

Sub kHz Squeezing for Gravitational Wave Detection

LIGO-G040416-00-Z

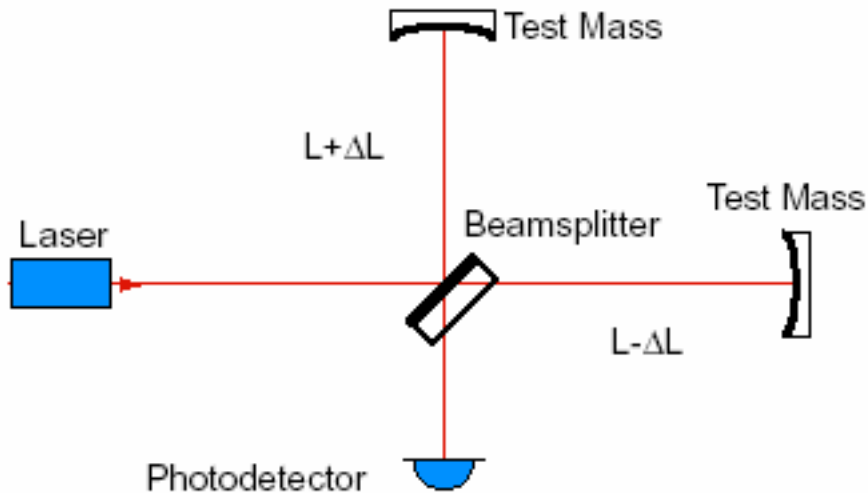
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Interferometric GW Detectors

Michelson Interferometer



LIGO (USA), L=4km



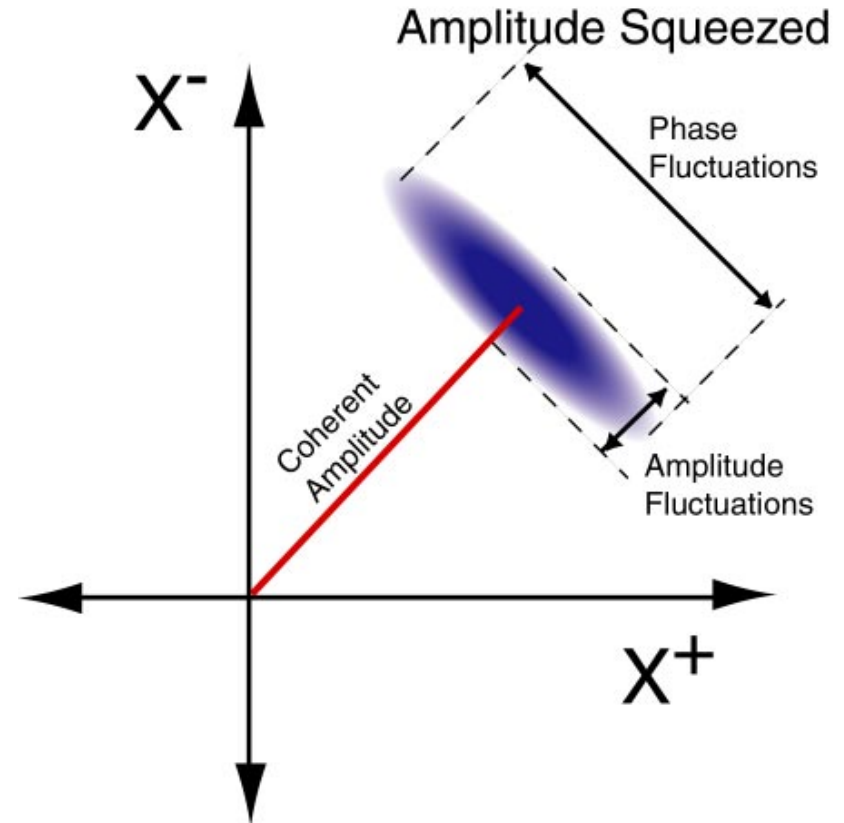
Strength of GW given by Strain, h ;

$$\frac{\Delta L}{L} = \frac{h}{2} < 10^{-22} \left(\frac{1}{\sqrt{\text{Hz}}} \right)$$

Quantum Mechanical Noise

- The EM field has quantum mechanical fluctuations
- The HUP relation for the EM field.

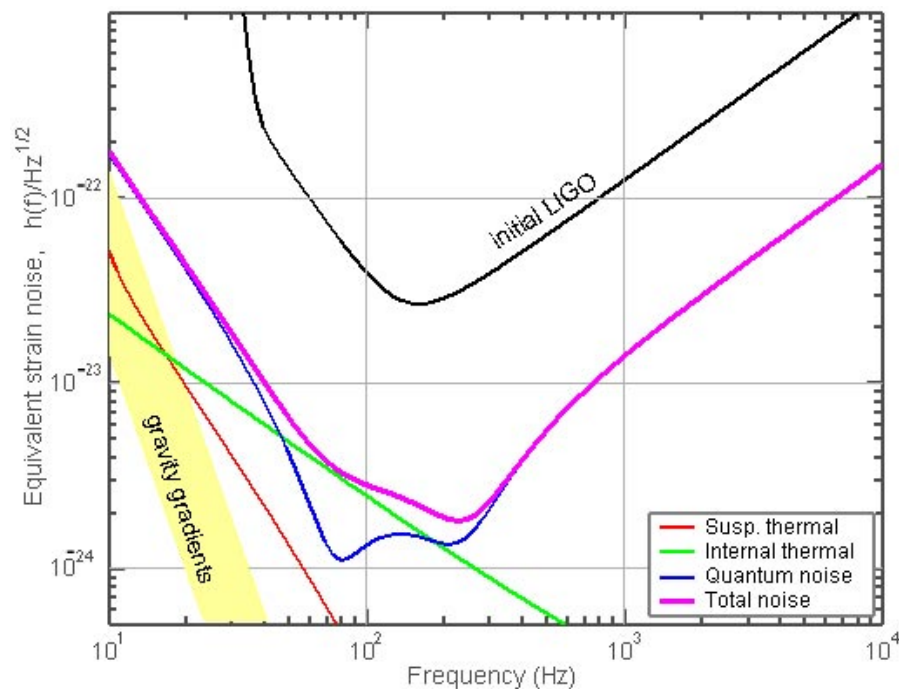
$$\Delta \hat{X}^+ + \Delta \hat{X}^- \geq 1$$



Low Frequency Squeezing?

- Applications
 - Gravitational Wave Detectors
 - Position sensing
 - Atomic Force Microscopy
 - Other quantum noise limited applications

Advanced LIGO target sensitivity



<http://www.ligo.caltech.edu/advLIGO/>

Previous Low Frequency Results

- Recent CW LF Results include
 - 220kHz - W.P. Bowen *et al.* [1]
 - 80kHz - R. Schnabel *et al.* [2]
 - 50kHz - J. Laurat *et al.* [3]

All experiments used common mode noise cancellation!

- We chose to investigate OPO

[1] W.P. Bowen *et al.* J. Opt. B **4** 421 (2002)

[2] R. Schnabel *et al.* arXiv quant-ph/0402064 (2004)

[3] J. Laurat *et al.* arXiv:quant-ph/0403224 (2004)

OPA/OPO Theory

Equations of motion for a singly resonant OPO/OPA;

$$\dot{\mathcal{A}} = -(\kappa_a + i\delta\Delta)a + \varepsilon a^\dagger b + \sqrt{2\kappa_{in}^a} A_s + \sqrt{2\kappa_{out}^a} A_v + \sqrt{2\kappa_l^a} A_l \quad (1)$$

a - fundamental field mode

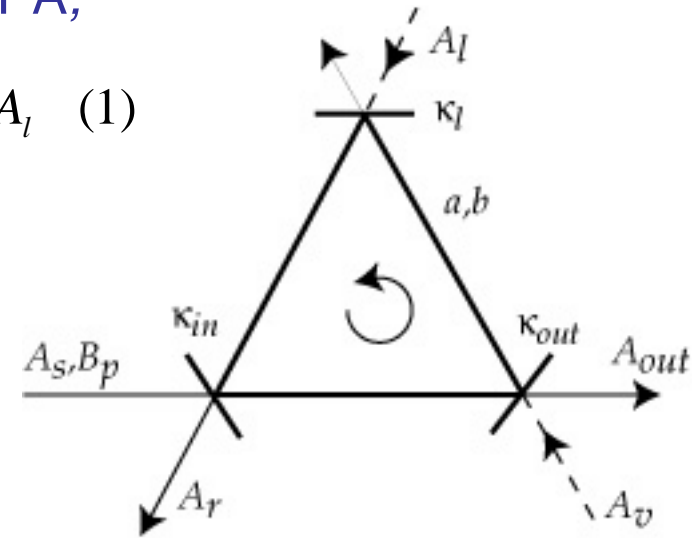
b - harmonic (pump) field

κ_j - decay constants

$\delta\Delta$ - fluctuating detuning

ε - nonlinear coupling strength

A_j, B - fields entering the cavity



B.Buchler PhD Thesis ANU 2002

The linearized equation of motion for the fluctuations is given by;

α - coherent amplitude of fundamental field, β - coherent amplitude of pump field

$$\delta\dot{\mathcal{A}} = -\kappa_a \delta a - i\alpha \delta\Delta + \varepsilon(\alpha^* \delta b + \beta \delta a^\dagger) + \sqrt{2\kappa_{in}^a} \delta A_s + \sqrt{2\kappa_{out}^a} \delta A_v + \sqrt{2\kappa_l^a} \delta A_l \quad (2)$$

OPA/OPO Theory II

The variances in the frequency domain for the OPA/OPO output are;

$$V_{OUT}^{\pm}(\omega) = \left[C_s V_s^{\pm}(\omega) + C_l V_l^{\pm}(\omega) + C_v^{\pm}(\omega) V_v^{\pm}(\omega) + \alpha^2 \left(C_p V_p^{\pm}(\omega) + C_{\Delta}^{\pm} V_{\Delta}^{\pm}(\omega) \right) \right] / |D^{\pm}(\omega)|^2 \quad (3)$$

↑	↑	↑	↑	↑
Seed	Loss	Vacuum	Pump	Detuning
(f < 2MHz)			(f < 2MHz)	(f < 50kHz)

For below threshold OPO $\alpha = 0$ and $V_s^{\pm} = 1$;

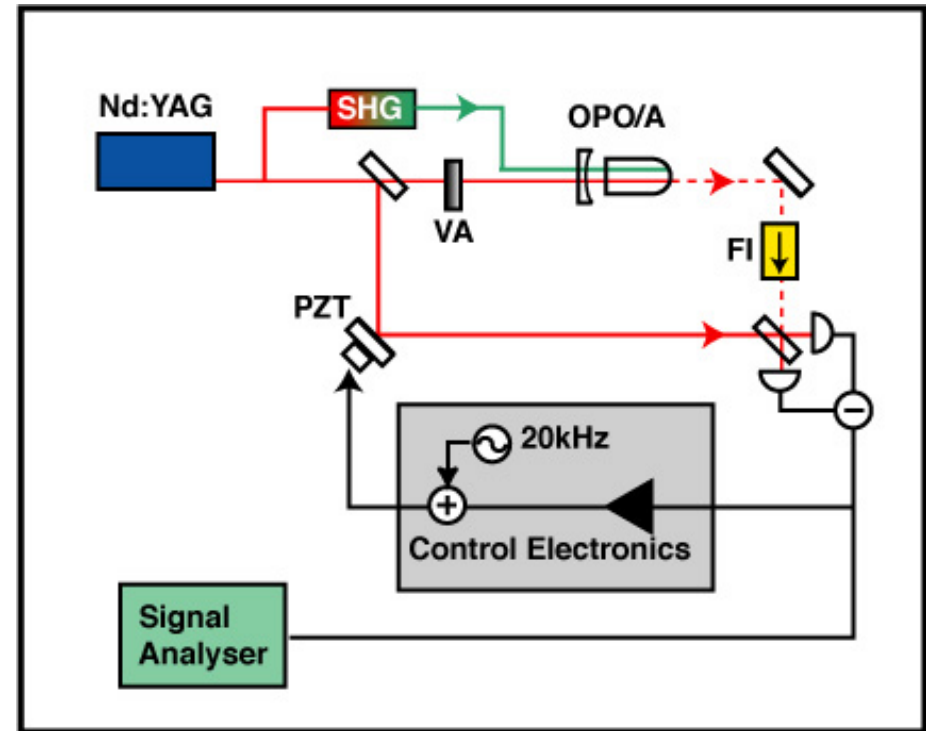
$$V_{OPO}^{\pm}(\omega) = \left[C_s + C_l + C_v^{\pm}(\omega) \right] / |D^{\pm}(\omega)|^2 \quad (4)$$

OPO is immune to laser noise, pump noise and detuning noise!

ANU OPA/OPO Experiment

- Seed power was varied - transition from OPA to OPO
- OPO/OPA cavity not locked;
- Homodyne phase locked using **noise power locking [3]**
- Noise power locking requires no coherent amplitude in the squeezed beam - **can lock a vacuum state.**
- In OPO operation a Faraday Isolator was used to reduce backscatter from homodyne detector

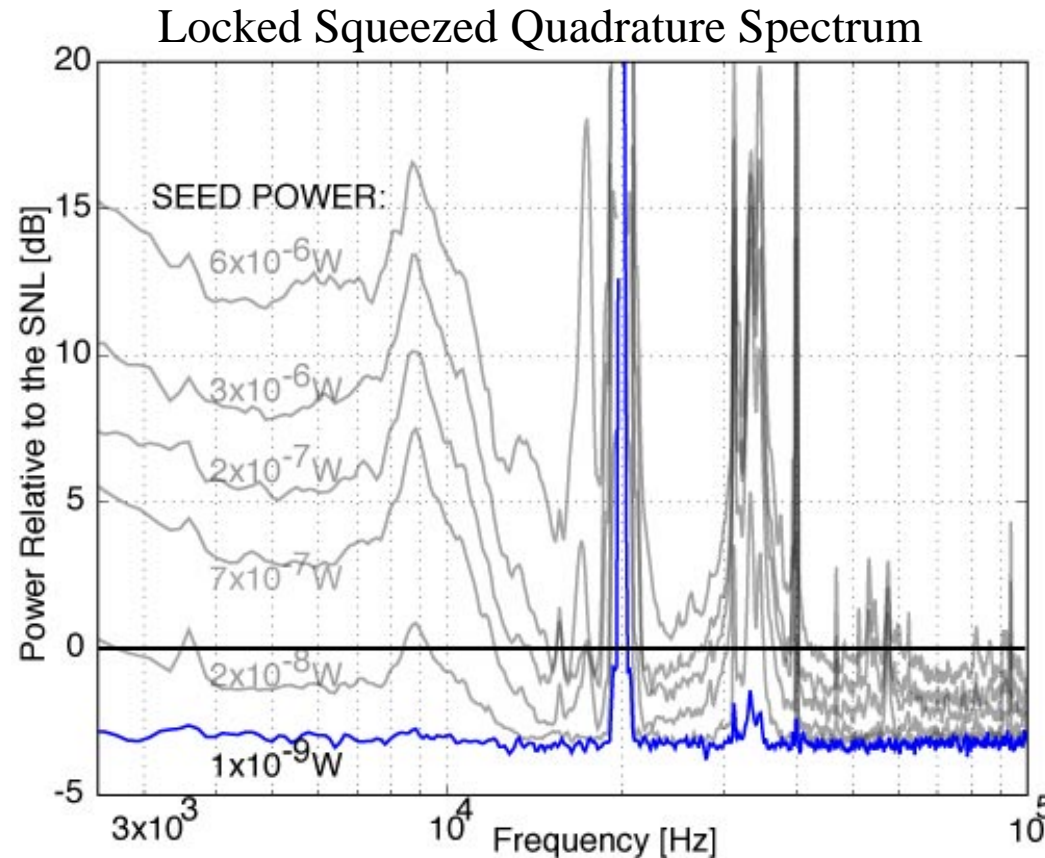
Experiment Schematic



[3] For example, J. Laurat *et al* arXiv:quant-ph/0403224

OPA Squeezed Quadrature Spectrum

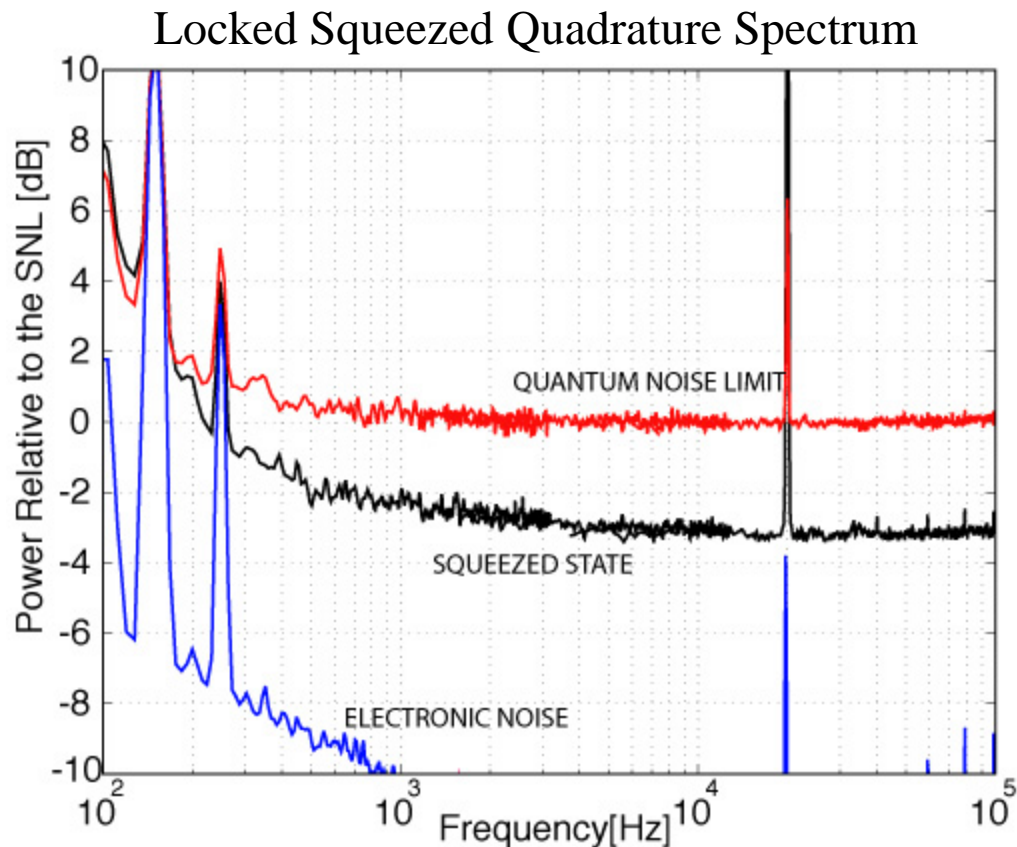
- Transition from OPA to OPO made by reducing seed power.
- Minimum noise quadrature was recorded.
- OPO immunity to noise sources
- Noise power locking modulation frequency peak at 20kHz



RBW = 128Hz, RMS averages = 1000, Electronic noise (at -12dB) subtracted from all traces

OPO Squeezed Quadrature Spectrum

- Lowest frequency squeezing result to date
- Covers SNL frequencies of LIGO
- Measurement limited at low frequencies by the stability of the unlocked OPO



From 100Hz-3.2kHz: RBW = 8Hz, no. RMS ave = 500
From 1.6kHz-12.8kHz: RBW = 32Hz, no. RMS ave = 1000
From 3.8kHz-100kHz: RBW = 128Hz, no. RMS ave = 2000

State Purity Results

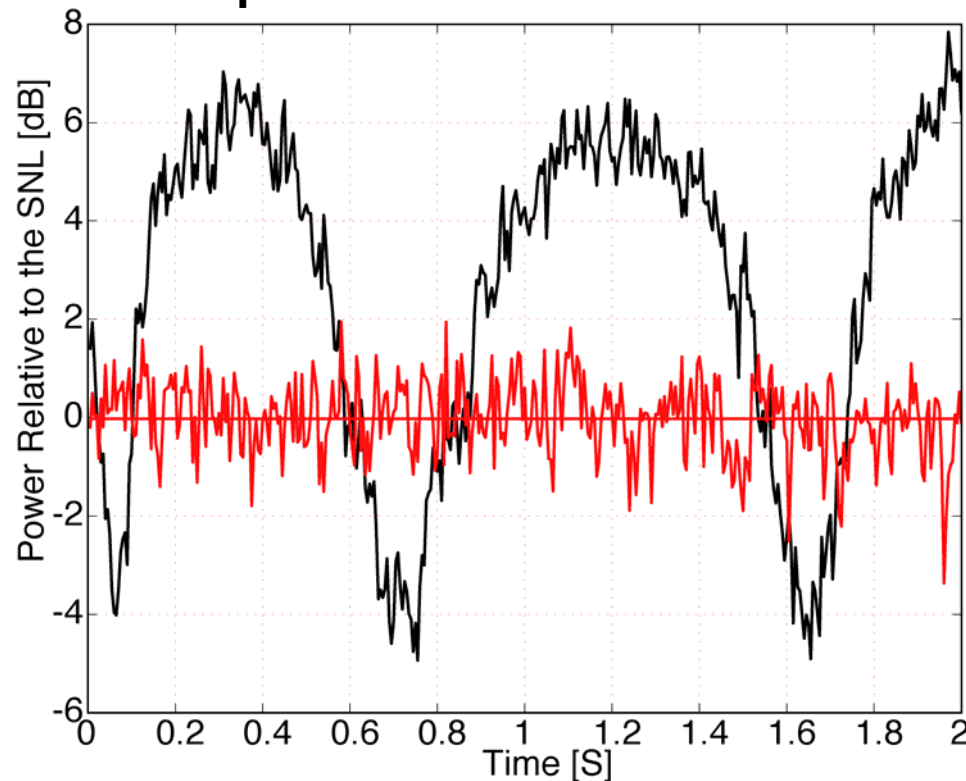
- $V_{\text{MEASURED}}^{\text{SQZ}} = 3.5 \text{ dB} \pm 0.4\text{dB}$
- Measured purity,

$$V^+V^-_{\text{M}} = 1.6 \pm 0.2$$

- $V_{\text{INFERRED}}^{\text{SQZ}} = 5.5 \text{ dB} \pm 0.6\text{dB}$
- Inferred purity before detection

$$V^+V^-_{\text{I}} = 1.3 \pm 0.1$$

Squeezed State at 11.2kHz



Squeezed State at 11.2kHz, RBW = 1kHz, VBW = 30Hz
Electronic noise was (9dB below SNL) was subtracted from traces

Conclusions & Future Work

Conclusions

<http://arXiv:quant-ph/0405137> (2004)

- Coupling mechanism of noise sources identified - the coherent seed field
- **Below threshold OPO is immune to laser, pump and detuning noise !**
- OPO squeezing measured down to 200Hz - lowest to date
- Noise locking technique used for homodyne phase

Future Work

- Develop new generation of squeezer that can be locked in OPO operation
 - Generate larger amounts of squeezing
 - Probe lower frequencies
- Further investigation of noise locking technique

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with;

$$D^{\pm}(\omega) = i\omega + \kappa_a + \begin{bmatrix} 3 \\ 1 \end{bmatrix} \epsilon^2 \alpha^2 / (2\kappa_b) \mp \epsilon\beta$$

$$C_s = 4\kappa_{in}^a \kappa_{out}^a$$

$$C_l = 4\kappa_l^a \kappa_{out}^a$$

$$C_v^{\pm}(\omega) = |2\kappa_{out}^a - D^{\pm}(\omega)|^2$$

$$C_p = 4\kappa_{out}^a \kappa_{in}^b (\epsilon/\kappa_b)^2$$

$$C_{\Delta}^{\pm} = 8\kappa_{out}^a \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$

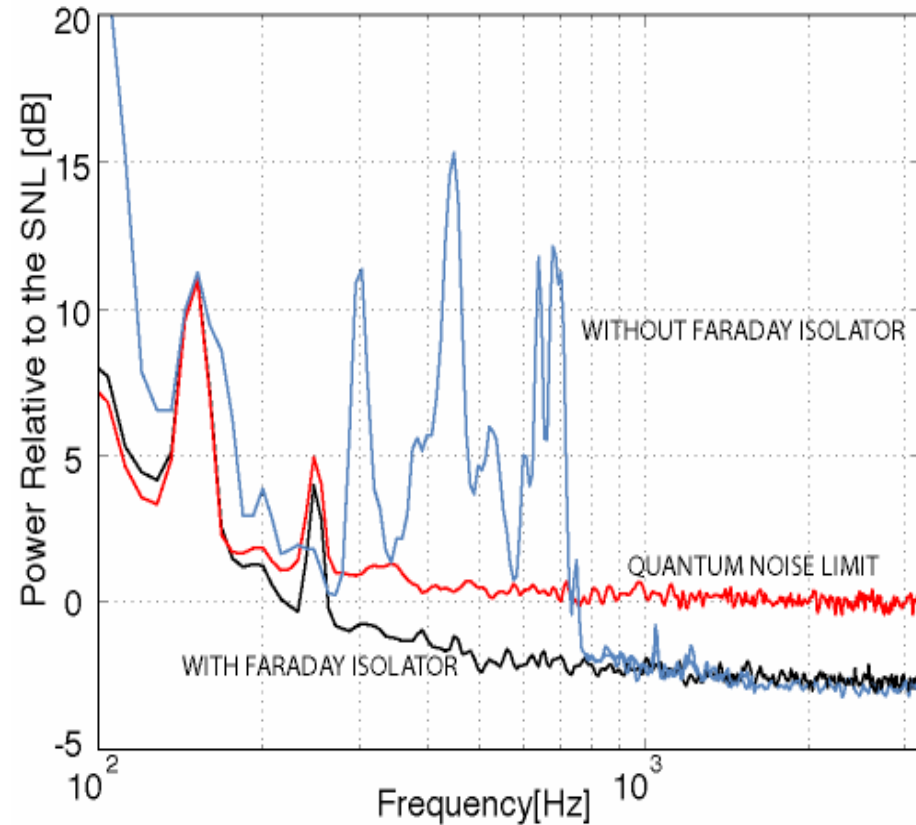
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OPO Squeezing Without/With Isolator

- Light from the local oscillator beam backscattered from the photodetectors seeded our OPO cavity ($\sim 1\text{pW}$)
- Undesired seed contributed to low frequency noise contamination.
- A Faraday Isolator between OPO cavity and homodyne detector to eliminated seed - **low frequency squeezing was recovered!**



RBW = 8Hz, No.RMS ave = 400 without isolator, 500 for QNL and with Isolator. Electronic noise (not shown) was not subtracted