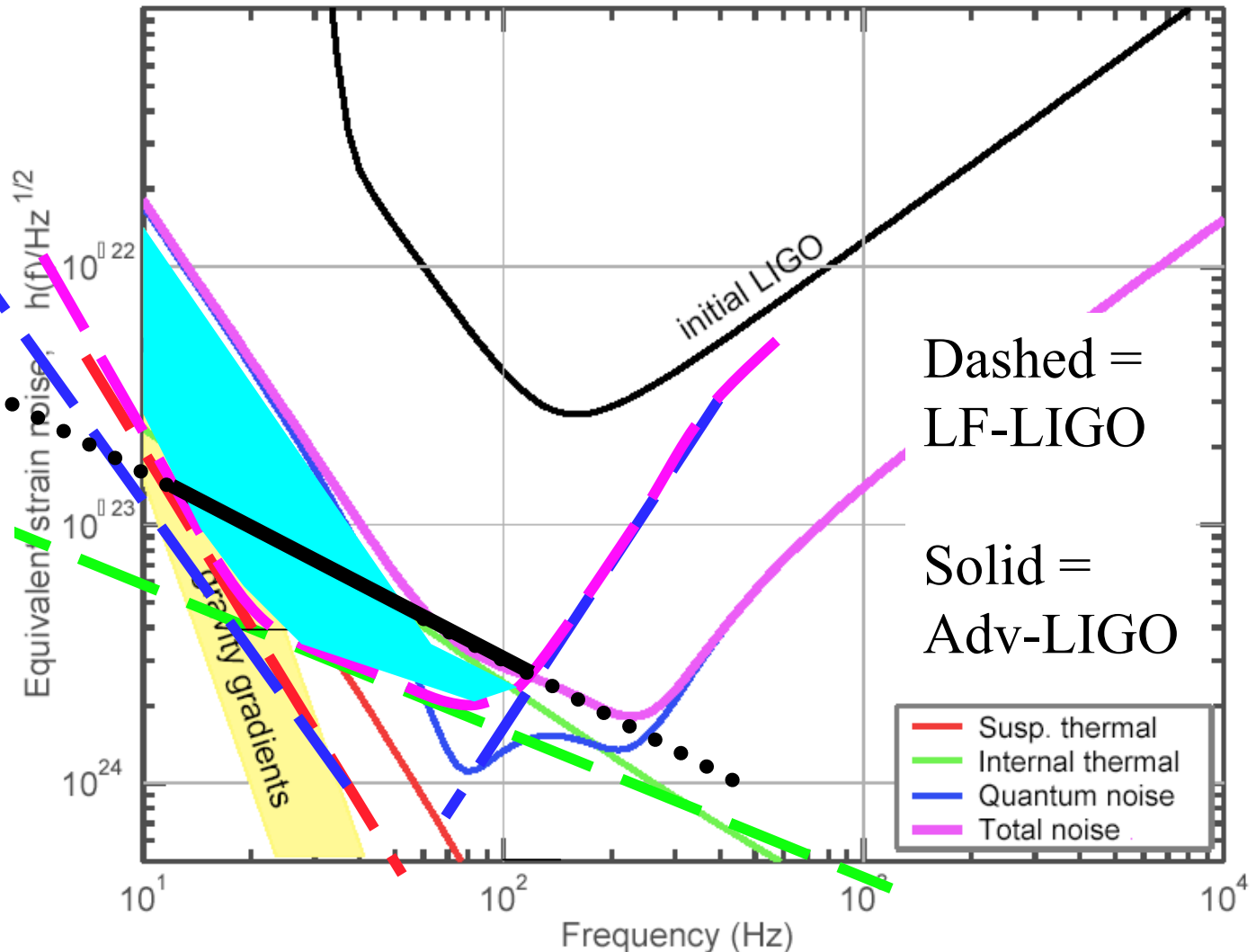
- With longer mirror suspensions (1-1.5m) the suspension thermal noise is pushed at lower frequency
- Gravity gradient limitations get uncovered
- Can start testing GG subtraction techniques
  - Note: Clearly for the future will need to go underground to fight GG
- Even aboveground there is so much clear frequency range to allow substantial detection improvements



# Is gravity gradient going to stop us?

50+50  $M_{\text{sun}}$   
inspiral at  $z=2$

Conclusions  
We can possibly recover most of the yellow band



# Do we need a new design?

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- **Virgo optical and control design is nearly optimal,**
  - The **Virgo interferometer** is (or soon will be) fully validated.
  - Will only need minor improvements and some simplifications
- **Laser can be the same as LIGO (lower power)**
- **Seismic Attenuation and Suspensions**
  - large optics: already developed for advanced LIGO (downselected at the time)
  - Small optics: use TAMA-SAS design
  - Both well tested

All components off the shelf and tested.

**Technically we can build it almost immediately**

# When and where to implement LF GWID?

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- Cannot disrupt Adv-LIGO operations
- Above the Adv.-LIGO beamline => must be installed forward of Adv-LIGO
- At least all the main mirror vacuum tanks must, but probably all of the interferometer should, be installed at the same time as Adv-LIGO

# Can we afford LF GWIDs

- LSC and Advanced LIGO have decided not to pursue the L.F. option to focus on different possible sources, and dedicated all available sources to it
- A L.F. interferometer can be done only with external support
- A LF brother for Adv-LIGO would be a **simpler and cheaper interferometer**.
- **Seismic and suspension** design is available using the **inexpensive, existing, and well validated**, SAS and Virgo concept
- There is space in the existing facilities,
  - except small buildings for mode cleaner end towers if needed.

# Can we afford a LF GWID

- Estimation of project costs:

Color code: Prices per unit **Price per interferometer** Cost source

- Large Vacuum tanks (2 m diameter ~Virgo design) 0.4 Meu Actual Cost
- Large SAS tower (including control electronics) .25 Meu A.C./Bids
- Mirrors 0.3 Meu Bids
- 7 or 8 systems(vacuum+SAS+mirror) per interferometer **7.6 Meu**
- Small vacuum tank and TAMA-SAS suspensions 0.2 Meu A. C. + Bids
- 6 to 8 needed per interferometer **1.6 Meu**
- Small optics **0.2 Meu** Est.
- Laser **0.5 Meu** rec. LIGO
- Gate valves 0.1 Meu A.C.
- 6 needed **0.6 Meu**
- New building for mode cleaner, and 150 m vac pipe: **0.5 MUS\$** Est. F. Asiri
- Design **0.5 Meu** Est./A.C.
- Various **3.0 Meu** Est.
- Total per interferometer **14.5 Meu**
- Spares (1 set optics) **4.0 Meu**





# Can we afford a LF-GWID

- We are talking of 15 M US\$
- per interferometer **for components**  
+ for spares 5 MUS\$
- **Manpower** estimated staff of
- 20 persons for 5 years for 1 interferometer,
- 30 persons for 2 interferometers
- at 100,000 US\$ per person/year, for 1 interferometer 10 MUS\$  
for 2 interferometers 15 MUS\$
- Estimated Grand Total
- **for one interferometer** 30 MUS\$
- **for two interferometers** 50 MUS\$

# L F G W I D Characteristics

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- Shortened SAS to fit under roof
- Longer mirror suspensions
  - Suspension T.N. freq. cut  $\sim 1/\sqrt{L}$
- **Everything hanging down**

Auxiliar suspended tables above beam line for pickoff, etc.

- **Stay out of the way of Adv. LIGO**



## How big a mirror can we get?

- larger mirrors are feasible today
  - 75 Kg fused silica
  - 430 mm diameter
  - (Heraeus bid)

# Is Virgo an optimized LF GWID?

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- Mostly yes, but needs its scheduled upgrades
  - Monolithic Fused Silica suspensions for suspension thermal noise
  - New mirrors, (including to replace the low-Q Herasyl mirrors at the end stations) possibly heavier ones.
- Mexican hat mirrors would be necessary to reduce the coating thermal noise problem
  - And a new injection telescope to match the wider beam




# Is there space in Virgo for a HF companion?

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- A new L building should be built in front of the central building to house the companion, as well as new or enlarged end stations.
- The Virgo beam is in the center of the beam pipe; during the Virgo upgrade the fused silica suspensions should be made longer to lower the beam line and make space for an HF companion.
- Given the location of the present gate valves, venting of the 3 Km pipes would be necessary to install the companion vacuum tanks.

# What would be the interest of Virgo in a Low Frequency companion?

- Virgo is already focusing on low frequencies where the new observed possible sources may emit.
- Why should it need a companion?
- Present LIGO has essentially no LF capabilities
- Adv-LIGO will have broad-band capabilities but it will run optimized for high frequency narrow-banding,
- 
- The LF range may not be sufficiently covered by LIGO to provide optimized coincidence



# Should EGO push to build Low Frequency companion(s) for LF coincidence detection in the LIGO facilities?

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- Economically it makes lots of sense,
- Two independent interferometers can be built without having to build new facilities
- No new concepts or difficult developments are needed
  - The Virgo concept is perfectly adequate

## Are LF interferometers in the LIGO facilities adequate LF companions for Virgo

- The LIGO facilities are not well aligned with Virgo,
- But two of them are available
- Coincidence running and coverage of both source polarizations are possible if two LF-GWID are implemented!!!
- Three point observation gives the best pointing capabilities.
  
- This development could be made while developing new generation IF in new facilities

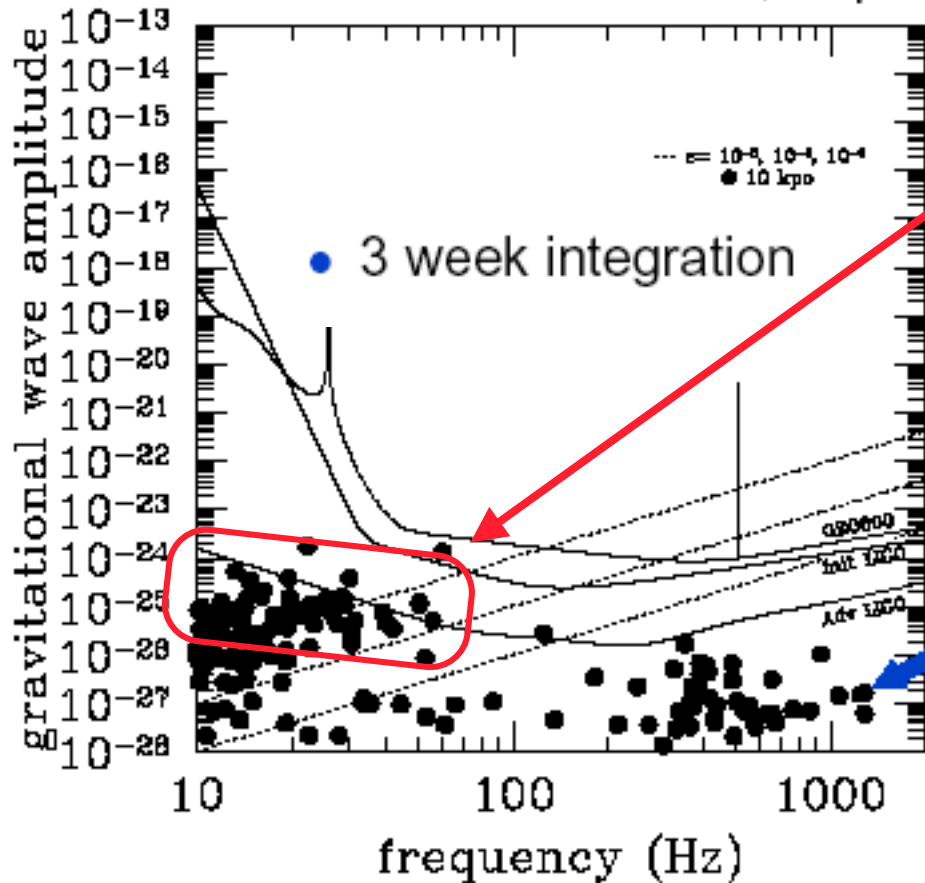


# Interesting question.

Matthew Benacquista

- How did the inferred 1000 s.m. BH get in cores of globular clusters?
- Star merger in cluster core + direct collapse?
- Or
- Sequential accretion of  $\sim 10$  s.m. BH?
  
- Presence or absence of GW signal give the answer
-

# Older motivations?



- A LF-GWID would allow exploration of a much richer ns population than an HF-GWID

- Teviet Creighton  
<http://cajagwr.caltech.edu/scripts/seminars.html>

# Other motivations?

## Cosmic background

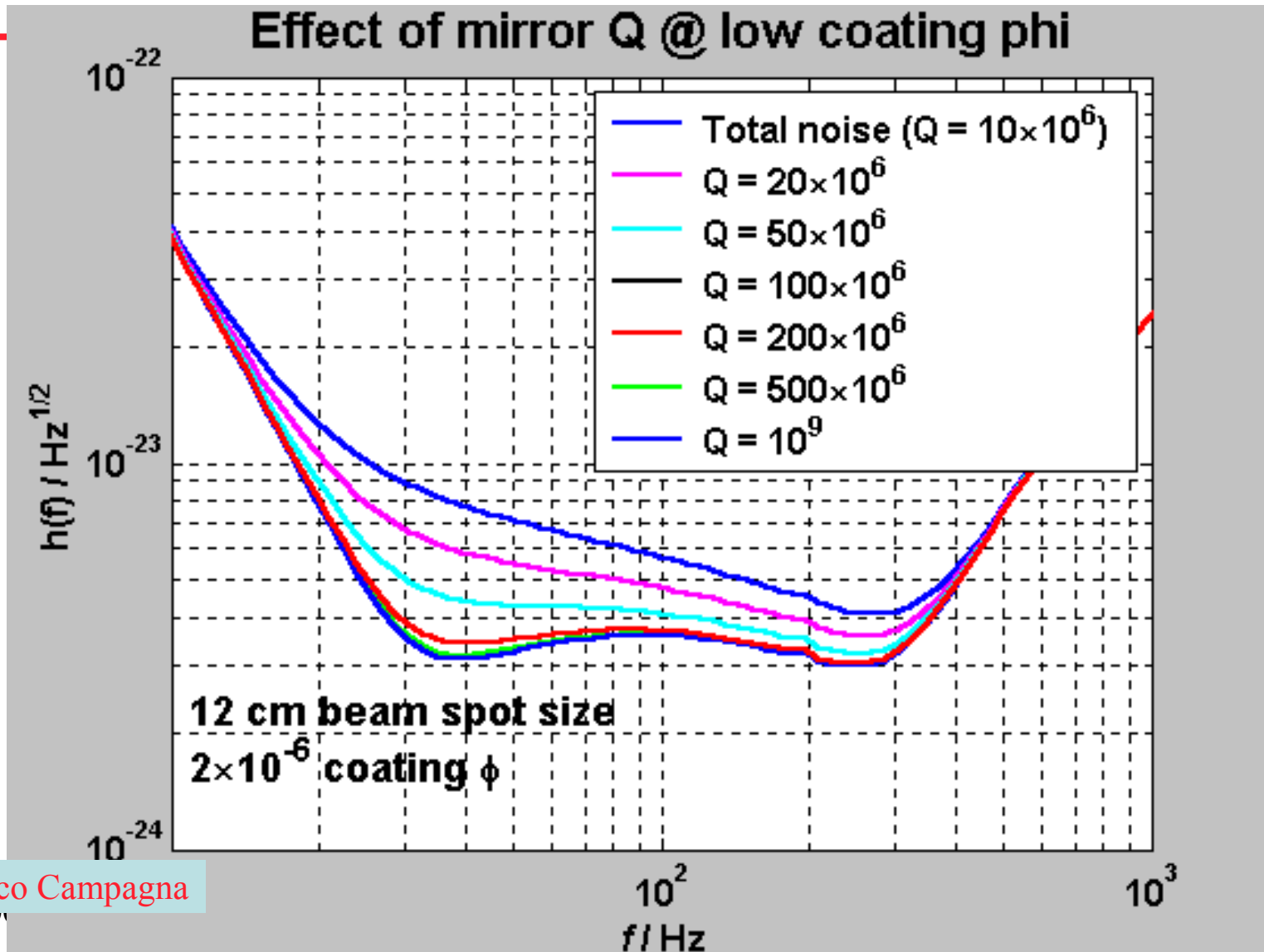
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- The sensitivity to GW cosmic background (if the background is flat in frequency) would increase at LF with  $f^{3/2}$  and
- The GW background signal coherence of LF interferometers would be almost perfect

- Albert Lazzarini <http://www.ligo.caltech.edu/docs/G/G030242-01/>



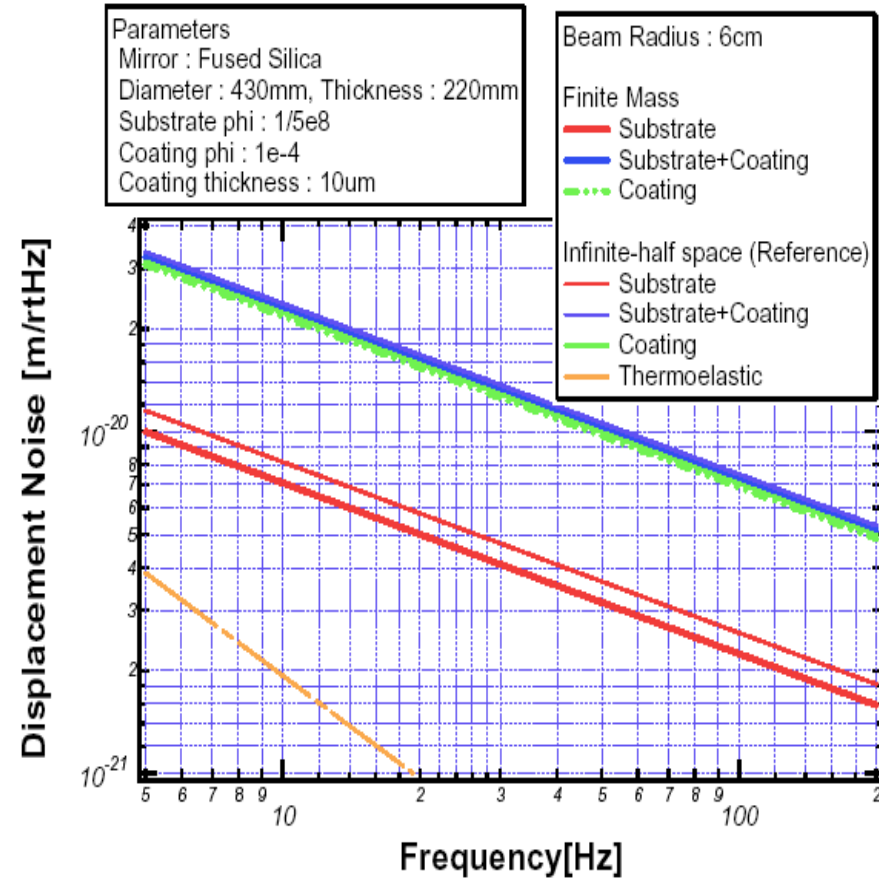
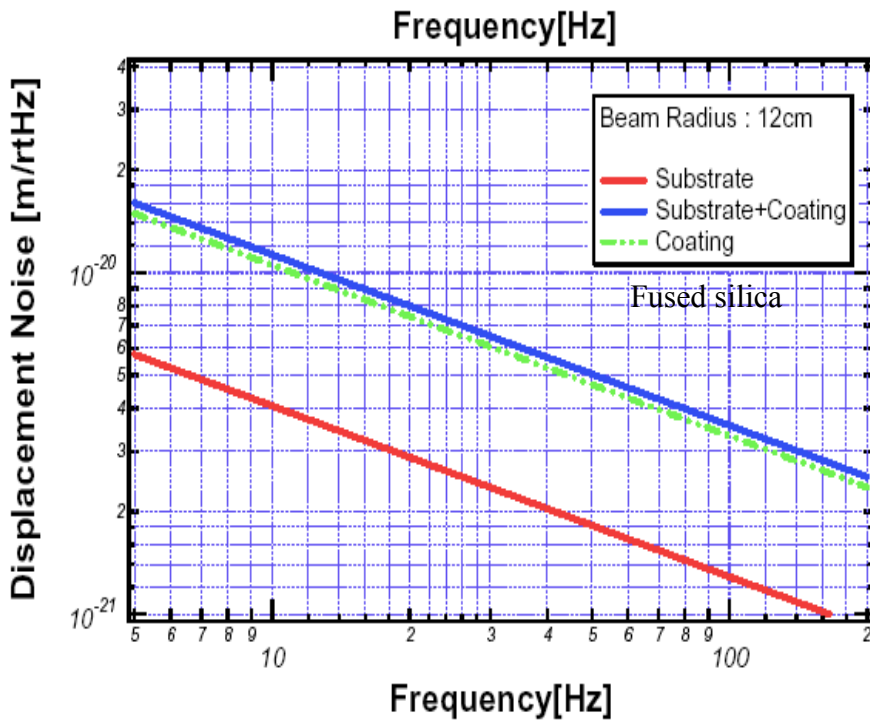
What happens if one could have a better coating Q-factor!





# Effect of spot size

ANSYS “complete” Simulation  
from Kenji Numata

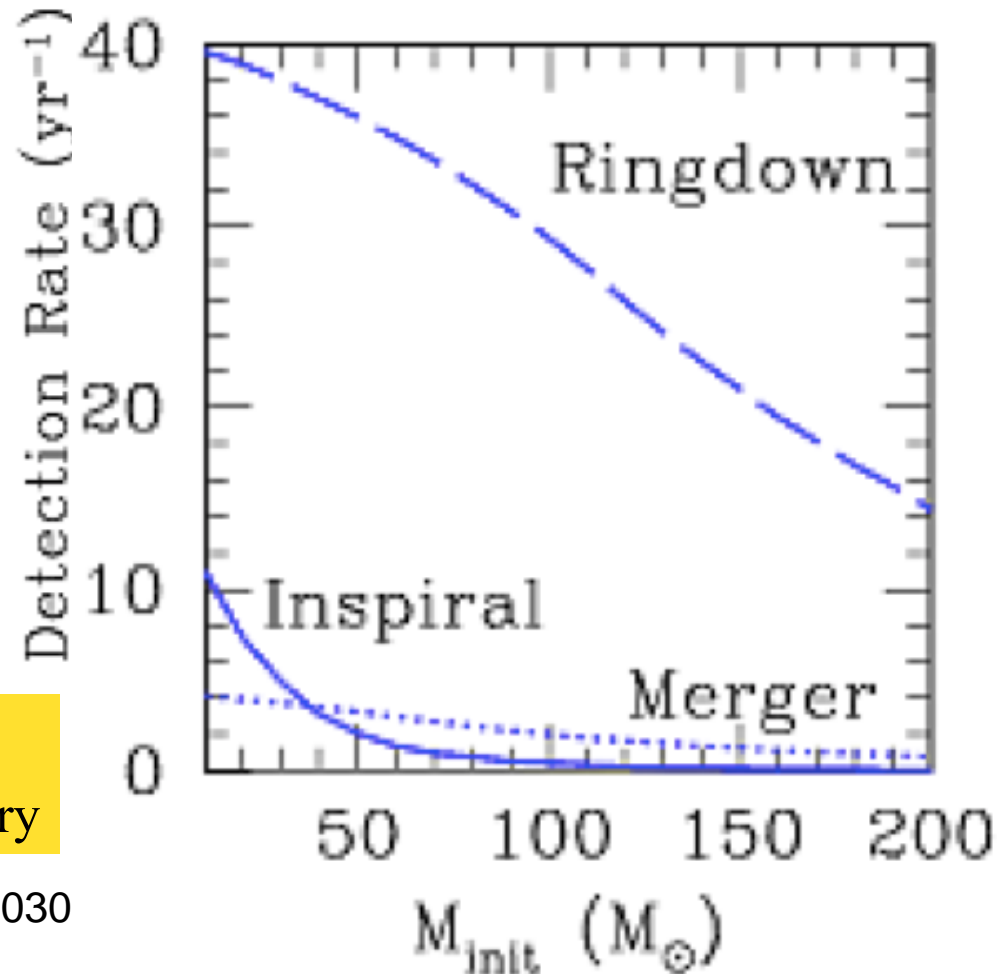


For spot size effects on sapphire, see Erika D’ambrosio, ref.

28th of May 2003

# Predicted inspiral rate

- If central BH initial mass is higher, the Adv-LIGO detection rate is strongly depressed by LF and template limitations.
- a LF-GWID inspiral would recover the high detection rate by a large factor



•Cole Miller  
•Very preliminary

# Predicted inspiral rate

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- $\Delta M$  assumed to be  $\Delta M = 10 M_{\text{sun}}$
- If accretion was with bigger increments (say  $\Delta M = 30 M_{\text{sun}}$ )
  - (Heavier masses are slowed down first)
- Number of accretion events  $\sim 1/\Delta M$
- But signal amplitude and detectable range  $\sim \Delta M$
- Number of detectable events  $\sim \Delta M^2$
- If lower frequency sensitivity is available

# Signal to noise at 200 MPc

Inspiral mass	Adv LIGO S/N	LF LIGO S/N
1.4+1.4	4	4.4
30+30	51.5★	57.1★
50+50	78.9★	87.4★

Q silica 50M (conservative)  
Coating Phi 2  $10^{-5}$

A-LIGO seis. Wall @ 10 Hz  
Standard configuration

LF-L susp. Noise limited

Bench/Gregg Harry

- ★ Assuming templates applicable throughout the frequency range, see Iyer et al.



## What is relevant for LF-GW observations

- Tens of BH-BH detectable inspiral events per year are expected Coleman Miller. Astrophysics Journal 581: 438-450, Dec 2002
- GW Signals from massive BH will carry farther than NS
  - Signal amplitude roughly proportional to mass
  - Can reach much farther  $M^3$  (if not limited in freq.)
- BUT
- Most signals start above  $20+20 M_{\text{sun}}$ .
  - Close to ISCO difficult to make templates

# Other motivations?

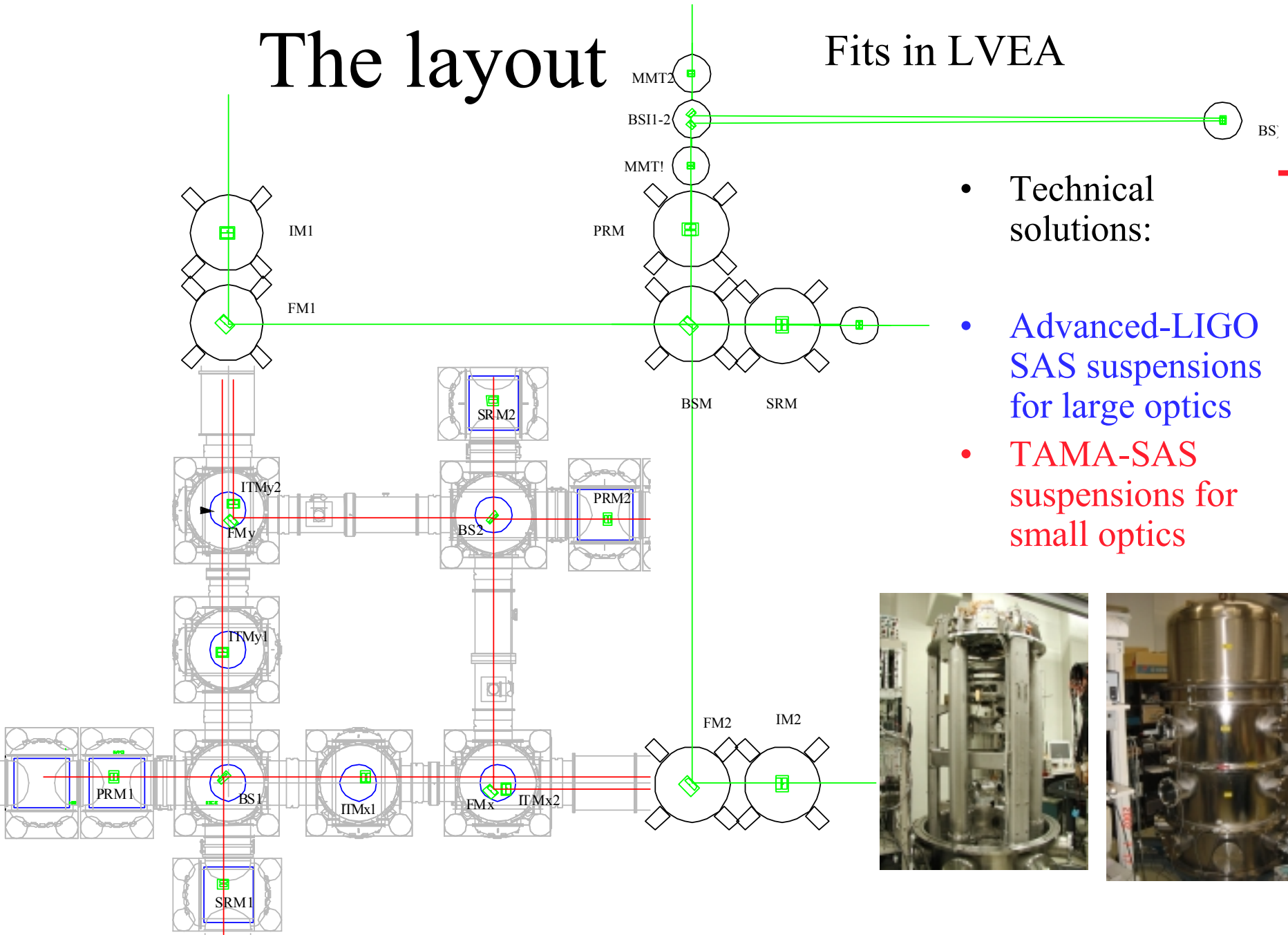
## BH chirp and ringdown

- **final chirp frequency** can be approximated by:
- $f \sim 4.4 / (M/M_{\text{sun}})$  kHz
  - 100  $M_{\text{sun}}$  **systems at 44 Hz,**
  - 1000  $M_{\text{sun}}$  **systems at 4.4 Hz**
- Kerr BH ringdown frequency after merger for mass M:  
 $f \sim (32/M)$  kHz
  - » (J. Creighton, gr-qc/9712044 or F. Echeverria, PRD 40, 3194 (1989))
- **ringdown for a 1000  $M_{\text{sun}}$  BH at  $\sim 32$  Hz.**

Matthew Benacquista

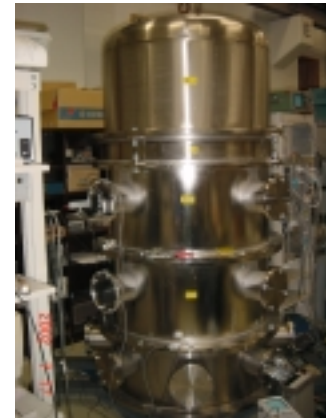
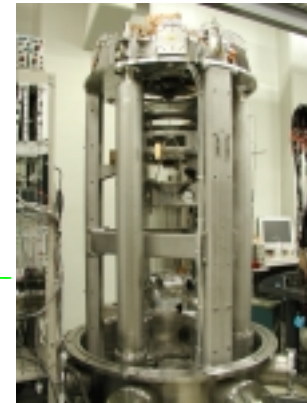
# The layout

## Fits in LVEA



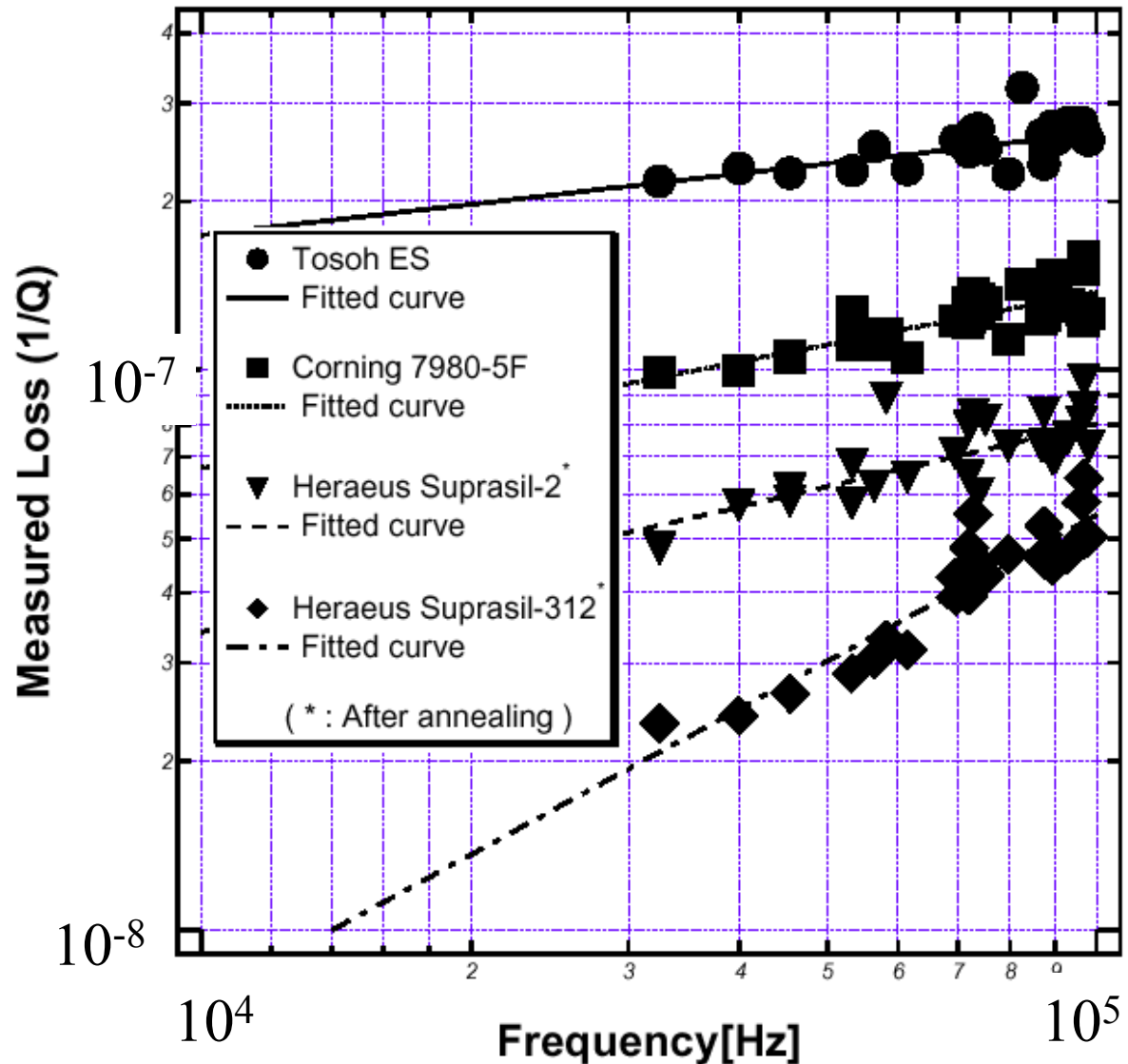
- Technical solutions:

- Advanced-LIGO SAS suspensions for large optics
- TAMA-SAS suspensions for small optics



The Q-factor improves at lower frequency

How much better does it get at 100 Hz?



# Implications at L.F.

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- Fused silica allows for much lower thermal noise floor at L. F. (if coating problem is solved)
- Fused Silica only tolerates “lower” beam power
- At lower frequencies much lower power is required ( $\sim 1/f^2$ )
- larger beam sizes  $\Rightarrow$  less beam power problem
- **Fused silica is the ideal choice for LF interferometers**