

# Proposed Control Room Figures of Merit for Pulsar Sensitivity

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# DMT Infrastructure to Exploit

- Real-time access to online data
- Graphical display:
  - Time histories (strip charts)
  - Spectral plots
- Web page summaries and plots
- Trend file output of selected FOM values
- Monitoring of the monitor

**Proposed FOM's based on ideas  
suggested by pulsar group members**

# Pulsar Figure of Merit 1

## Strain sensitivity – Fixed time intervals

- Rescaled power spectral density for observation time T:

$$\langle h_0 \rangle = 11.4 \sqrt{S_n(f_s)/T}$$

- Display  $\langle h_0(f_s) \rangle$  over  $f_s = 10\text{-}2000$  Hz for time intervals:
  - 1 day
  - Length of data run (e.g., 70 days for S3) ← Primary FOM1
  - 1 year
- Result: pulsar-relevant PSD (no change in shape)

# Pulsar Figure of Merit 1 (cont.)

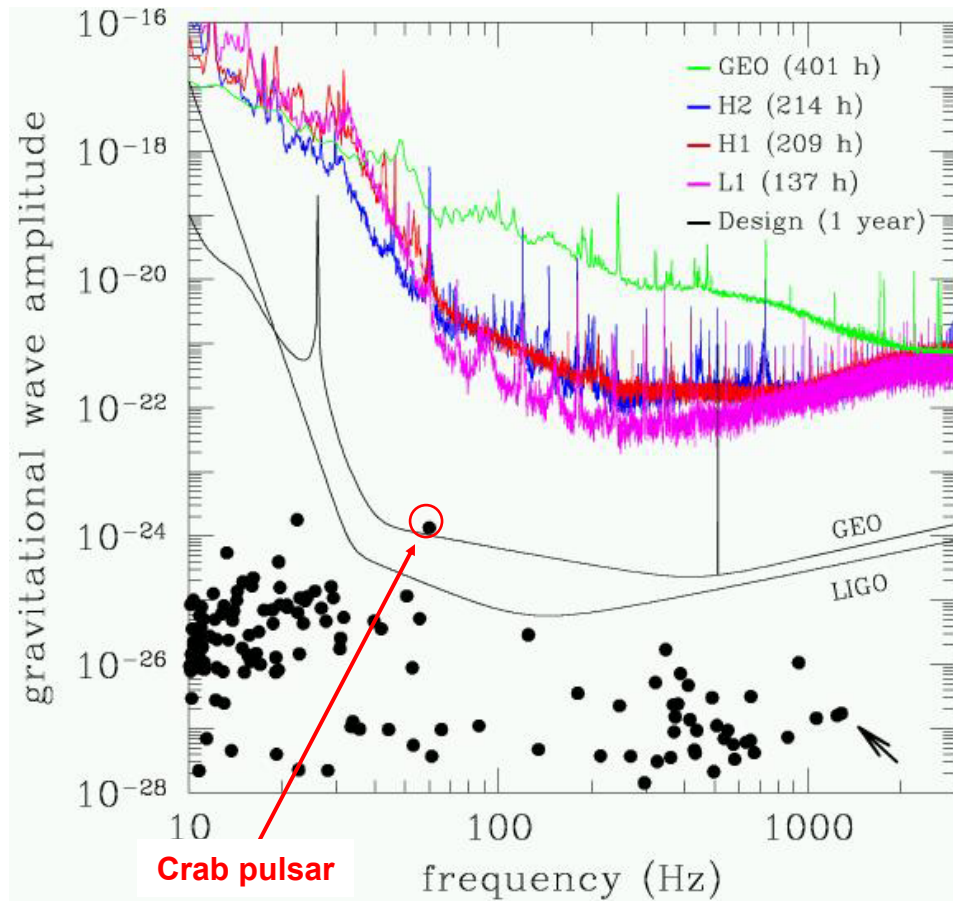
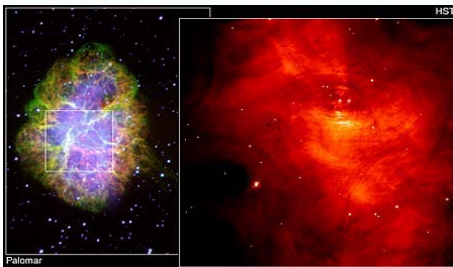


Figure 1 from  
S1 pulsar paper

Colored curves for  
actual S1  $T_{\text{obs}}$  values

Black curves for 1 year  
at design

Dots are energy  
conservation limits on  
known pulsars



## Pulsar Figure of Merit 2

### Time needed to meet energy conservation limit for known pulsars

- For pulsar with  $f_s = 2f_{\text{rot}}$ , spin-down  $\dot{P}$ , moment of inertia  $I$ , and at distance  $r$ , **energy conservation** requires:

(assuming all energy loss due to gravitational waves!)

$$h_{EC} = \frac{5.7 \times 10^{-21}}{[r/(1\text{kpc})]} \sqrt{\left(\frac{f_s}{1\text{kHz}}\right) \left(\frac{\dot{P}}{10^{-13}\text{s/s}}\right) \left(\frac{I}{10^{45}\text{g}\cdot\text{cm}^2}\right)}$$

- Observation time required to attain sensitivity to  $h_{EC}$ :

$$T = \frac{(11.4)^2 S_n(f_s)}{h_{EC}^2}$$

## Pulsar Figure of Merit 2 (cont.)

For reference, at LIGO I design at  $\sim 60$  Hz [ $\sim 10^{-22}$  / sqrt(Hz)], testing energy conservation for the Crab requires  $T_{\text{EC}} \sim 9$  days

Display an instantaneous frequencies series with  $T_{\text{EC}}$  vs  $f_s$  for discrete, known pulsars.

Provide summary web table of instantaneous  $T_{\text{EC}}$  values and recent averages

For selected pulsars, display time history of  $T_{\text{EC}}$  and write trend

Example: 12-hour strip chart of Crab  $T_{\text{EC}}$  (weeks) ← Primary FOM2

Astrophysically interesting

Experimentally challenging in the extreme:  $f_s \sim 59.93$  Hz

## Pulsar Figure of Merit 3

### Ellipticity sensitivity – known and unknown pulsars

- For known pulsars, FOM1 converts to a pulsar ellipticity sensitivity:

$$\langle \epsilon \rangle = (9.5 \times 10^{-6}) \left[ \frac{r}{\text{kpc}} \right] \left[ \frac{f_s}{\text{kHz}} \right]^{-2} \left[ \frac{I}{10^{45} \text{g} \cdot \text{cm}^2} \right]^{-1} \left[ \frac{\langle h_0 \rangle}{10^{-23}} \right]$$

- Display graph and html table of  $\langle \epsilon \rangle$  for known pulsars for same time intervals as in FOM1 (e.g., 1 day, run duration, 1 year)
- Display generic curves of  $\langle \epsilon \rangle$  vs  $f_s$  for same time intervals assuming pulsar at fixed distance of 1 kpc (adds  $1/f_s^2$  weight to PSD)

**Primary FOM3:** Graph of  $\langle \epsilon \rangle$  for known pulsars for run duration

# Pulsar Figure of Merit 4

## Cumulative actual sensitivity

- At start of data run, monitor starts accumulating ideal sensitivities, using

$$\langle h_0(f_s) \rangle = 11.4 [\langle S_h \rangle_{\text{cumulative}}]^{1/2}$$

Where  $\langle S_h(f_s) \rangle_{\text{cumulative}}$  is the cumulative weighted average of  $\langle S_h \rangle$

- Display graph (smooth curve vs  $f_s$ )
- Display html table for known pulsars of cumulative values and energy-conservation limits



## Pulsar Figure of Merit 4 (cont.)

### Remarks:

- Useful for performance evaluation
- But not useful for real-time feedback
- Patrick warns me that history retention and keeping track of science mode vs common mode are painful
- Would **not** include as a primary FOM
- Lowest-priority FOM to implement

# Summary

Three “primary” FOM’s for (reasonably) prominent display:

(FOM1) Pulsar strain sensitivity for ( $T_{\text{obs}} = \text{data run}$ )

(FOM2) Time (weeks) to reach energy conservation limit for Crab

(FOM3) Ellipticity sensitivity to known pulsars ( $T_{\text{obs}} = \text{data run}$ )

**We have a volunteer! -- Greg Mendell**