

# *The Effect of Transverse Shifts on the LIGO Interferometer*



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## *Purpose*

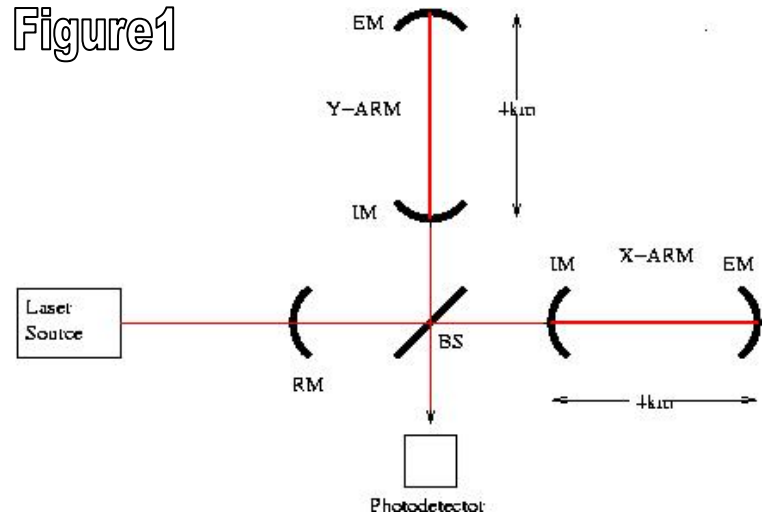
- Through computer simulations I will map the response of the interferometer to various transverse shifts in the optics.
- Determine how these shifts will effect the detector's performance.

## *Motivation*

- It is believed that one of the input mirrors at the Hanford observatory is misaligned by 1-2 cm.
- Also, the laser beam, at times, has been shifted on the order of 1 cm.

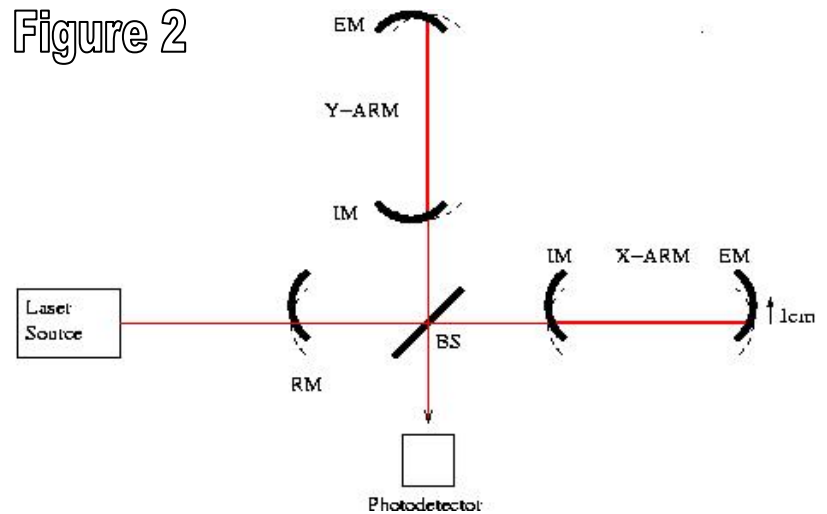
- Figure 1 shows the interferometer in the normal operating state or the unperturbed state.

Figure 1



- Figure 2 shows the interferometer in a perturbed state where all the mirrors have been shifted in the x-direction by 1 cm.

Figure 2



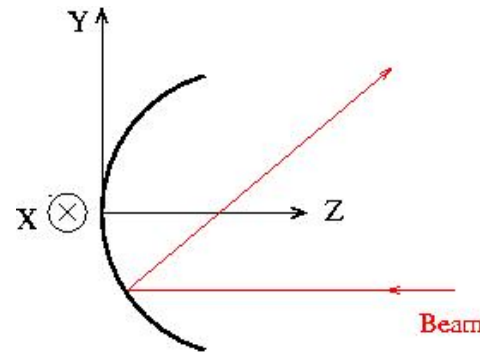
## End-to-End (e2e)

- Time domain simulation package.
- SimLIGO is a good description of the LIGO detector with detailed models of the optics, suspension system, noise sources, wavefront and length sensors, etc.
- Relatively Long simulation time.

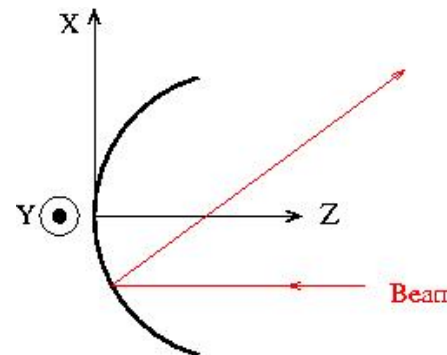
## MIT FFT Code

- Frequency domain simulation package.
- Gives a very accurate description of the interferometer in the steady state.
- Static simulation that doesn't simulate feedback corrections.
- Relatively short simulation time.

- Rotation about the x-axis is known as pitch. If the mirror is offset by 1cm in the Y-direction, a pitch of  $0.01/R$  radians is needed to counter the shift, where  $R$  is the radius of curvature for that mirror.
- Similarly, rotation about the y-axis is called yaw (notice the sign difference between the two).



Positive Y-Shift  
 Negative Pitch =  $\frac{dY}{R}$



Positive X-Shift  
 Positive Yaw =  $\frac{dx}{R}$

$$\text{Yaw} = \frac{\Delta x}{R}$$

Example of Rotation: If  $R = 7500\text{m}$ , then a 1cm shift would produce equivalent yaw (or pitch) of

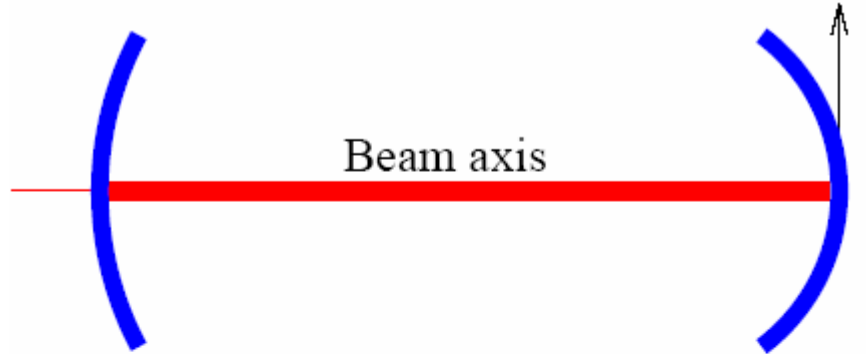
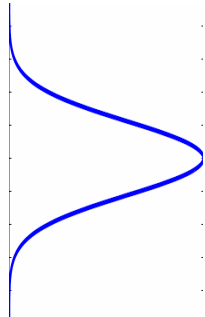
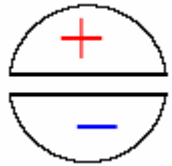
$$\frac{0.01 \text{ m}}{7500 \text{ m}} = 1.3 \times 10^{-6} \text{ radians}$$

Divergence angle: 
$$\phi = \frac{\lambda}{\pi \omega_0} = 1 \times 10^{-5} \text{ radians}$$

A calculation by Fritschel suggests that a misalignment of  $1 \times 10^{-8}$  radians should result in a 0.5% increase in shot noise.

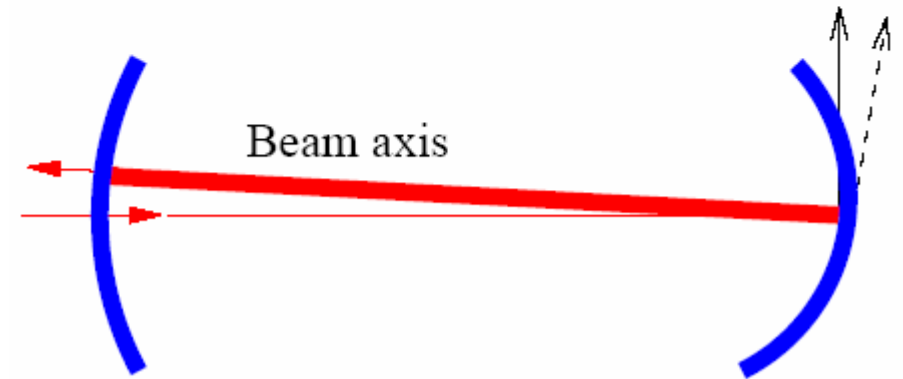
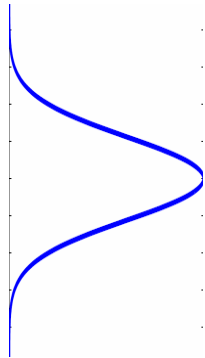
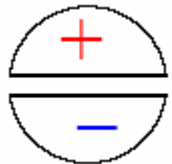
**Signal 0**

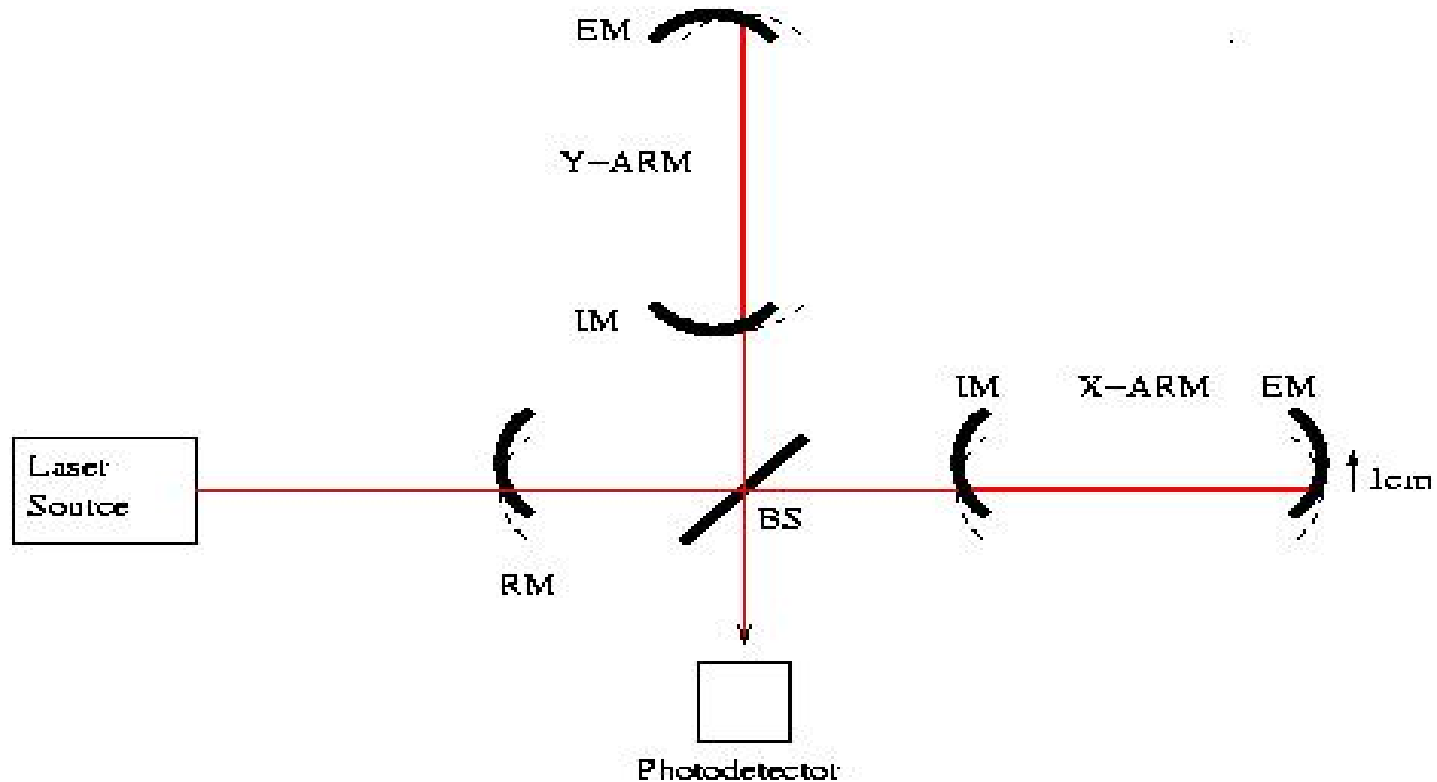
$\Leftarrow$



**Signal non0**

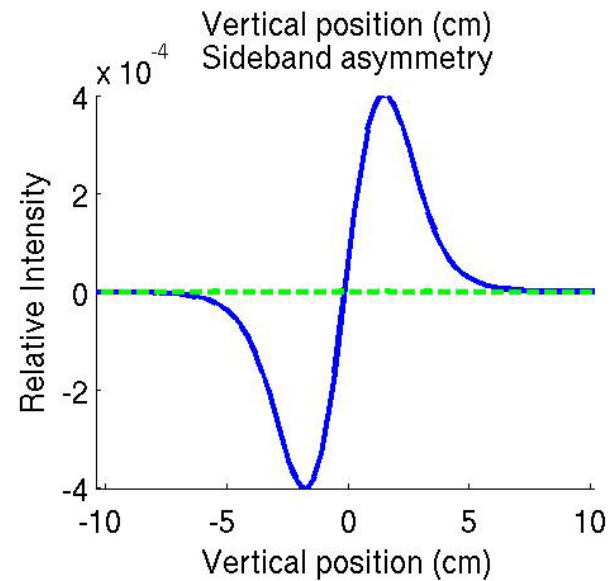
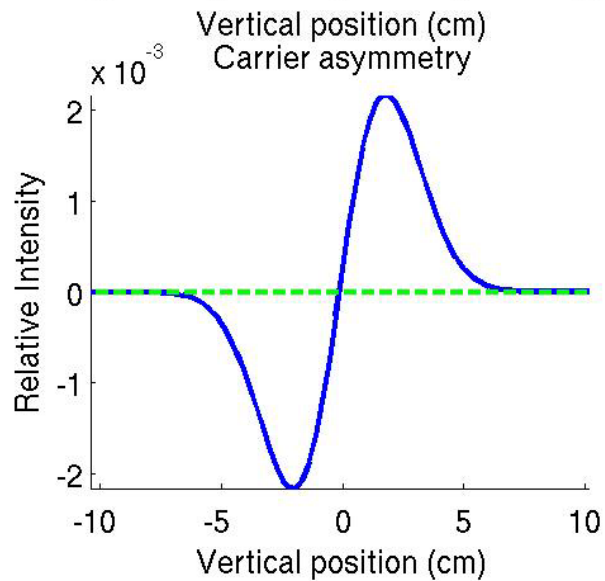
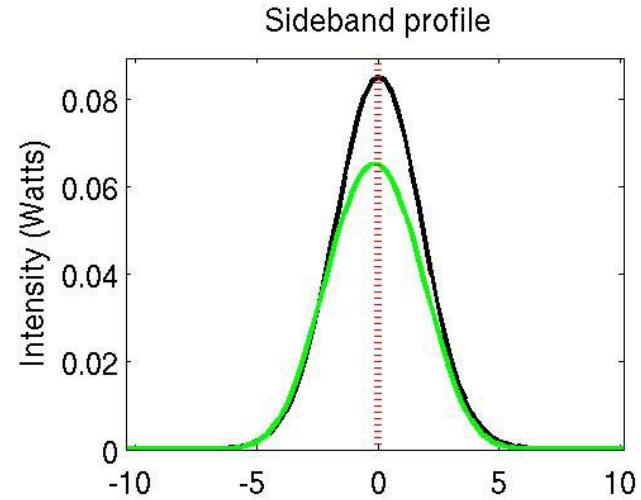
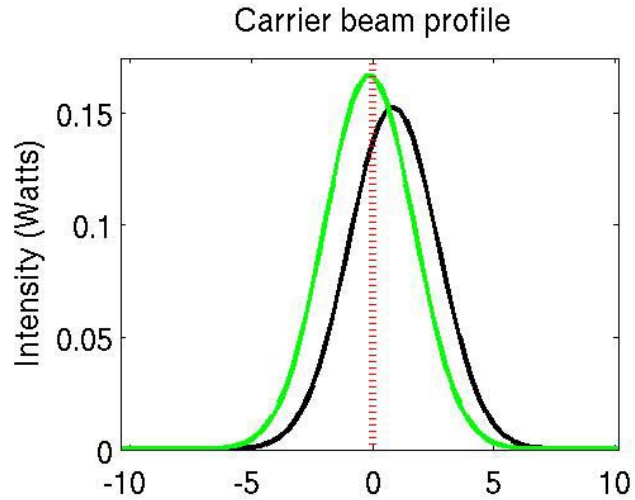
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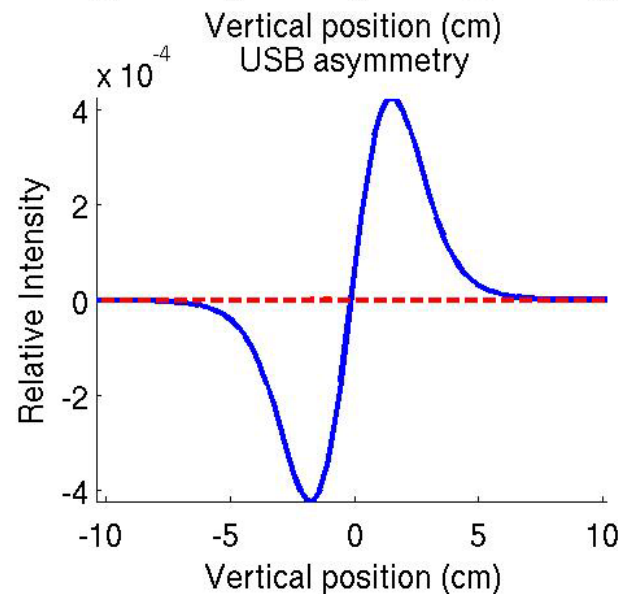
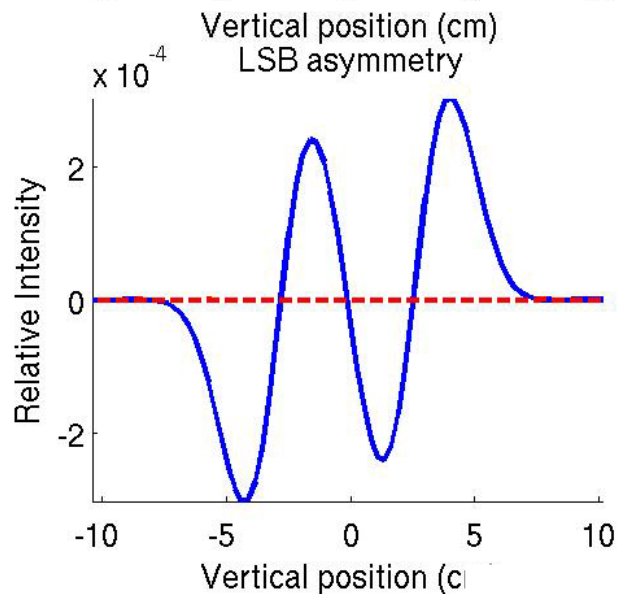
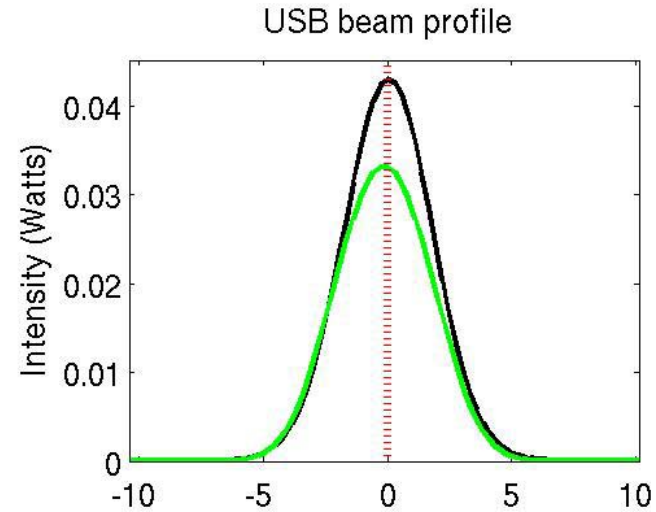
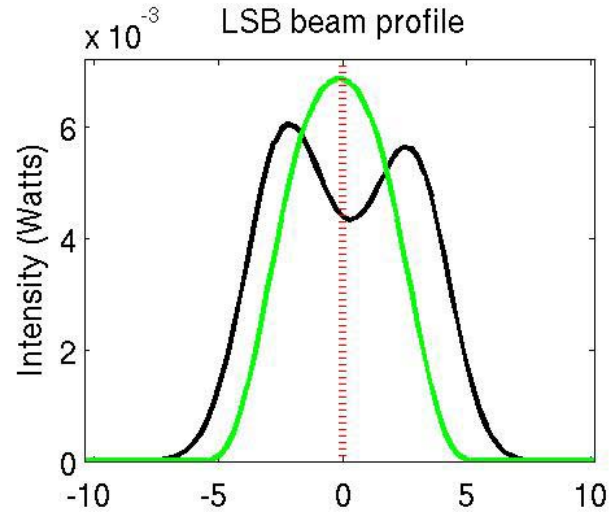


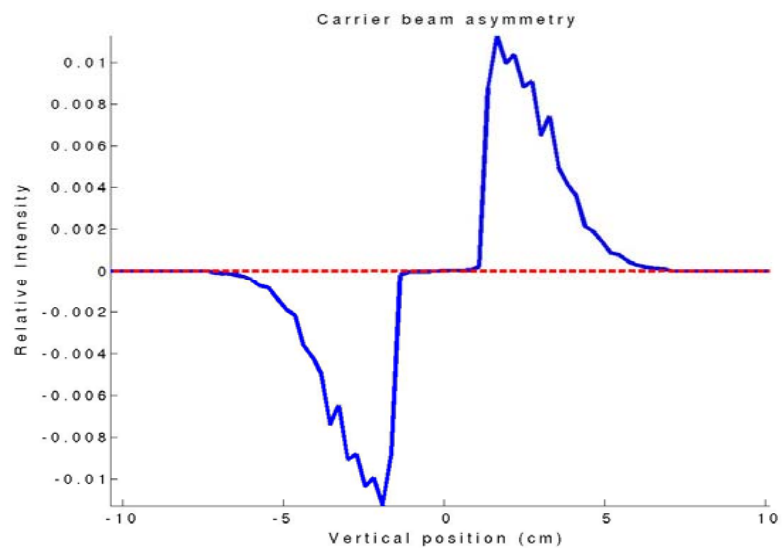
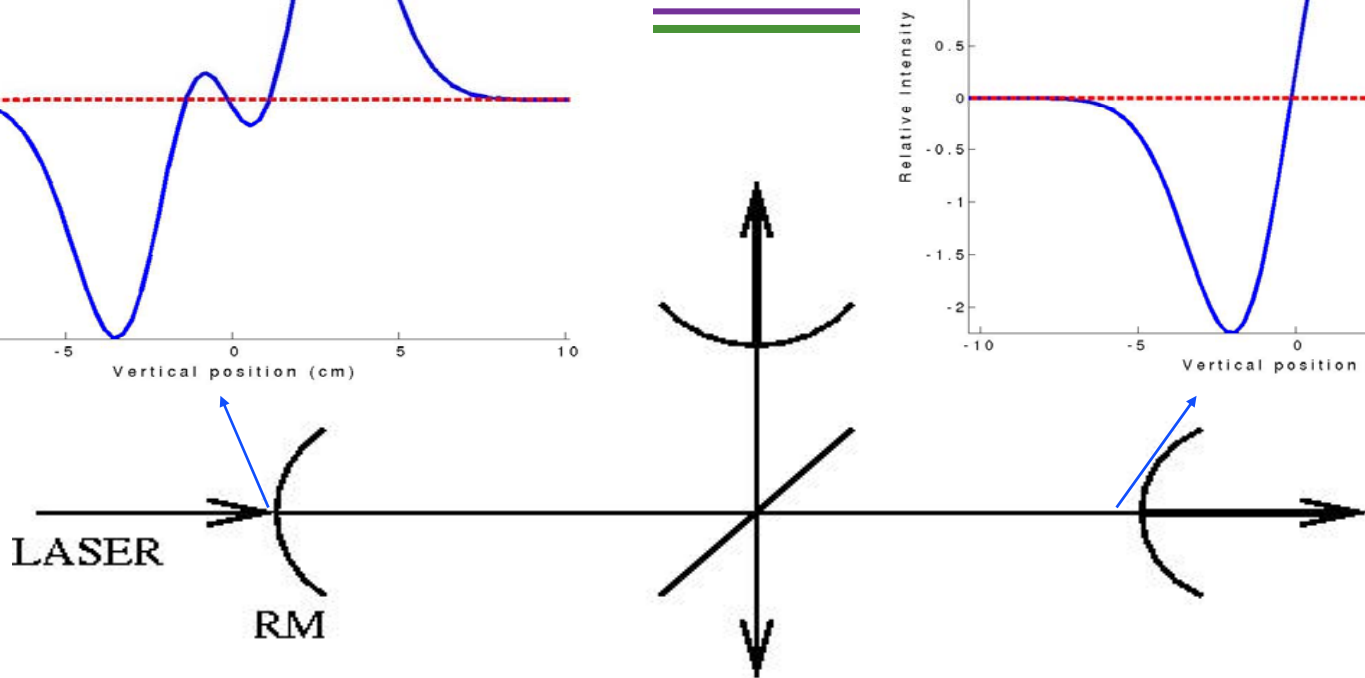
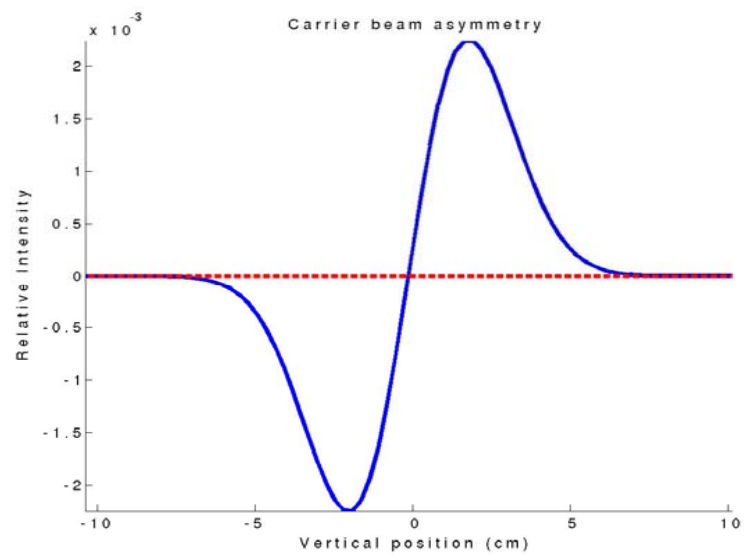
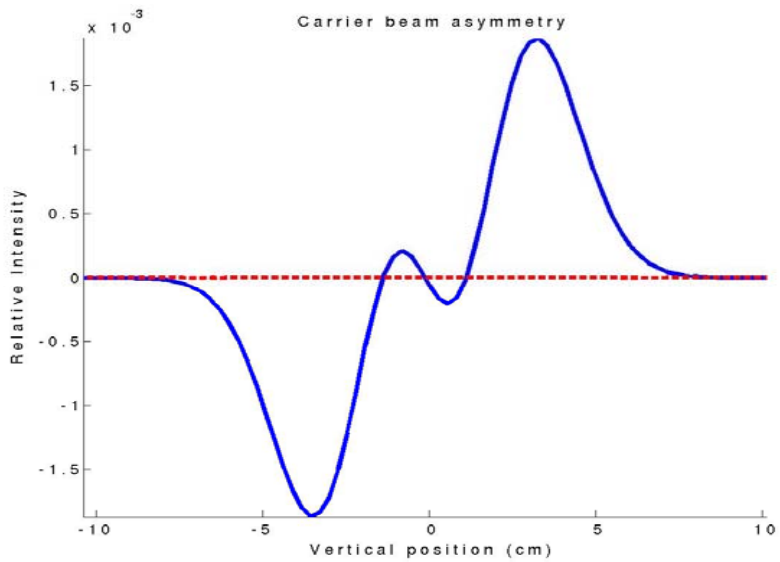


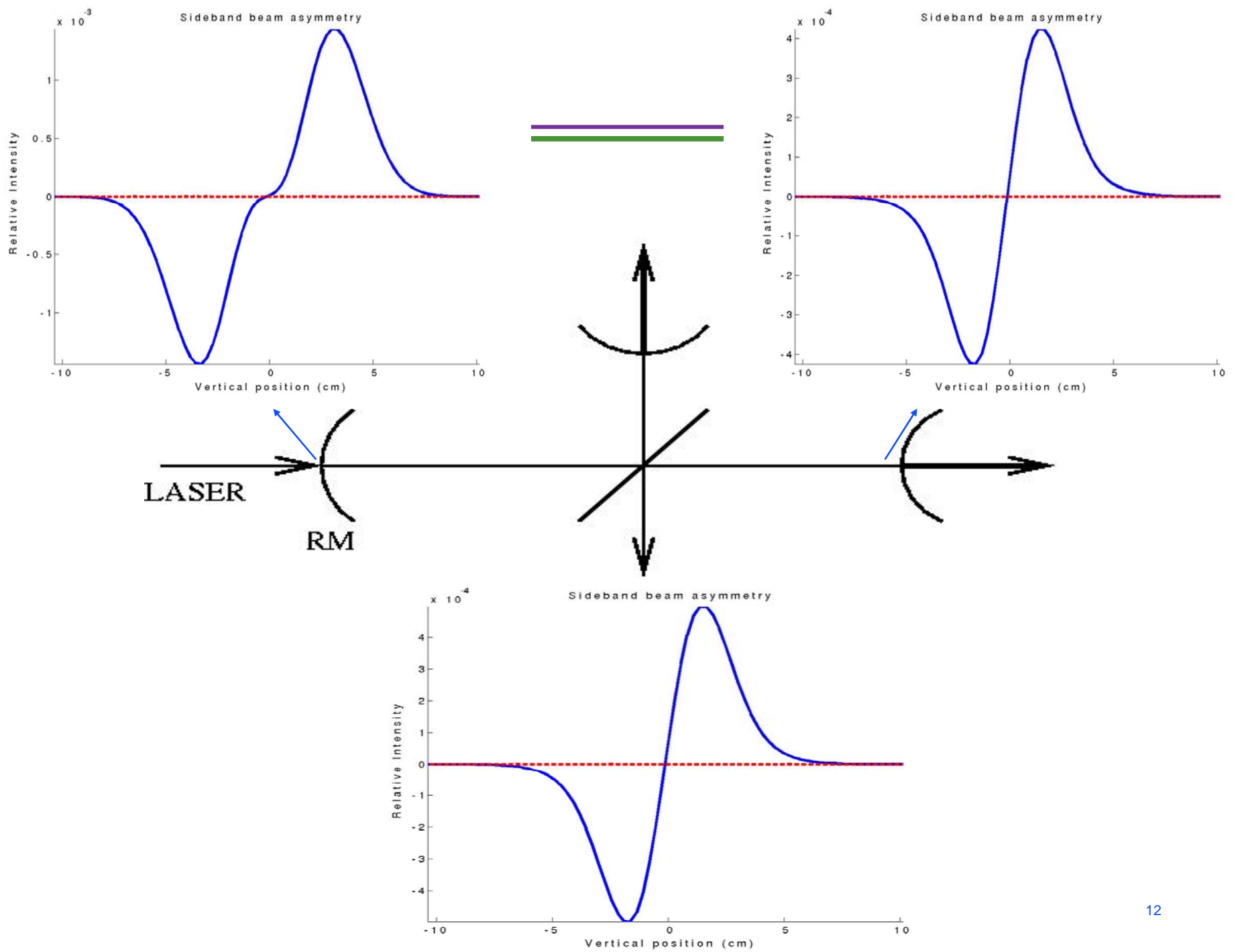
- In FFT I used the parameters and specifications to model LIGO Hanford's detector. In this simulation I shifted the 5 mirrors, Recycling, ITMX, ETMX, ITMY, ETMY, by 1cm in the x direction.

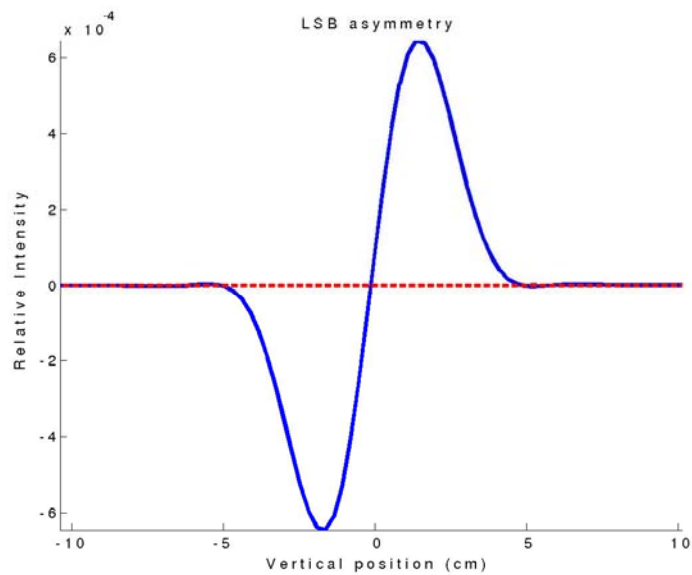
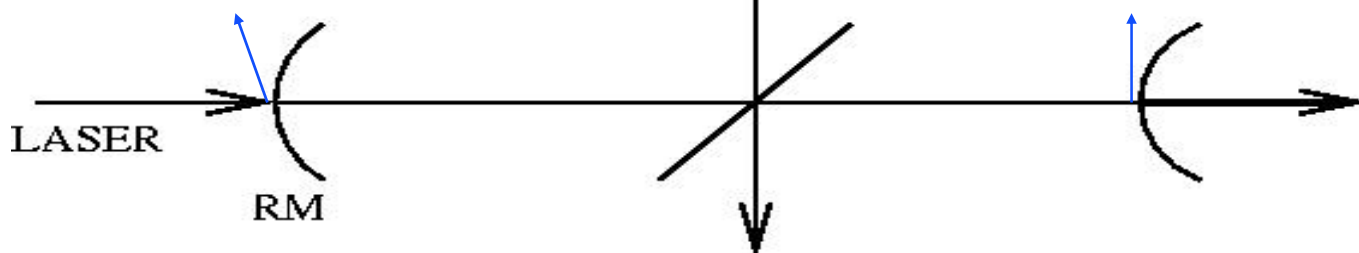
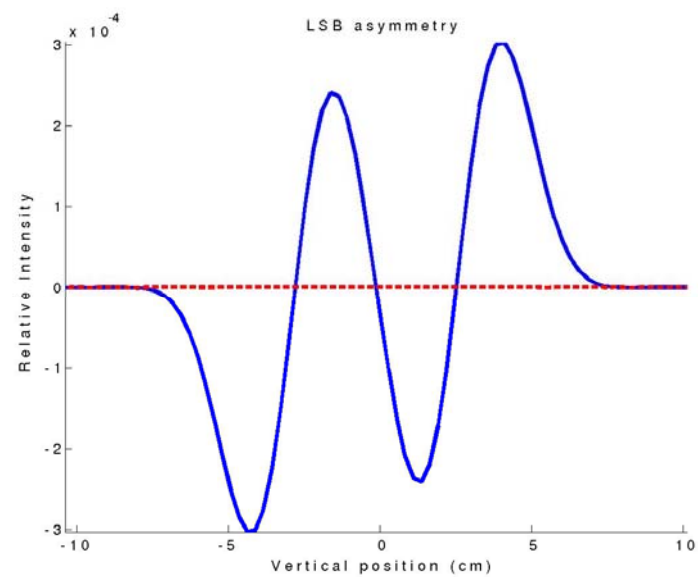
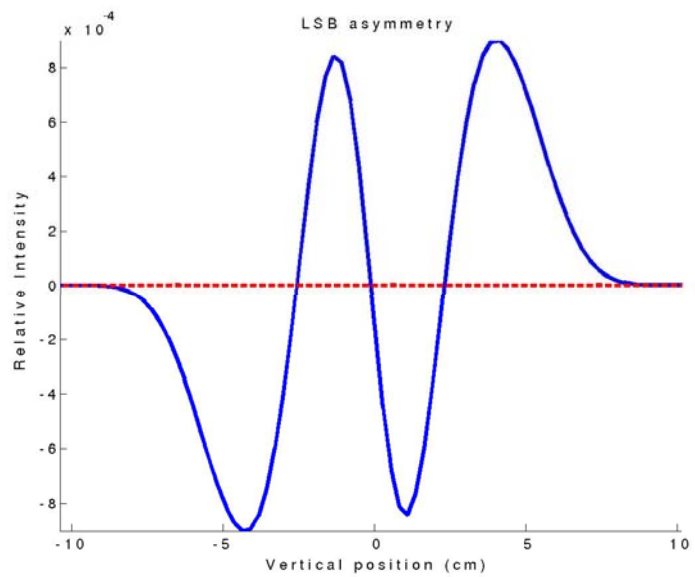


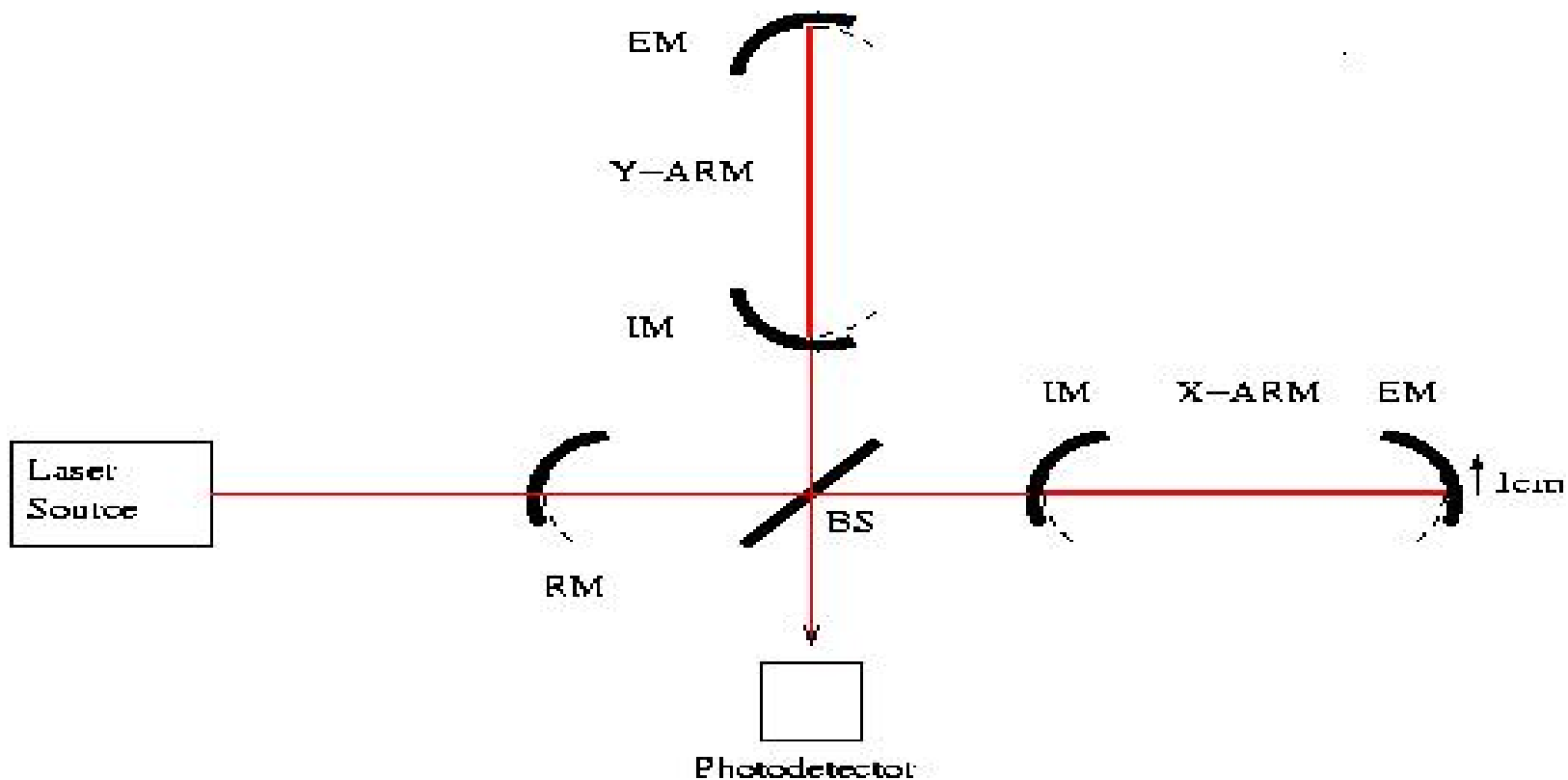






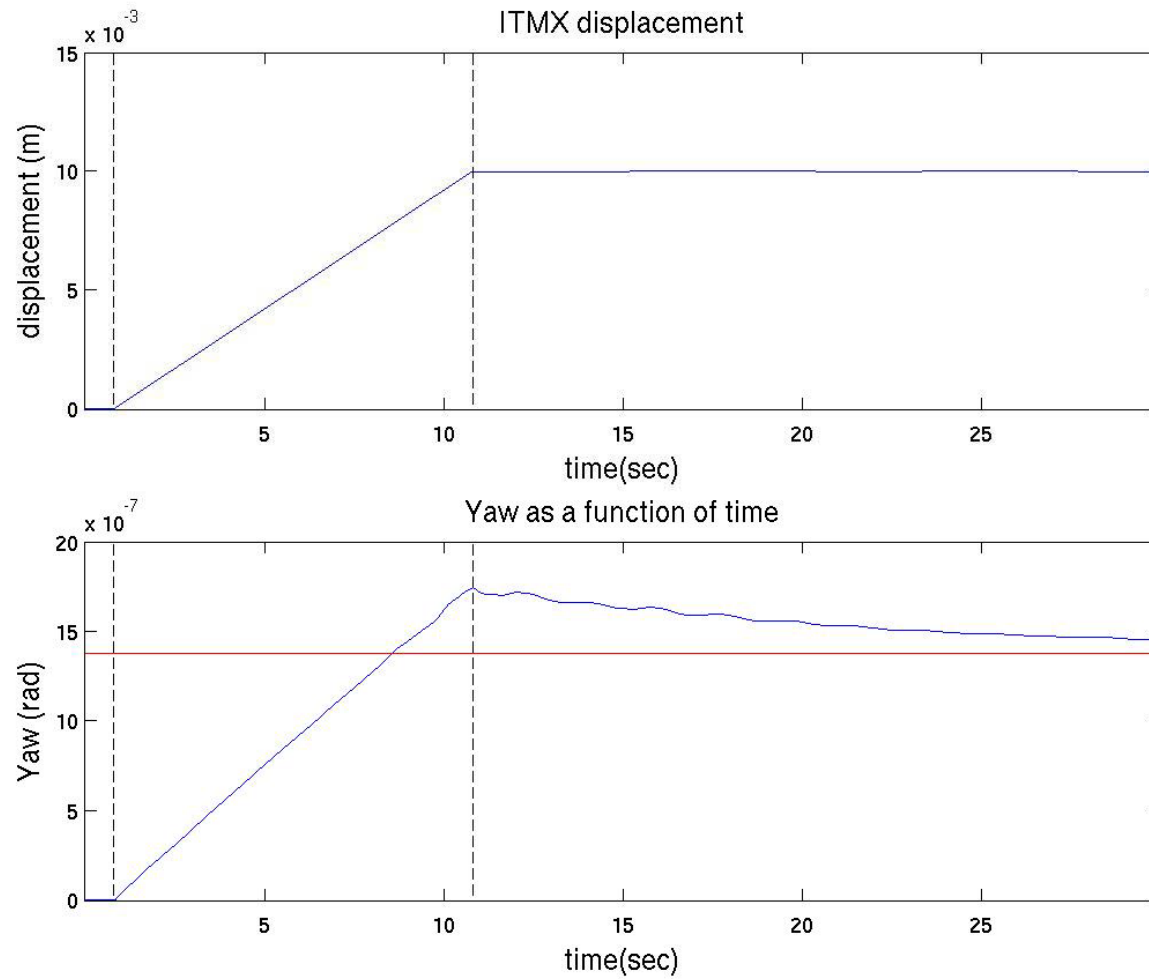




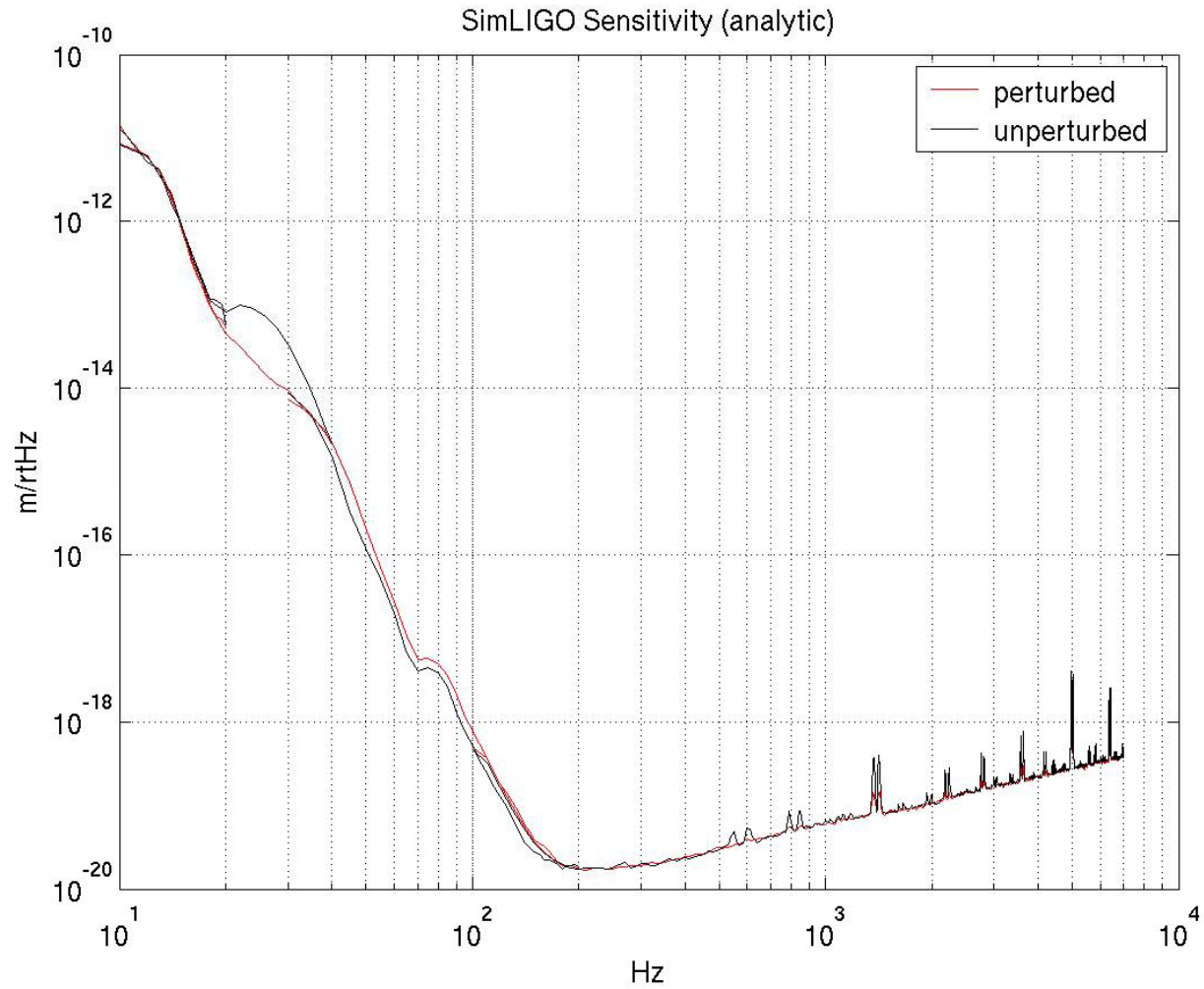


- To stay in a resonant and locked state, the mirrors of the interferometer must rotate to counteract the 1cm shift.

# *e2e Run: Shift in All mirrors*



# Sensitivity/Noise Curve





- Through my investigations this summer, I was able to diagnose some errors in the simulation programs.
- The independent simulation packages gave coinciding results, which adds some credibility to the simulations.
- Many of the results obtained agree with prior predictions made about how transverse shifts should affect the interferometer.

## Special Thanks to

- Biplab Bhawal
- Ken Libbrecht
- LIGO/SURF
  - NSF

