

Astrophysical constraints on BH-NS and NS-NS mergers and the short GRB redshift distribution

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Feb 23, 2007

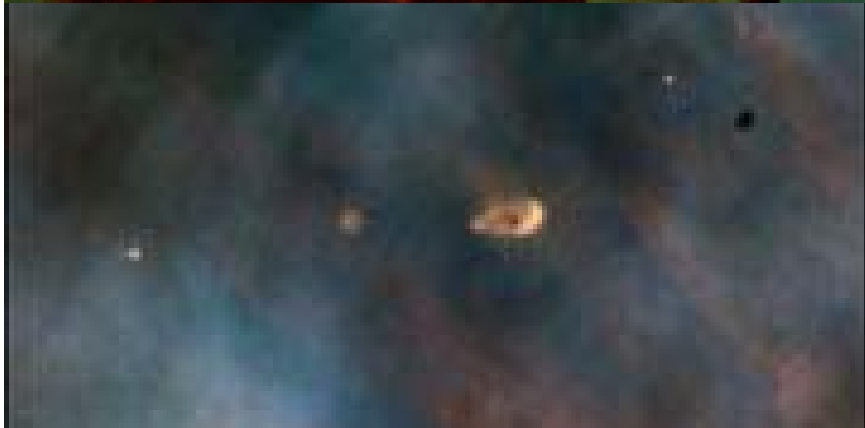
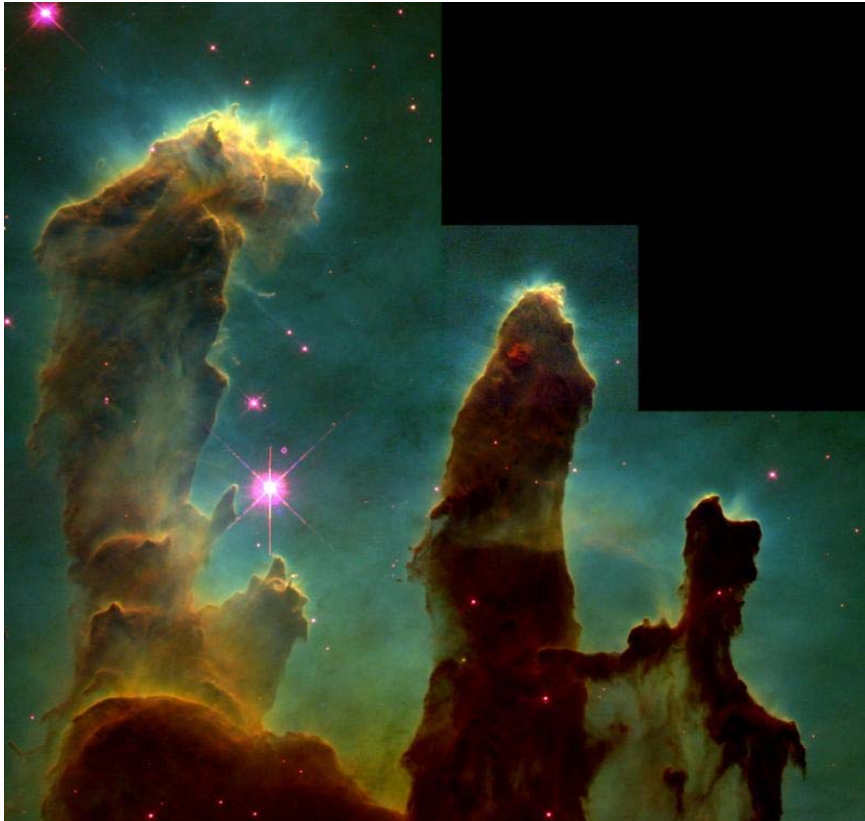
Outline

- Gravitational Wave Searches for Binaries
- How to Make Compact Binaries
 - Population synthesis
- Predictions and Constraints: Milky Way
 - Comparing predictions to observations
 - Physics behind comparisons : what we learn
 - What if a detection?
- Why Ellipticals Matter
 - Two-component star formation model
- Predictions and Constraints Revisited
 - Prior predictions
 - Reproducing Milky Way constraints
- Short GRBs
- Conclusions

Collaborators

- V. Kalogera Northwestern
 - C. Kim Cornell
 - K. Belczynski New Mexico State/Los Alamos
 - T. Fragos Northwestern
 - J. Kaplan Northwestern
-
- LSC (official LIGO results)

Big Picture



EM Waves

Source:

~any accelerating charge

Strong coupling:

Imaging often practical:

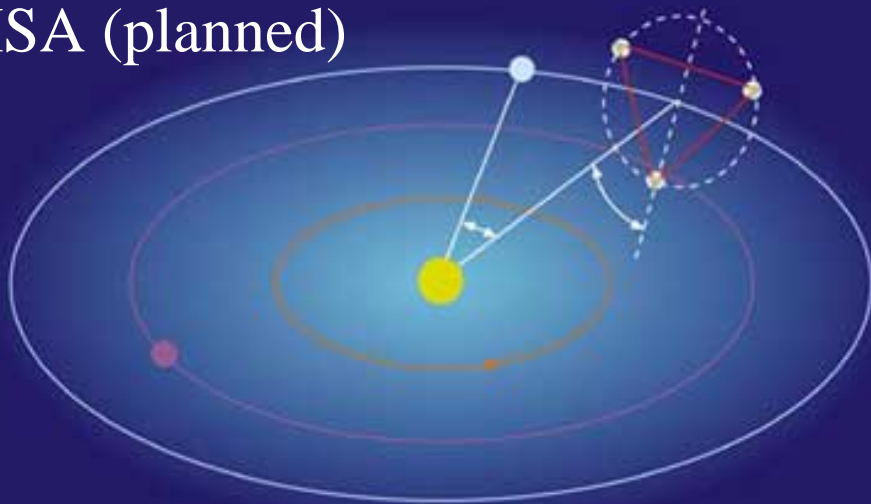
(common sources)

>> wavelength

- Easy to make & detect
- Easy to **obscure**

Big Picture: Spectrum

LISA (planned)



LIGO (running)

QuickTime™ and a
TIFF (LZW) decompressor
are needed to see this picture.

Detectors

Pulsar timing
CMB fluctuations

Space-based interferometers
(LISA)

Ground-based interferometers
(LIGO/VIRGO/GEO/TAMA)

Big Science Payoff

Test GR (in detail)

- Orbits agree EMRI mergers
- Spacetime agrees EMRI mergers

Cosmology

- Trace galaxy mergers? Binary mergers
- Waves from inflation? Stochastic

Nuclear physics

- Compressibility of nuclear matter NS disruption
NS surface bumps

Supernovae

- Constrain asymmetry and kick Supernovae bursts
Binary mergers
- Spin imparted? Binary mergers

Stars near galaxy centers

- Capture rates

Small compact binaries

- Map all faint, close (“white dwarf”) binaries
- Mass transfer, tidal coupling,

Understand stellar evolution

- Mass transfer rates Binary mergers
- Maximum NS mass Binary mergers

Reveal mystery : GRB engines:

- Hypermassive NS?
- Merger-driven?

...and much more

Small effect at earth!

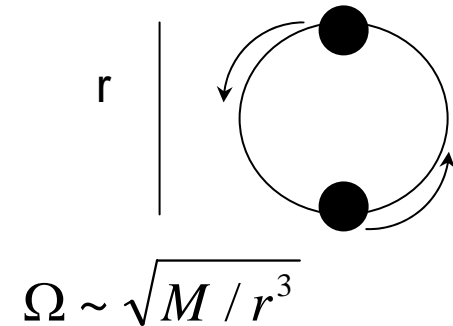
- Example:**

Two black holes

Newtonian circular orbit

$$f = 2 f_{orb} = 2(\Omega / \pi)$$

$$f = 10^3 \text{ Hz} (M / 8M_o)^{-1} (r / 6M)^{-3/2}$$



- Characteristic relative length changes**

~ (kinetic energy)/(distance)

$$h \sim \frac{1}{d} \frac{d^2 I}{dt^2} \sim \frac{Mv^2}{d} \sim \frac{M}{d} \left(\frac{M}{8M_o} \right)^{-1} \left(\frac{r}{6M} \right)^{-3/2}$$

$$h \sim 10^{-21} (M / 8M_o)^{5/3} (d / 3)$$

Sensitivity needed? (LIGO)

$$\Delta L \sim h L \sim 10^{-21} 4\text{km}$$

$$\sim 4 \times 10^{-16} \text{ cm}$$

laser light $\sim 10^{-4} \text{ cm}$

atom $\sim 10^{-8} \text{ cm}$

proton $\sim 10^{-13} \text{ cm}$

d

pickTime™ and a compressed decompressor to see this picture.

Sensitivities of detectors

- **Present sensitivities: LIGO**

Reached

~ design sensitivity

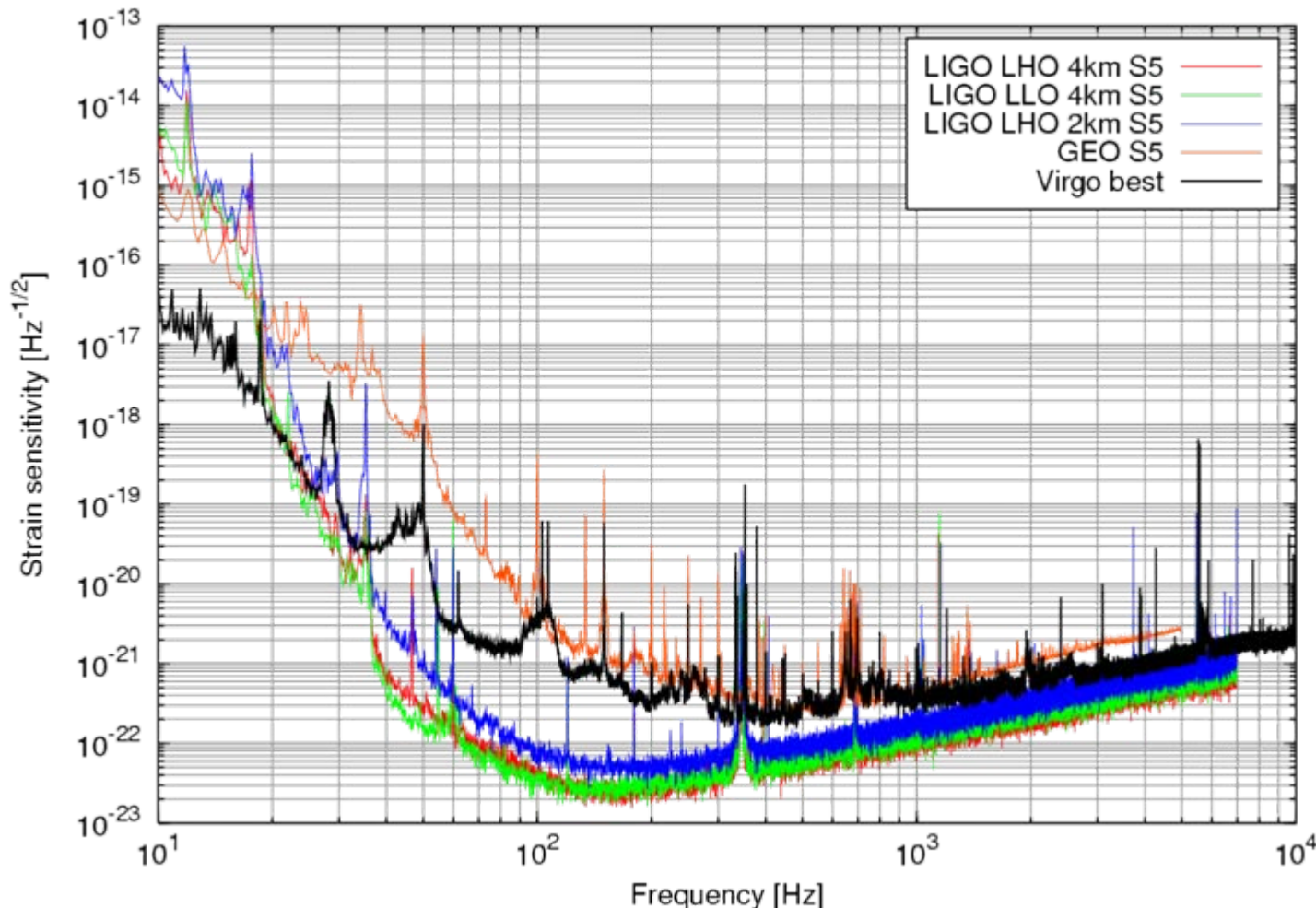
QuickTime™ and a
TIFF (Uncompressed) decompressor
are needed to see this picture.

LIGO:

- at target
- **taking data**
(~2 calendar yr)

Sensitivities of detectors

- Present sensitivities: Others



GEO

- at target
- much less sensitive

VIRGO

- near target
- target:
noise < LIGO
at low, high f

Sensitivities of detectors

- Lots of astrophysically relevant data:

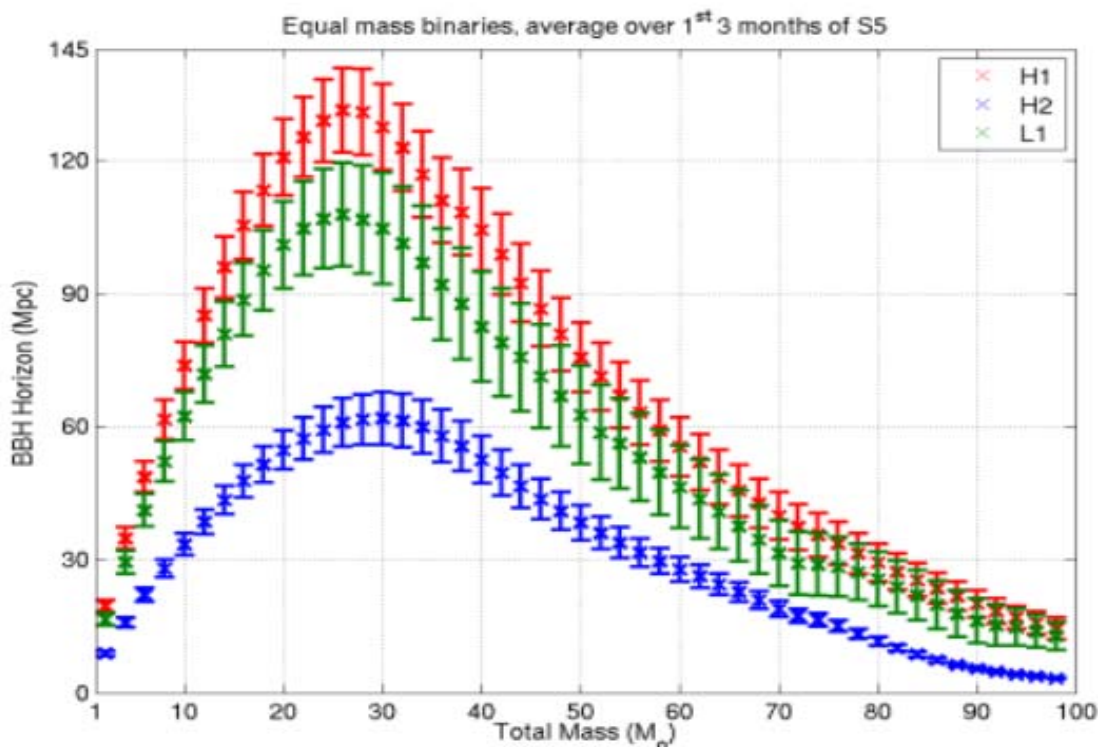
Example: Average distance to which $1.4 M_{\odot}$ NS-NS inspiral range ($S/N=8$) visible

QuickTime™ and a
TIFF (Uncompressed) decompressor
are needed to see this picture.

Sensitivities of detectors

Range depends on mass

- For 1.4-1.4 M_{\odot} binaries, ~ 200 MWEG (# of stars \leftrightarrow our galaxy) in range
- For 5-5 M_{\odot} binaries, ~ 1000 MWEGs in range
- Plot: Inspiral horizon for equal mass binaries vs. total mass
(horizon=range at peak of antenna pattern; ~ 2.3 x antenna pattern average)



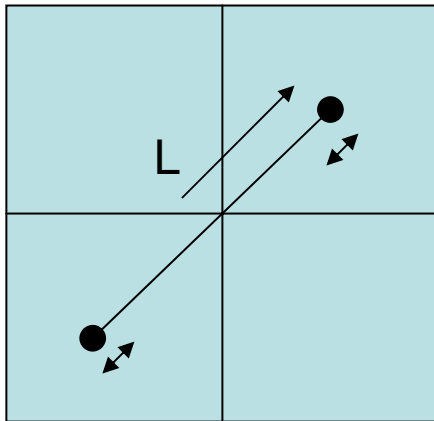
- ...using only the ‘inspiral signal’ (=understood)
- no merger waves
- no tidal disruption influences

Gravitational plane waves

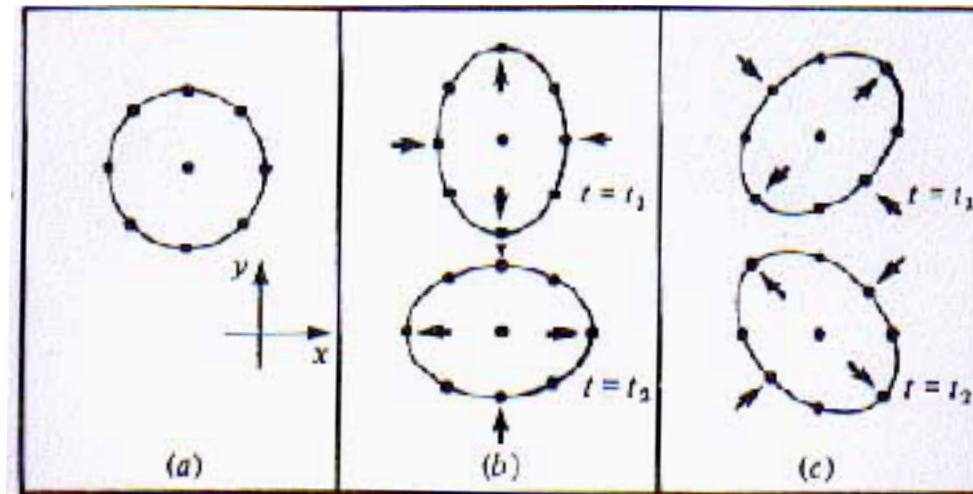
- Stretching and squeezing
Perpendicular to propagation
- Two **spin-2 (tensor)** polarizations

QuickTime™ and a
TIFF (LZW) decompressor
are needed to see this picture.

$$h \sim \Delta L/L$$



QuickTime™ and a
TIFF (LZW) decompressor
are needed to see this picture.



$$h_{xx} = -h_{yy} \quad h_{xy} = -h_{yx}$$

Detecting gravitational waves

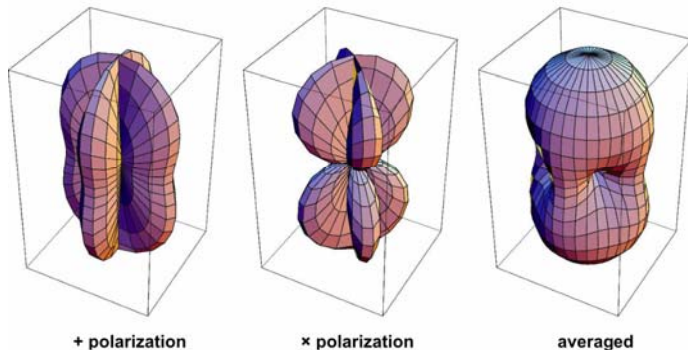
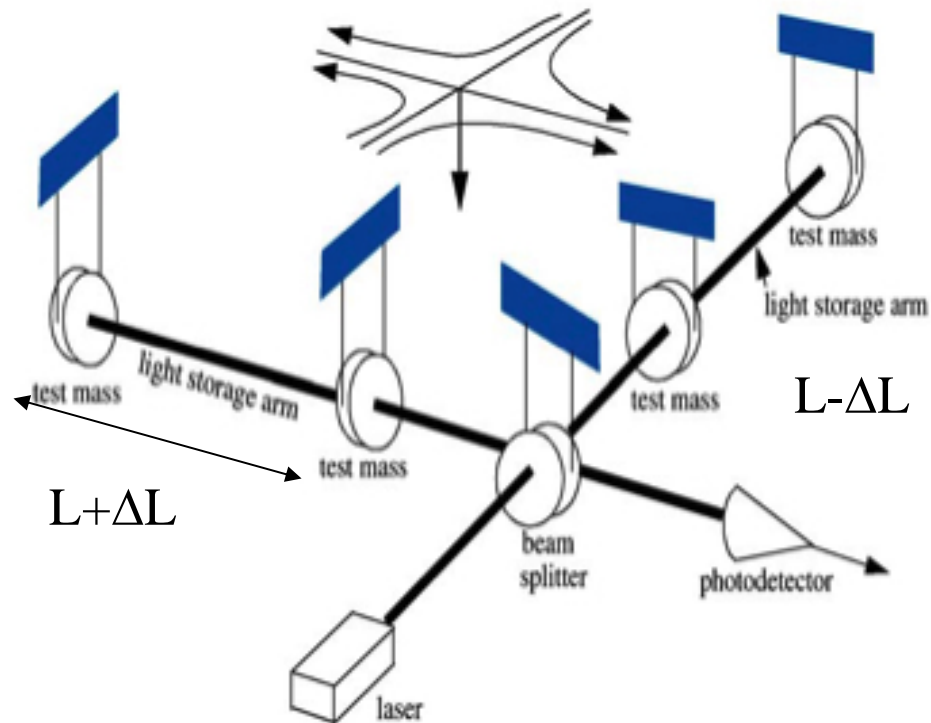
- Interferometer:

- Compares two distances
- Sensitive to

$$f \approx 1/t_{store}$$

[tunable]

- Each interferometer = (weakly) directional antenna



Jay Marx, [Texas symposium 2006](#)

Measuring inspiral sources

Using only ‘inspiral’ phase

____[avoid tides, disruption!]

- Mass

Must match!

$df/dt \rightarrow$ mass

- Distance

$$SNR \propto \frac{M^{5/6}}{d}$$

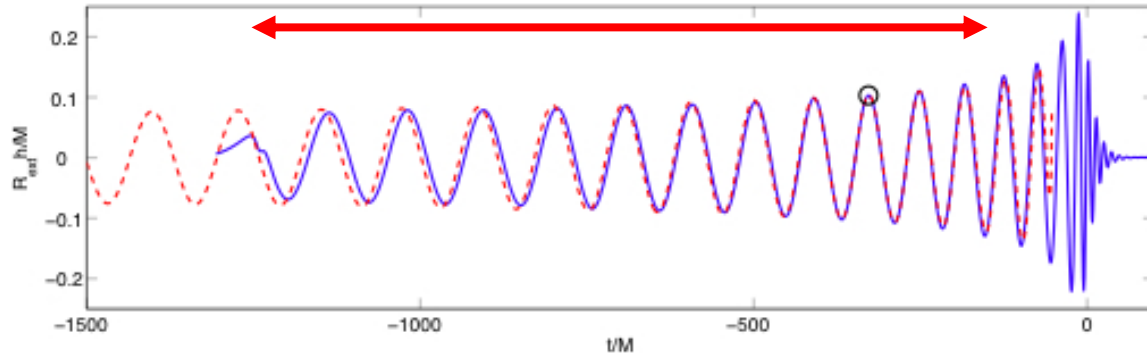
- Location on sky

- Orbit orientation

- (Black hole) spin

Precession

Only if extreme



Sample uses: short GRBs

1) Easily distinguish certain short GRB engines:

- ‘High’ mass BH-NS merger
- NS-NS merger

2) Host redshifts w/o afterglow association

source.

and a precursor picture.

Interpretation Challenge

“We saw three binary mergers...now what?”

Preparing to interpret measurements (detections *and* upper limits)
sometimes many are needed

Statistics of detection:

- If we detect several binary mergers we need to know how likely we are to see this many:
 - How many binary stars are in range?
[Galaxy catalogs, normalization]
 - What formation channels could produce mergers this often?
 - What channels could produce these *specific* mergers?

better than 30%??

...most of this talk

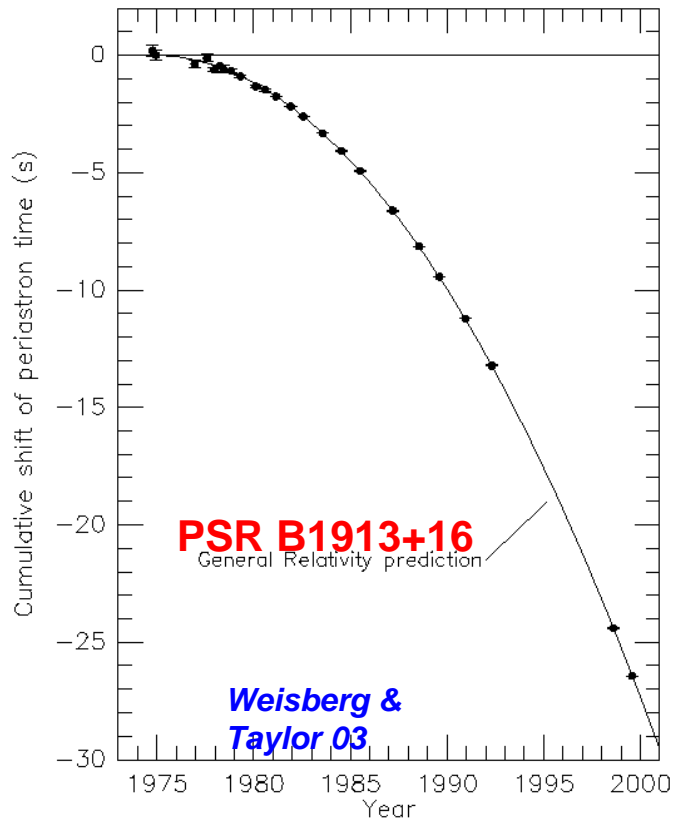
Outline

- Gravitational Wave Searches for Binaries
- How to Make Compact Binaries
 - Evolution of gas to merger
 - Observable phases
 - Population synthesis and *StarTrack*
- Predictions and Constraints: Milky Way
- Why Ellipticals Matter
- Predictions and Constraints Revisited
- GRBs
- Conclusions

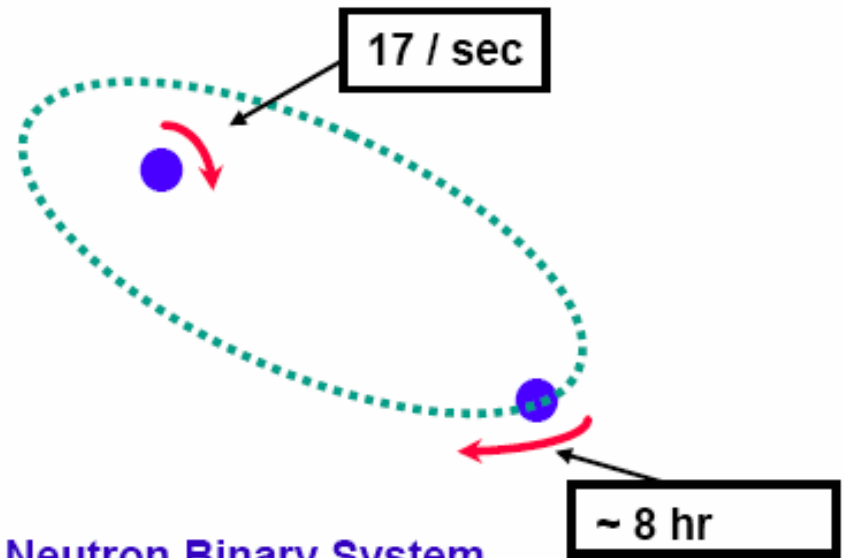
Observed pulsar binaries

- Hulse-Taylor binary:

(Nobel Prize, 1993)



PSR 1913 + 16 -- Timing of pulsars



Neutron Binary System

- separated by 10^6 miles
- $m_1 = 1.44m_\odot$; $m_2 = 1.39m_\odot$; $\varepsilon = 0.617$

Prediction from general relativity

- spiral in by 3 mm/orbit
- rate of change orbital period

Binary stellar evolution

Complex process

- Outline of (typical) evolution:
 - Evolve and **expand**
 - Mass transfer (perhaps)
 - Supernovae #1
 - Mass transfer (perhaps)
 - Supernovae #2

Note

- Massive stars evolve faster
- Most massive stars supernova, form BHs/NSs
- Mass transfer changes evolutionary path of star

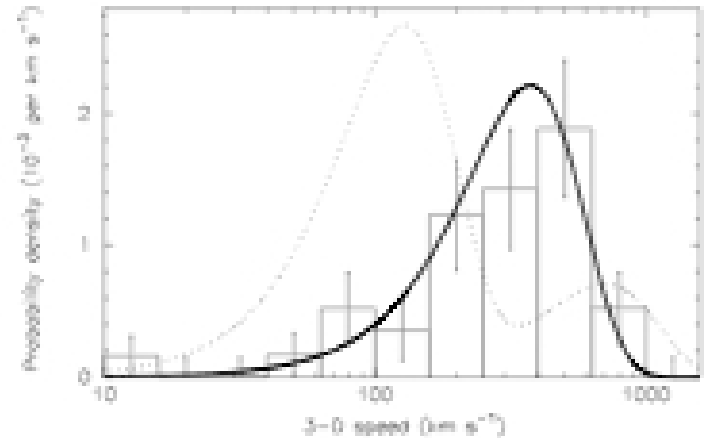
QuickTime™ and a
YUV420 codec decompressor
are needed to see this picture.

Movie: [John Rowe](#)

Binary stellar evolution

Parameterized (phenomenological) model

- Example: Supernovae kicks
 - Neutron stars = supernovae remnants
 - Observed moving **rapidly** :
 - Supernovae asymmetry --> kick
 - Model:
 - “Two-temperature thermal” distribution



Hobbs et al

- Many parameters (like this)
change results by **x10**

Observations suggest preferred values
conservatively: explore plausible range

StarTrack and Population Synthesis

Population synthesis:

- Evolve *representative sample*
- See what happens

Variety of results

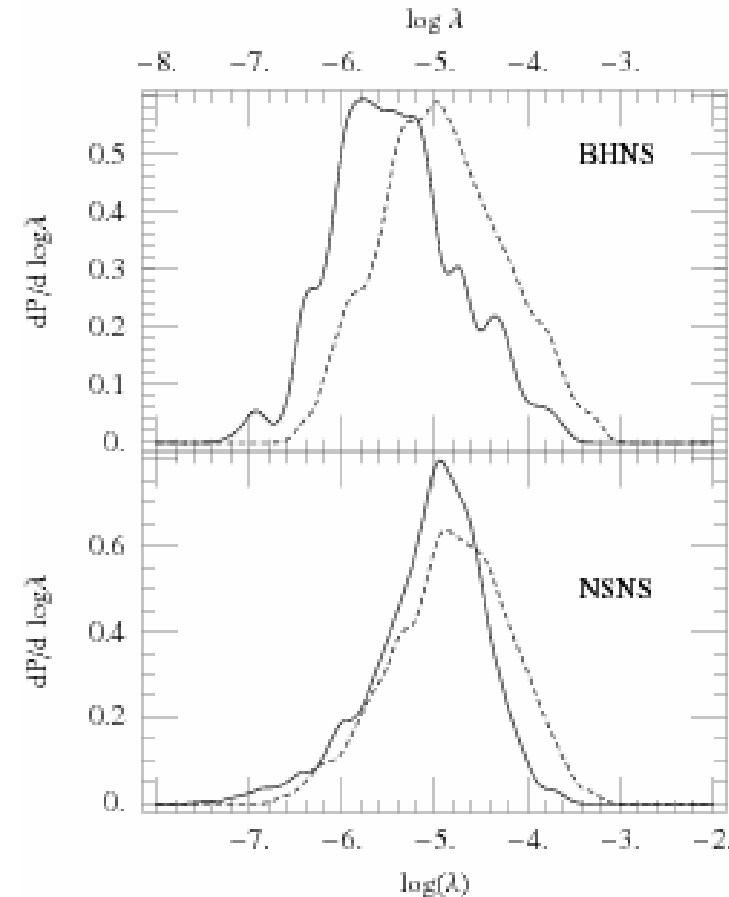
Depending on parameters used...

- Range of *number of binaries per input mass*

Plot: Distribution of mass efficiencies seen in simulations

Priors matter

a priori assumptions
about what parameters likely
influence *expectations*



More binaries/mass

O'Shaughnessy et al (in prep)

StarTrack and Population Synthesis

Population synthesis:

- Evolve *representative sample*
- See what happens

Variety of results

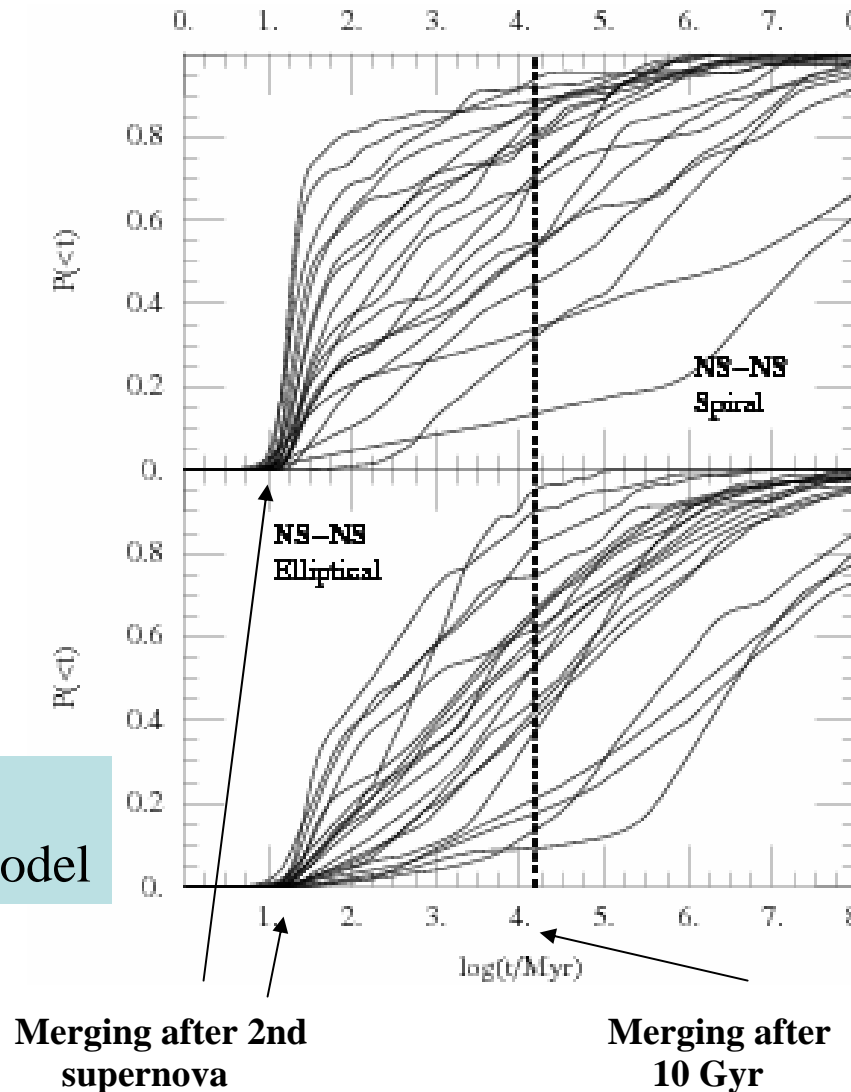
Depending on parameters used...

- Range of *number of binaries per input mass*
- Range of *delays between birth and merger*

Plot: Probability that a random binary merges before time 't', for each model

Priors matter

a priori assumptions
about what parameters likely
influence *expectations*



O'Shaughnessy et al (in prep)

: changed priors since last paper

Outline

- Gravitational Wave Searches for Binaries
- How to Make Compact Binaries
- Predictions and Constraints: Milky Way
 - Observations (pulsars in binaries) and selection effects
 - Prior predictions versus observations
 - Constrained parameters
 - Physics behind comparisons : what we learn
 - Revised rate predictions
 - What if a detection?
- Why Ellipticals Matter
- Predictions and Constraints Revisited
- GRBs
- Impact of detection(s)?
- Conclusions

Observations of Binary Pulsars

Observations

- 7 NS-NS binaries
- 4 WD-NS binaries

Kim et al ApJ 584 985 (2003)
Kim et al astro-ph/0608280
Kim et al ASPC 328 261 (2005)
Kim et al ApJ 614 137 (2004)

Rate estimate Kim et al ApJ 584 985 (2003)
(*steady-state approximation*)

Number + ‘lifetime visible’ + lifetime
+ fraction missed

=> **birthrate**

+ error estimate (number-> sampling error)

Note:

- **Only possible** because many single pulsars seen:
Lots of knowledge gained on selection effects
Applied to *reconstruct* N_{true} from N_{seen}

Predictions and Observations

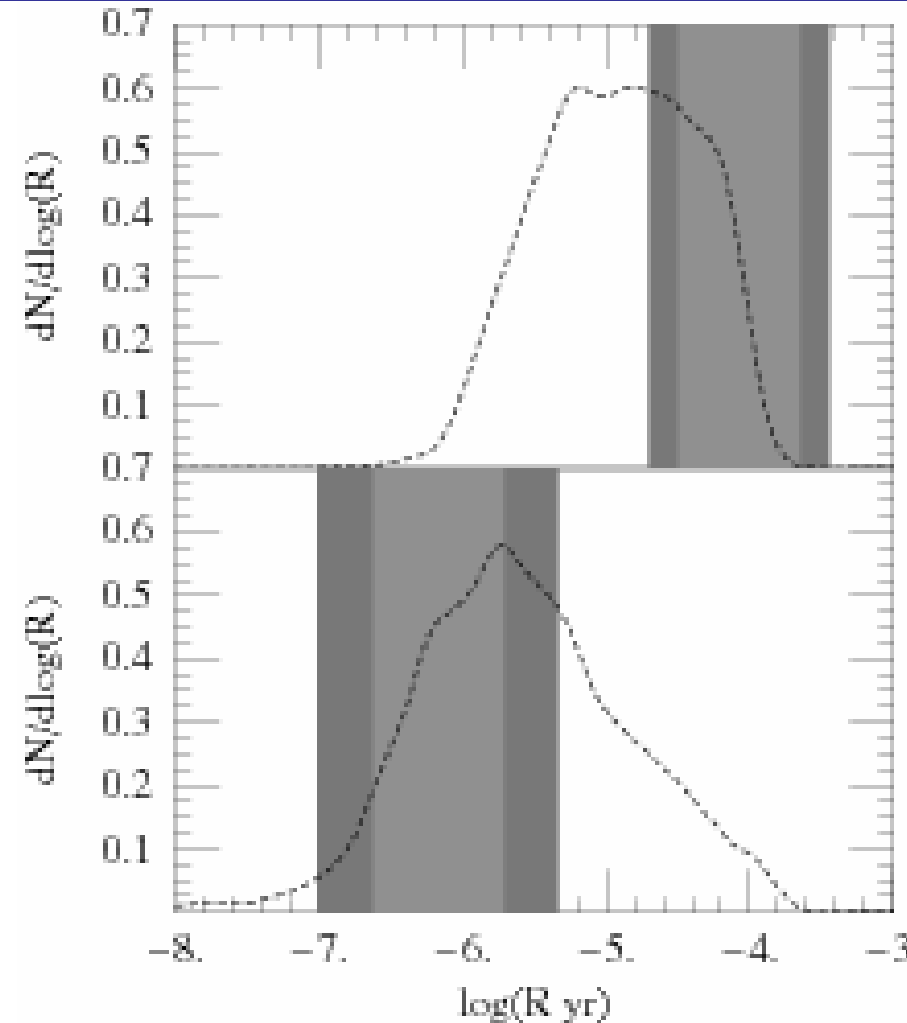
Formation rate distributions

- Observation: shaded
- Theory: dotted curve
- Systematics : dark shaded

Allowed models?

- Not all parameters reproduce observations of
 - NS-NS binaries
 - NS-WD binaries (massive WD)

--> **potential constraint**

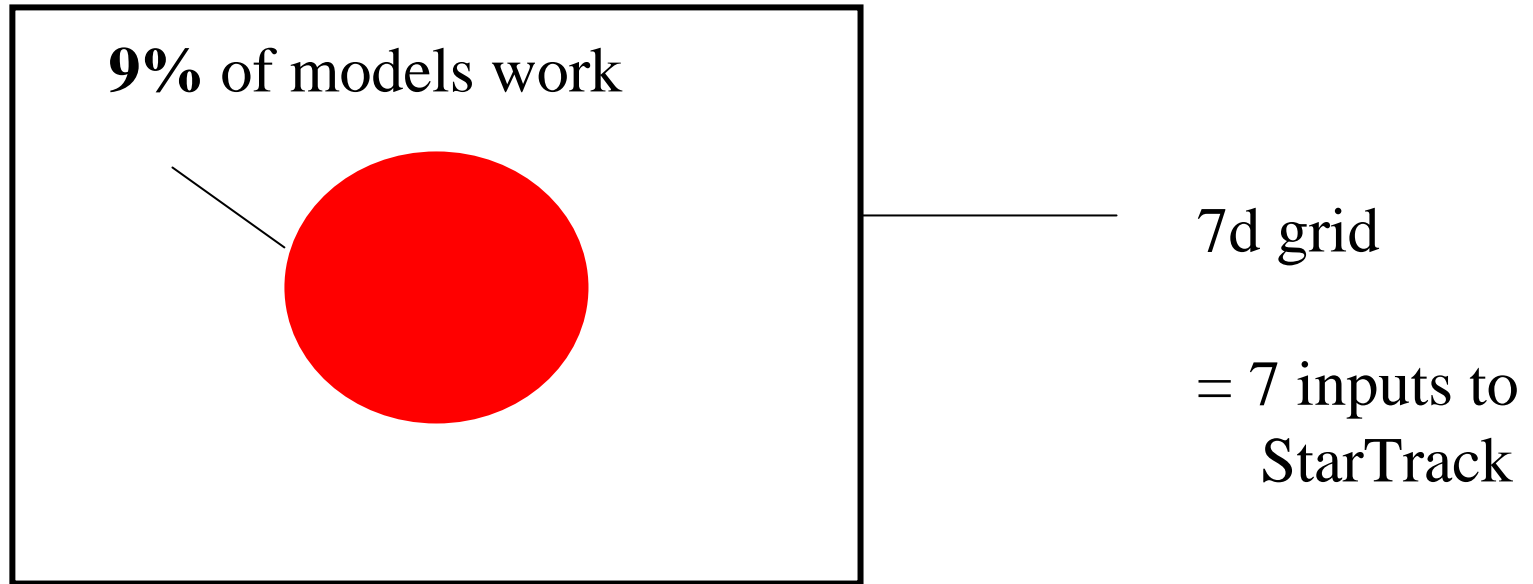


Plot

Merging (top), wide (bottom)
NS-NS binaries

Accepted models

Constraint-satisfying volume



7d volume:

- Hard to visualize!
- Extends over 'large' range:

characteristic extent(each parameter):
 $0.09^{1/7} \sim \mathbf{0.71}$

Accepted models

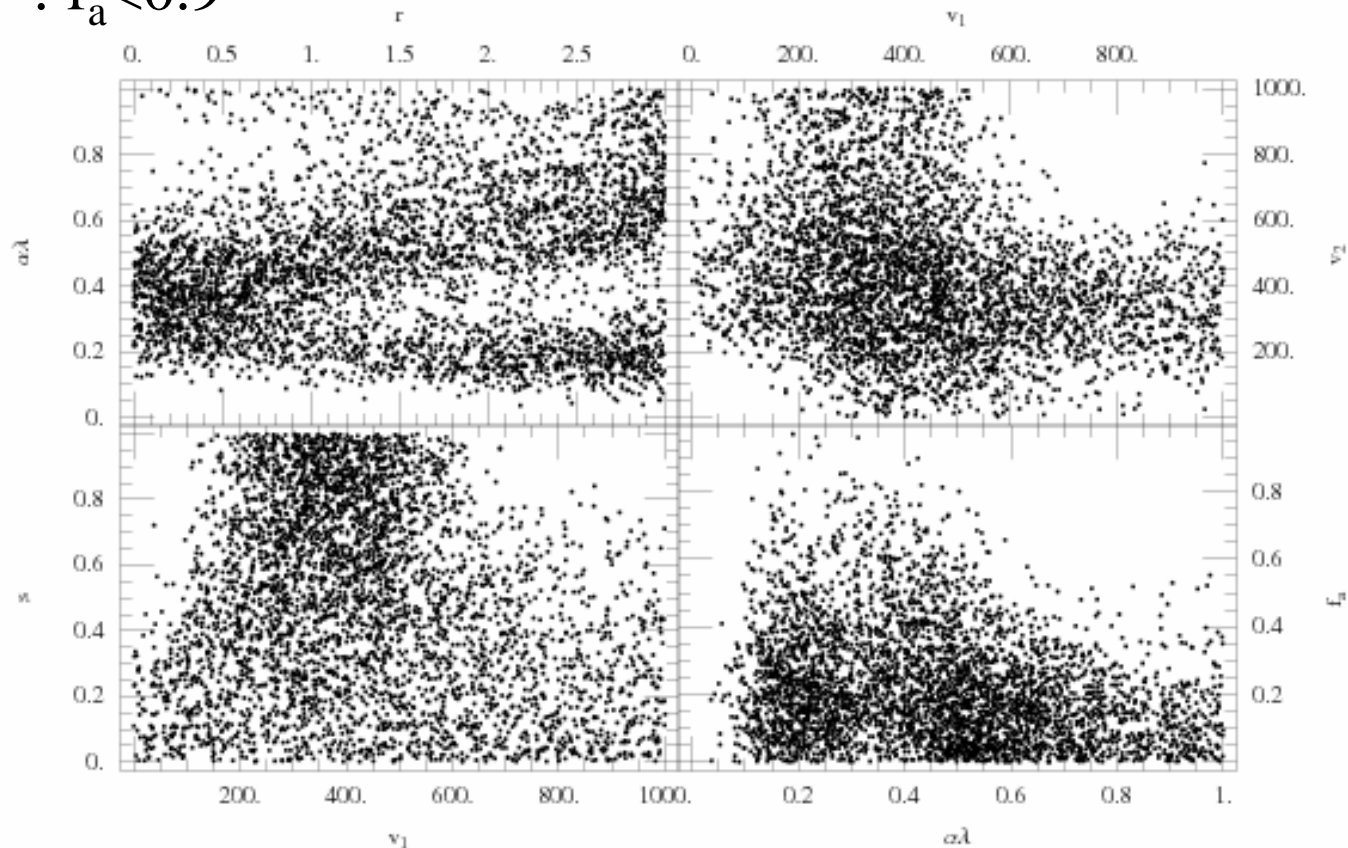
Parameter distributions

- Not all parameter combinations allowed

Examples:

- Kick strength: $v_1, v_2 \sim 300$ km/s
- CE efficiency: $\alpha\lambda > 0.1$
- Mass loss : $f_a < 0.9$

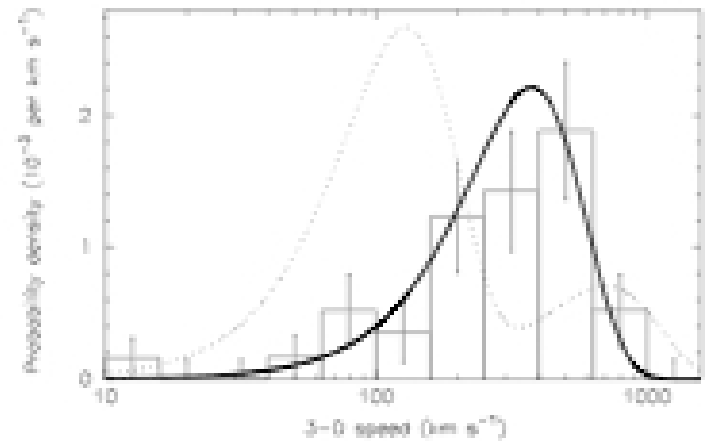
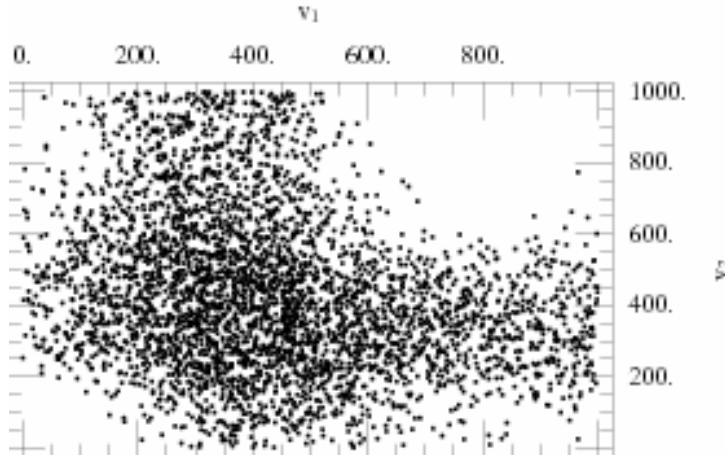
**Lots of physics
in
correlations**



Physics of comparison

Physics implied by constraints

- Kick strength: $v_1, v_2 \sim 300$ km/s
Pulsar motions \sim measure supernova kicks [e.g., Hobbs 2006]



Preferred kicks \sim **consistent with observations**
(*without* imposing that as a constraint)

Physics of comparison

Physics implied by constraints

- CE efficiency: $\alpha\lambda > 0.1$

CE efficiency = fraction of orbit energy needed to eject envelope surrounding two cores

Low $\alpha\lambda$:

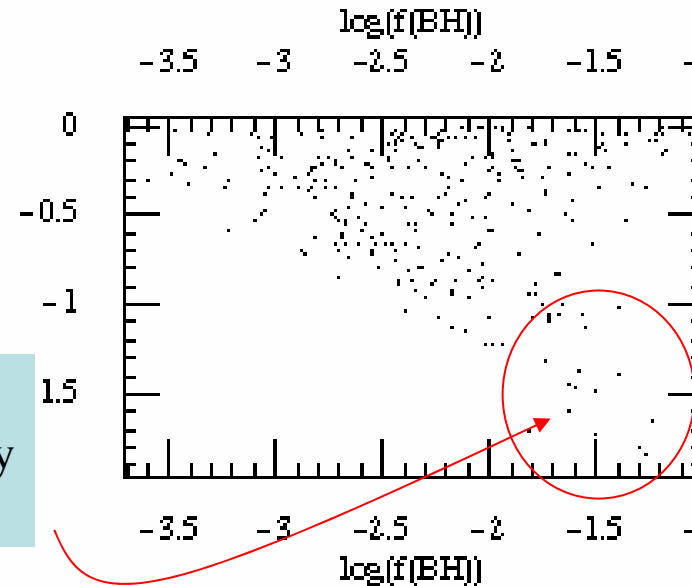
- closer final orbit needed to eject envelope
- some binaries merge in CE phase!
 - NS-NS rate down
 - BH-NS rate up (often)
 - BH-BH rate up

brings together distant holes



$\log(\alpha)$

Plot: BH-BH merger rate versus $\alpha\lambda$; low $\alpha\lambda$ imply high rate



Excluding low:

- High NS-NS rate needed to match observations
Low $\alpha\lambda$ can't make it
- Posterior rate prediction:
lower BH-BH rate

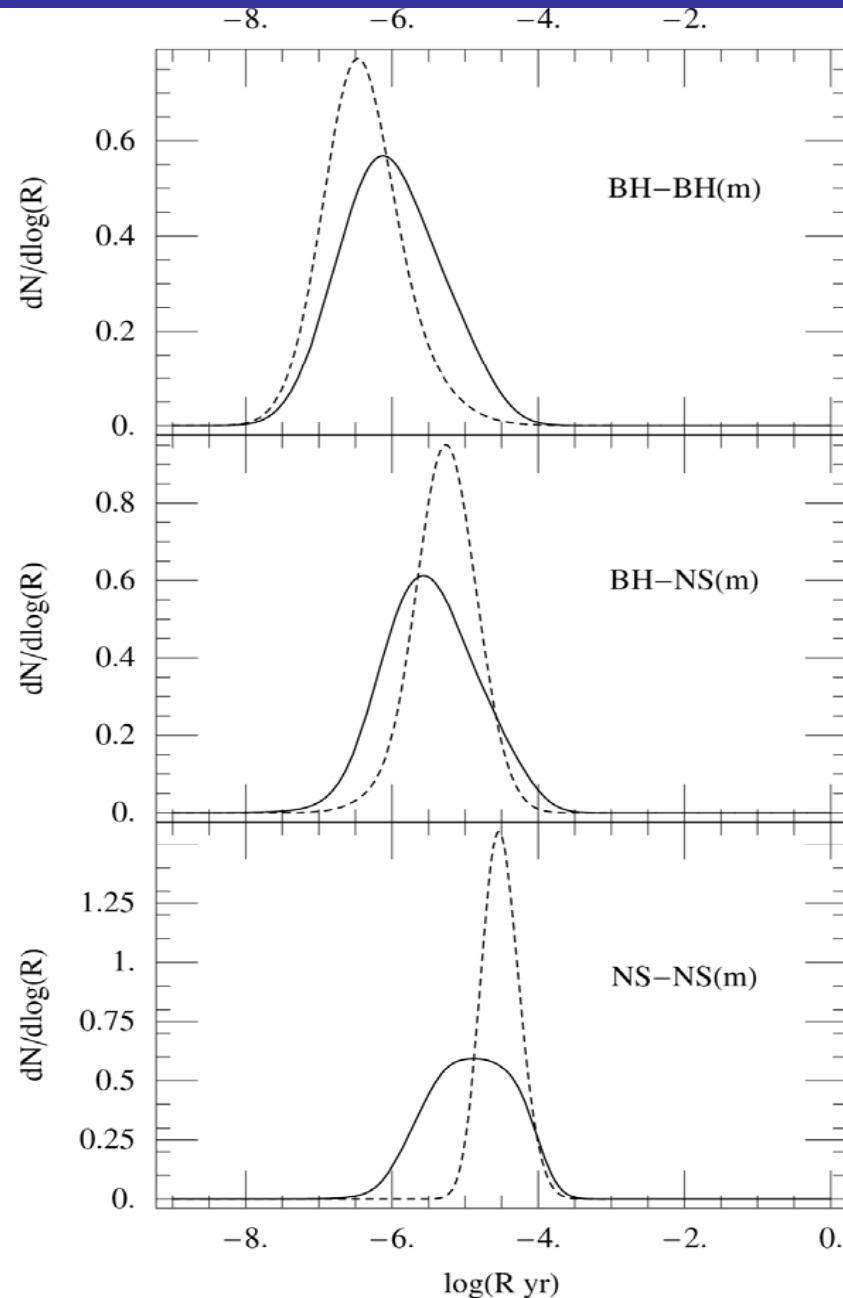
Revised rate predictions

Rate predictions change...

- Solid: Prior
- Dashed: After constraint

Warning: Priors matter

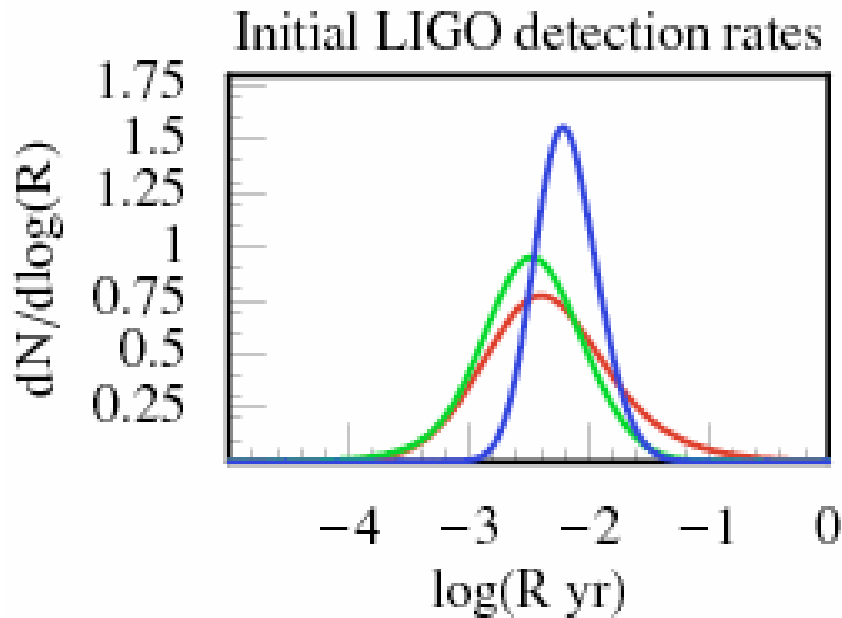
- Exact mean, probabilities depend on priors/assumptions
(= range of parameters allowed)
- *Trend* of change (before vs after) rather than specifics
 - **Fewer BH-BH**
 - **More NS-NS** (of course)



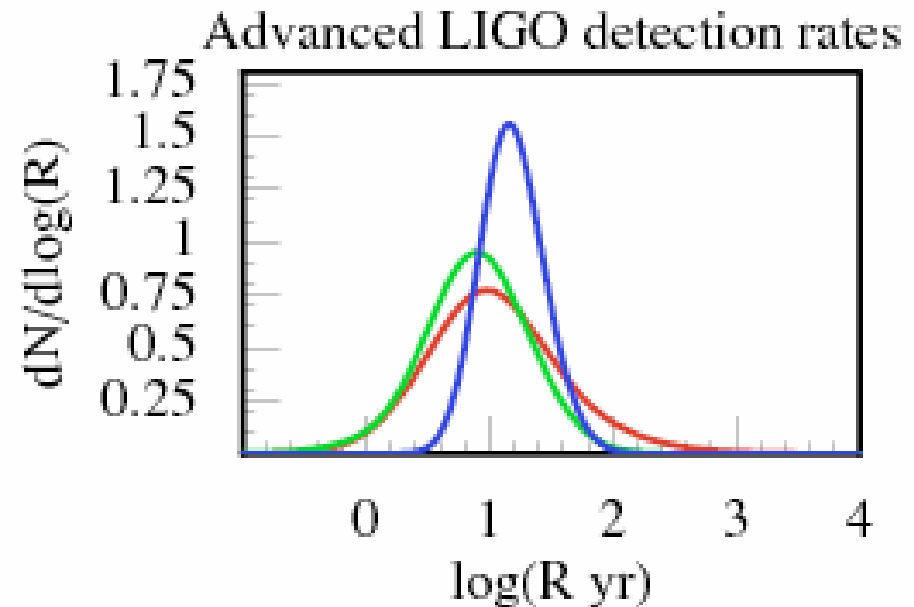
LIGO detection rates

Constrained LIGO detection rates

Assume all galaxies like Milky Way, density 0.01 Mpc^{-3}



Detection unlikely



Detection assured

Key

NS-NS

BH-NS

BH-BH

Detection: A scenario for 2014

Scenario: (Advanced LIGO)

- Observe $n \sim 30$ BH-NS events [reasonable]

Potential

- Stringent test of binary evolution model already!
- Stronger if
 - Orbit distribution consistency
 - More constraints

Independent channels (each depends differently on model params) →

Volume	$[0.09 (0.08)^3] \sim (4 \times 10^{-5})$!!
Params	$[0.09 (0.08)^3]^{1/7} \sim 0.24$

Outline

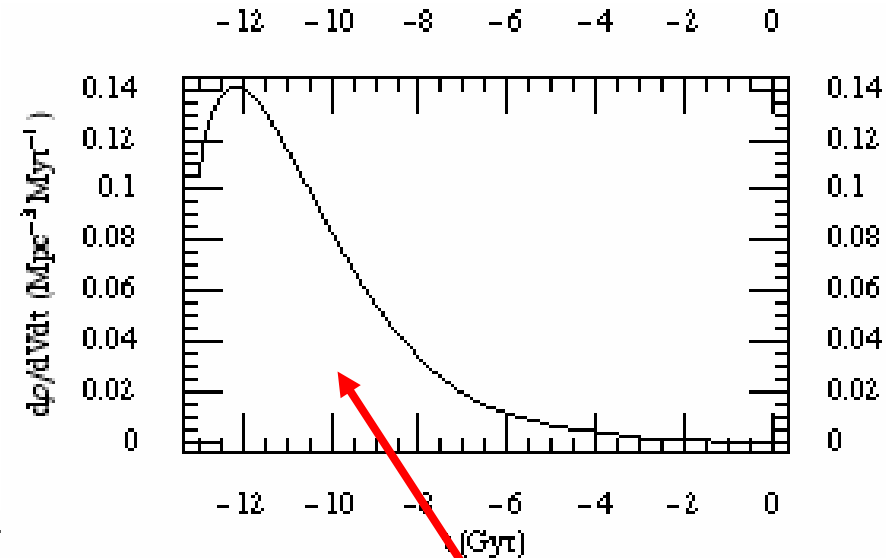
- Gravitational Wave Searches for Binaries
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Importance of early SFR

Long delays allow mergers in ellipticals now

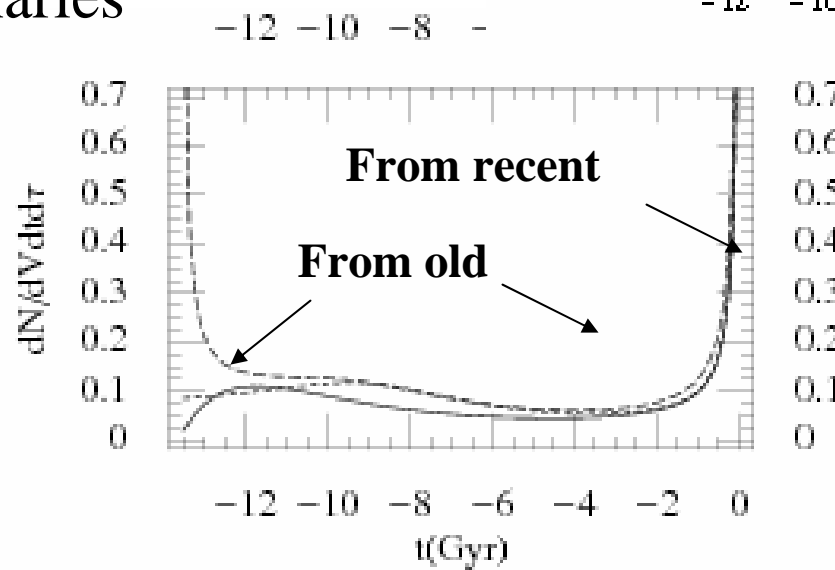
- Merger rate from starburst: $R \sim dN/dt \sim 1/t$
- SFR higher in past:

- Result:
 - Many mergers *now* occur in ancient binaries



Nagamine et al [astro-ph/0603257](https://arxiv.org/abs/astro-ph/0603257)

ancient SFR
= **ellipticals**
(mergers, ...)



Plot:

Birth time for present-day mergers

Two-component SFR

SFR

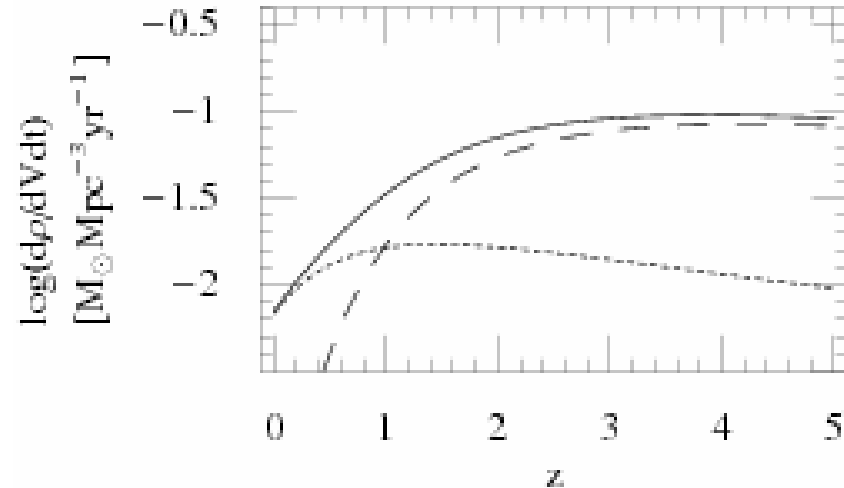
[Nagamine et al 2006]

- Separate elliptical, spiral!

Reliable?

- Normalization ok
- Spiral/elliptical ratio ok
- Time dependence reasonable

...uncertainty **smaller than popsyn**



Nagamine et al [astro-ph/0603257](https://arxiv.org/abs/astro-ph/0603257)

Predictions and constraints

Two-component predictions:

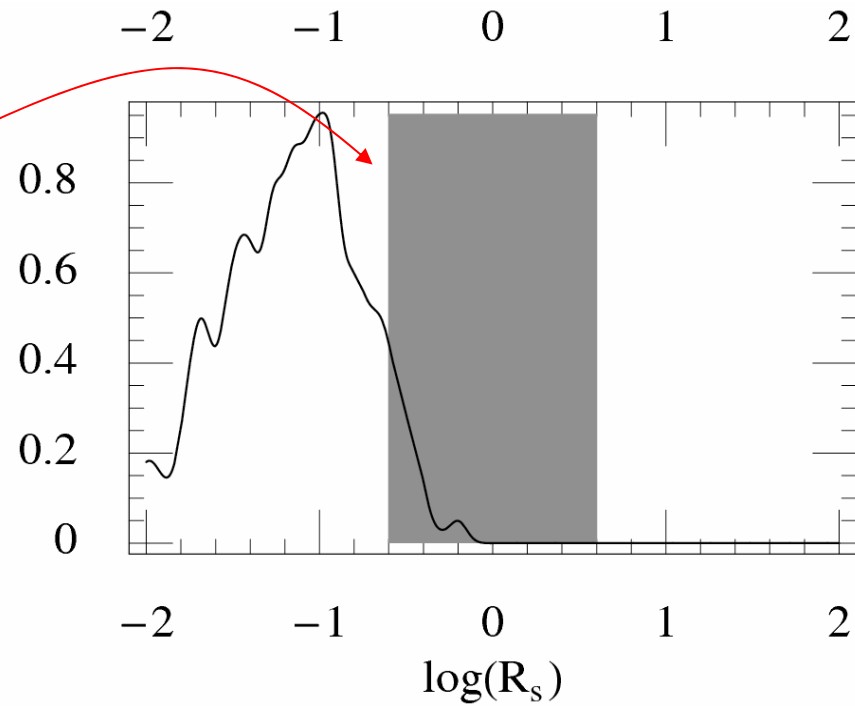
- Each prediction =
Rate density (/vol/time) versus time
for **each** of ellipticals, spirals
...mostly **unobservable** (except now in Milky Way)

Example: NS-NS merger rate in spirals

- Rate extrapolated from
Milky way:

$$R_s = 0.25 - 4 \text{ Myr}^{-1} \text{Mpc}^{-3}$$

- consistent parameters
unfinished / pending
- revised merger & LIGO rates
discuss in context of short GRBs



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- Gravitational Wave Searches for Binaries
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- Predictions and Constraints Revisited
- GRBs
 - Review + the short GRB merger model
 - Short GRB observations, the long-delay mystery, and selection effects
 - Detection rates versus L_{\min}
 - Predictions versus observations:
 - If short GRB = BH-NS
 - If short GRB = NS-NS
 - Gravitational waves?
- Conclusions

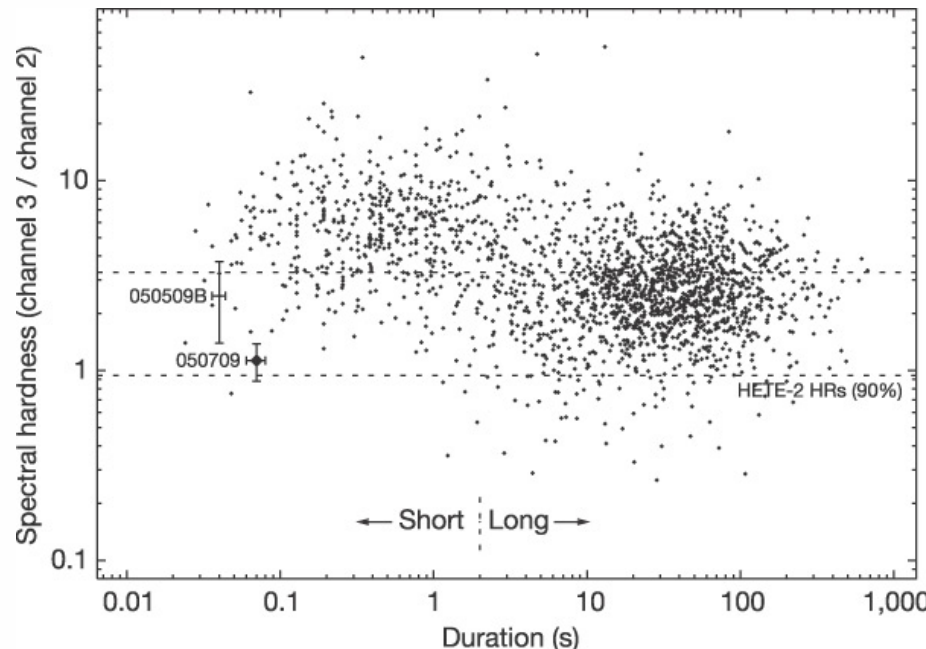
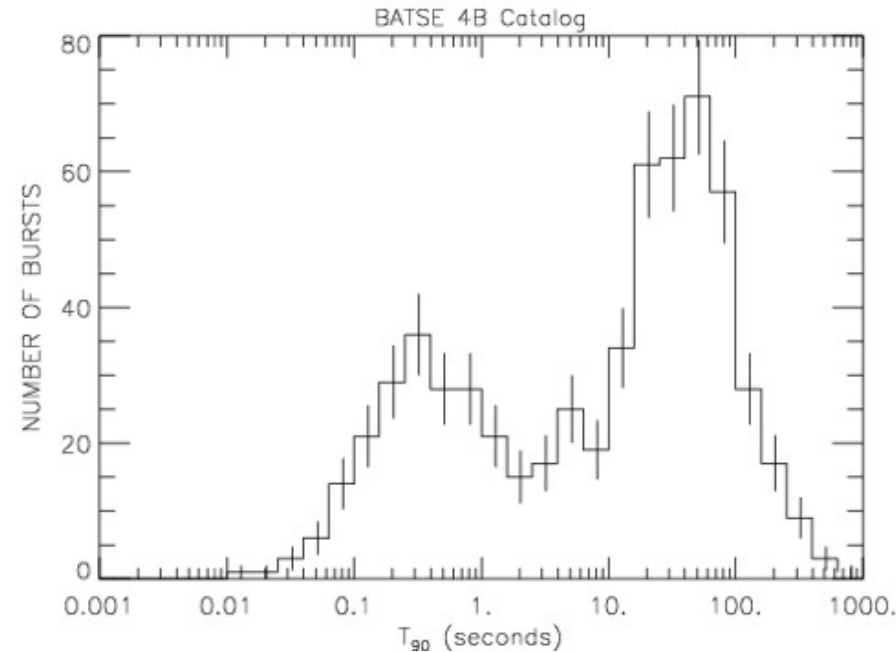
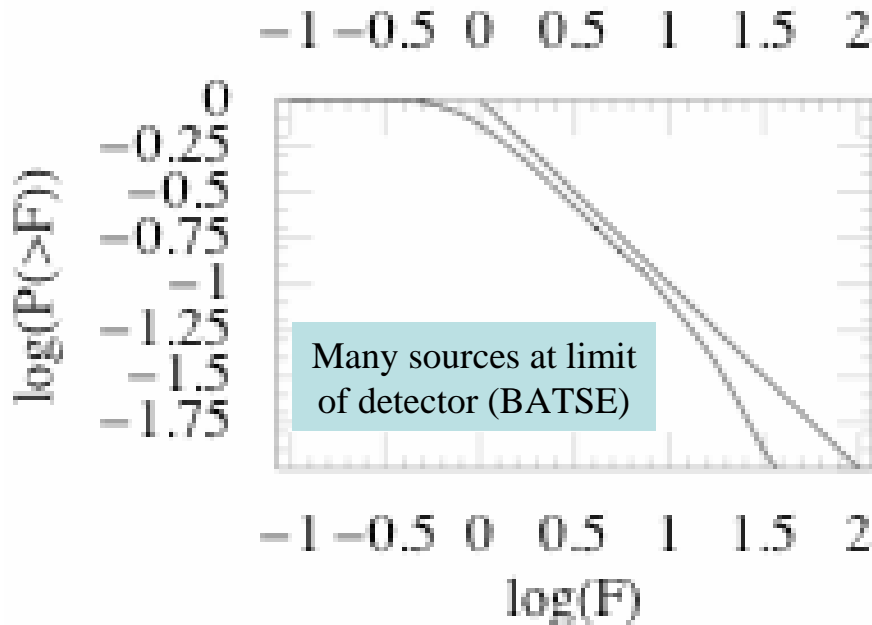
Short GRBs: A Review

Short GRBs (BATSE view)

- Cosmological
- One of two classes
- Hard: often peaks out of band
- Flux power law

$$dP/dL \sim L^{-2}$$

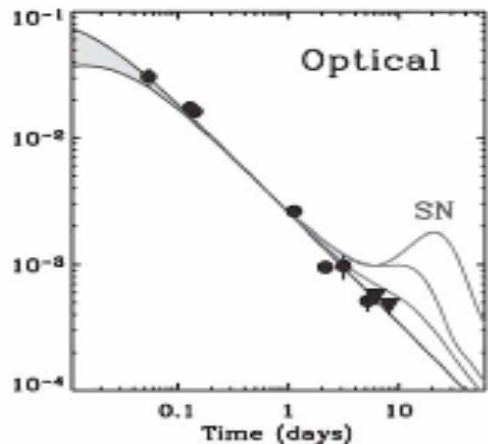
--> **most** (probably) **unseen**



Short GRBs: A Review

Merger motivation?

- No SN structure in afterglow



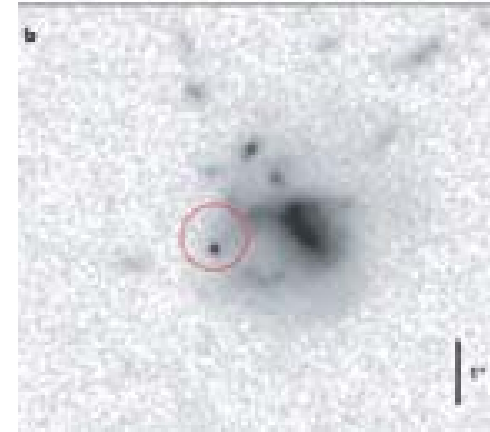
GRB 051221 (Soderberg et al 2006)

- In both **old**, young galaxies

Selected short GRBs			
GRB	Host	L/L_*	SFR M_{\odot}/yr
050509b	E	3	< 0.1
050709b	Sb/Sc	0.1	0.2
050724	E	1.5	< 0.03
051221	S	0.3	1.4
060502	E	1.6	0.6

(Nakar, 2006 : Table 3)

- Occasional host **offsets**



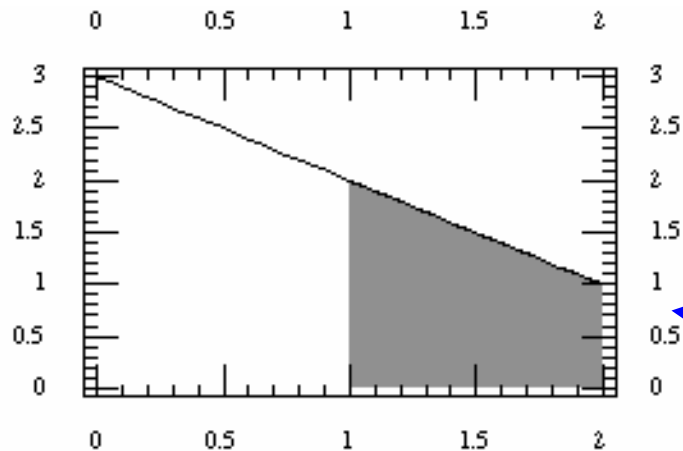
GRB 050709 (Fox et al Nature 437 845)

- Energetics prohibit magnetar

Observables: Detection rate?

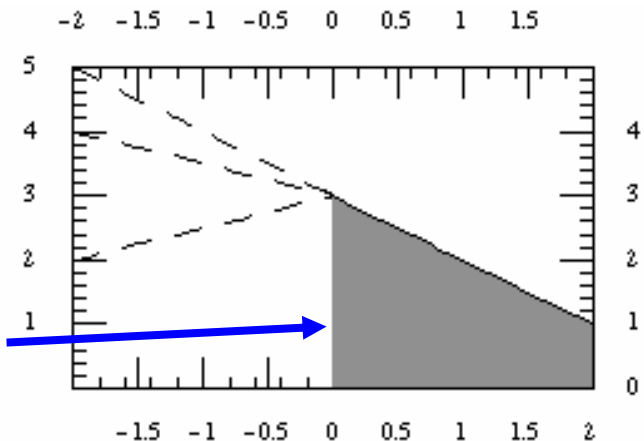
Binary pulsars

- Many (isolated) observed
- **Minimum luminosity** ~ known
- Observed number
--> **rate** (+ 'small' error)



Short GRBs

- Few observations
- **Minimum luminosity** ~ **unknown**
- Observed number
--> **rate upper bound**



Plots:
Cartoon on L_{\min}

observed

Conclusion:

The number (rate) of short GRB observations is a weak constraint on models

Observables: Redshift distribution

Redshift distribution desirable

- Low bias from luminosity distribution
- Well-defined statistical comparisons
Kolmogorov-Smirnov test (=use maximum difference)

Observed redshift sample

- Need sample with *consistent selection effects*
(=bursts from 2005-2006, with Swift)

Problem: Possible/likely bias towards low redshifts

Merger predictions \leftrightarrow short GRBs?

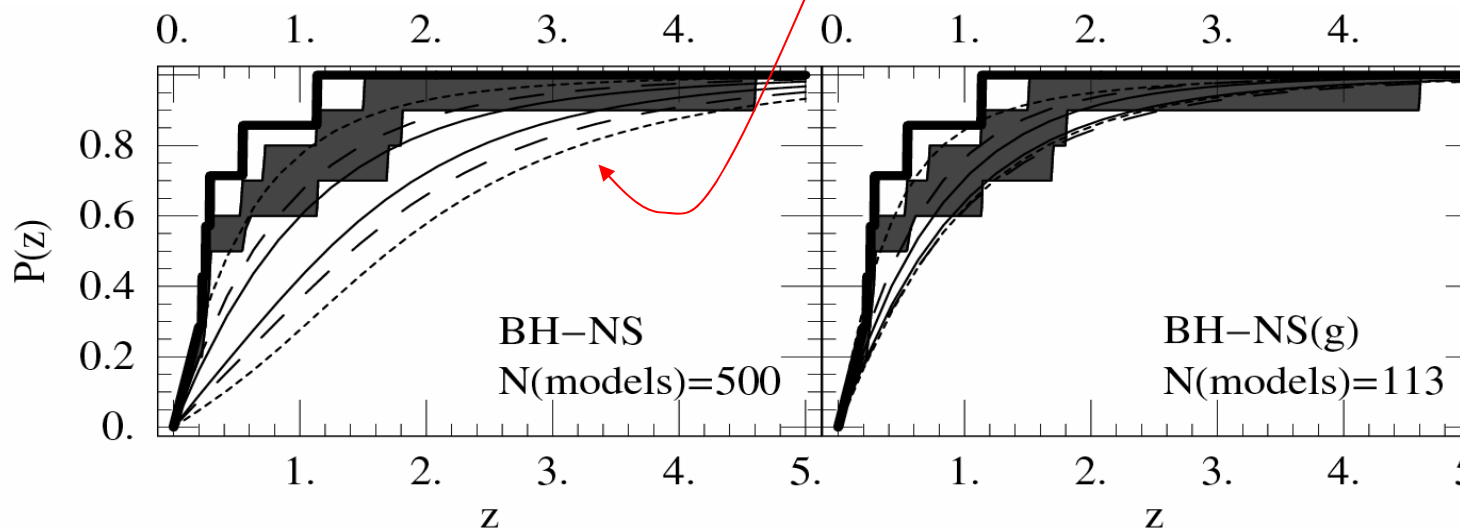
BH-NS?

- Predictions:
 - 500 pairs of simulations
 - Range of redshift distributions

- Observations:

- Solid: certain
- Shaded: possible

Key
Solid: 25-75%
Dashed: 10-90%
Dotted: 1%-99%

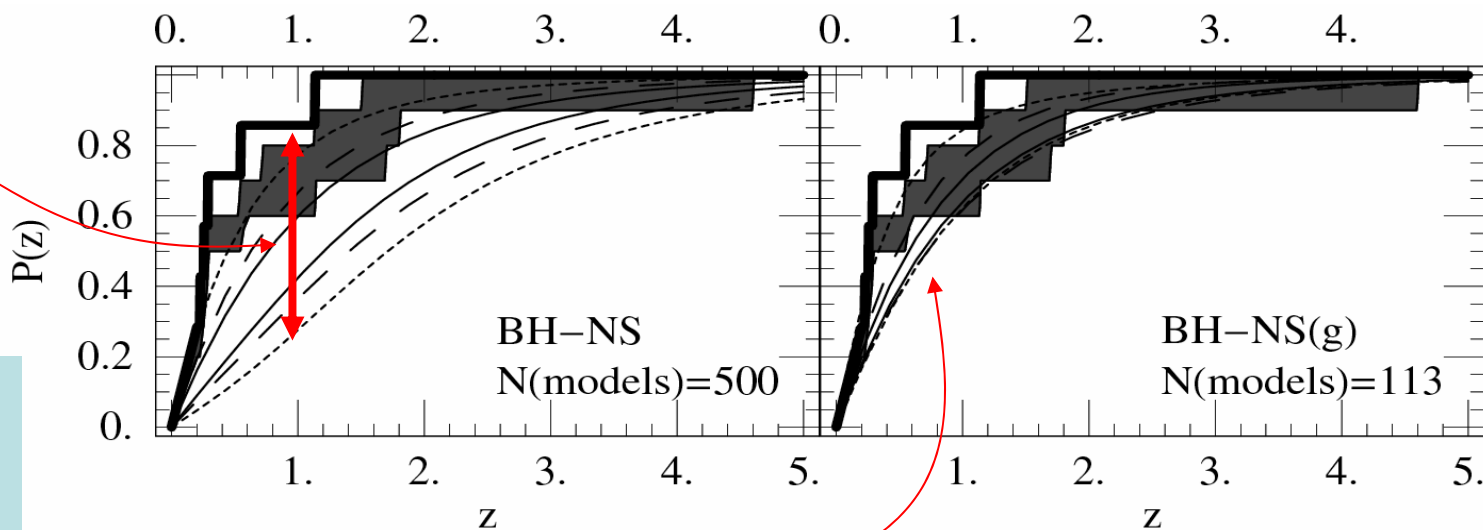


O'Shaughnessy et al (in prep)

Merger predictions \leftrightarrow short GRBs?

BH-NS?

- Predictions that agree?
 - Compare *cumulative distributions*:
 - maximum difference < 0.48 everywhere [95% Komogorov-Smirnov given GRBs]
 - Compare to **well-known** GRB redshifts since 2005 [consistent selection effects]
 - dominated by low redshift



Result:
Distributions
which agree
= mostly
at *low* redshift

O'Shaughnessy et al (in prep)

Merger predictions \leftrightarrow short GRBs?

BH-NS?:

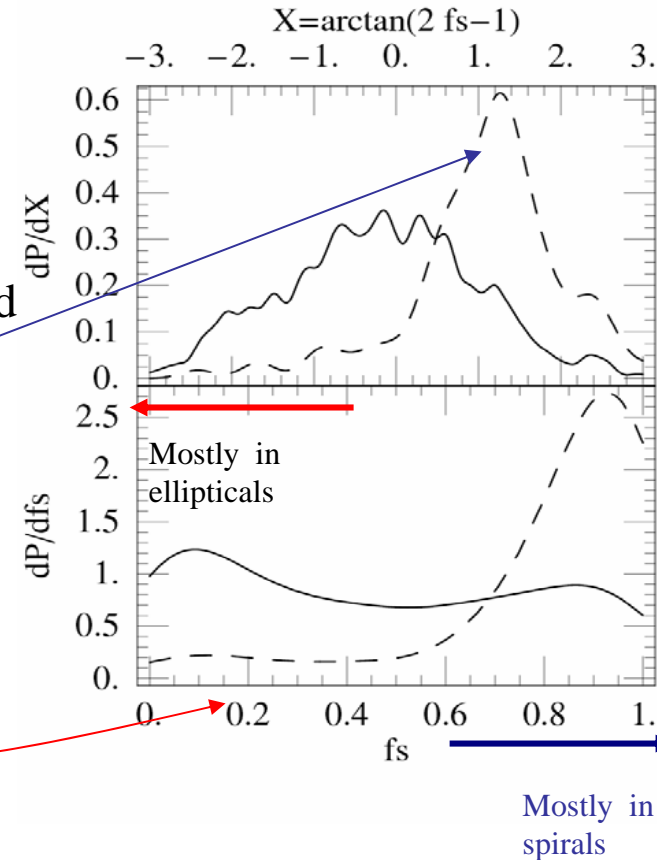
- Physical interpretation

- Observations : Dominated by **recent** events

- Expect:

- Most mergers occur in spirals (=recent SFR) and High rate (per unit mass) forming in spirals
- **or** Most mergers occur in ellipticals (=old SFR) and High rate (per unit mass) forming in elliptical and **Extremely** prolonged delay between formation and merger (**RARE**)

Plot: f_s : fraction of mergers in spirals ($z=0$)



- **Consistent...but...**

Short GRBs appear in ellipticals!

BH-NS hard to reconcile with GRBs??

O'Shaughnessy et al (in prep)

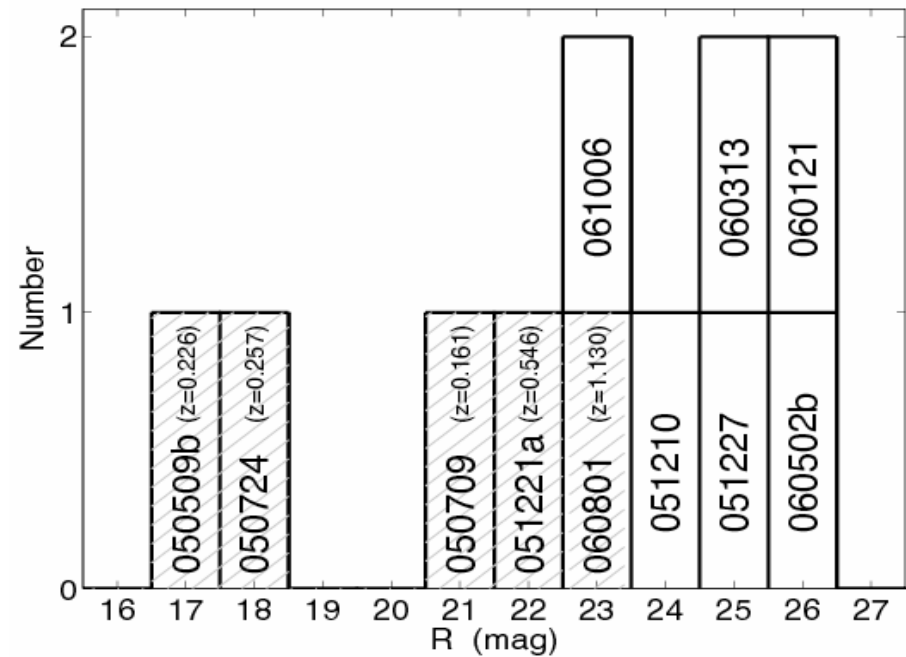
Merger predictions \leftrightarrow short GRBs?

BH-NS?:

- Conclusion = confusion
 - Theory + redshifts : Bias towards recent times, **spiral** galaxies
 - Hosts: Bias towards **elliptical** galaxies
- What if observations are *biased* to low redshift?
 - strong indications from deep afterglow searches [Berger et al, [astro-ph/0611128](https://arxiv.org/abs/astro-ph/0611128)]

- Makes fitting **easier**
Elliptical-dominant solutions
ok then (=agree w/ hosts)

Point: Too early to say
waiting for data;
more analysis needed



Merger predictions \leftrightarrow short GRBs?

NS-NS?:

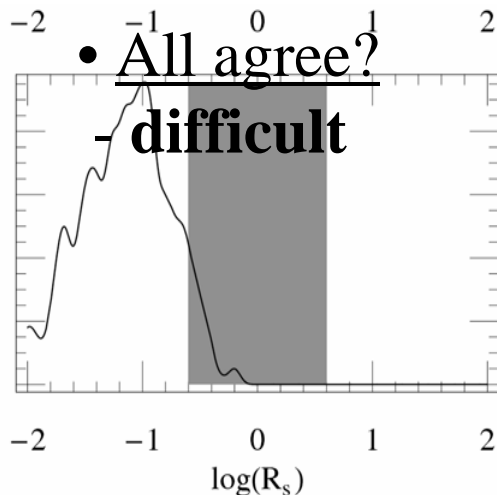
- Predictions & observations

- Matching redshifts

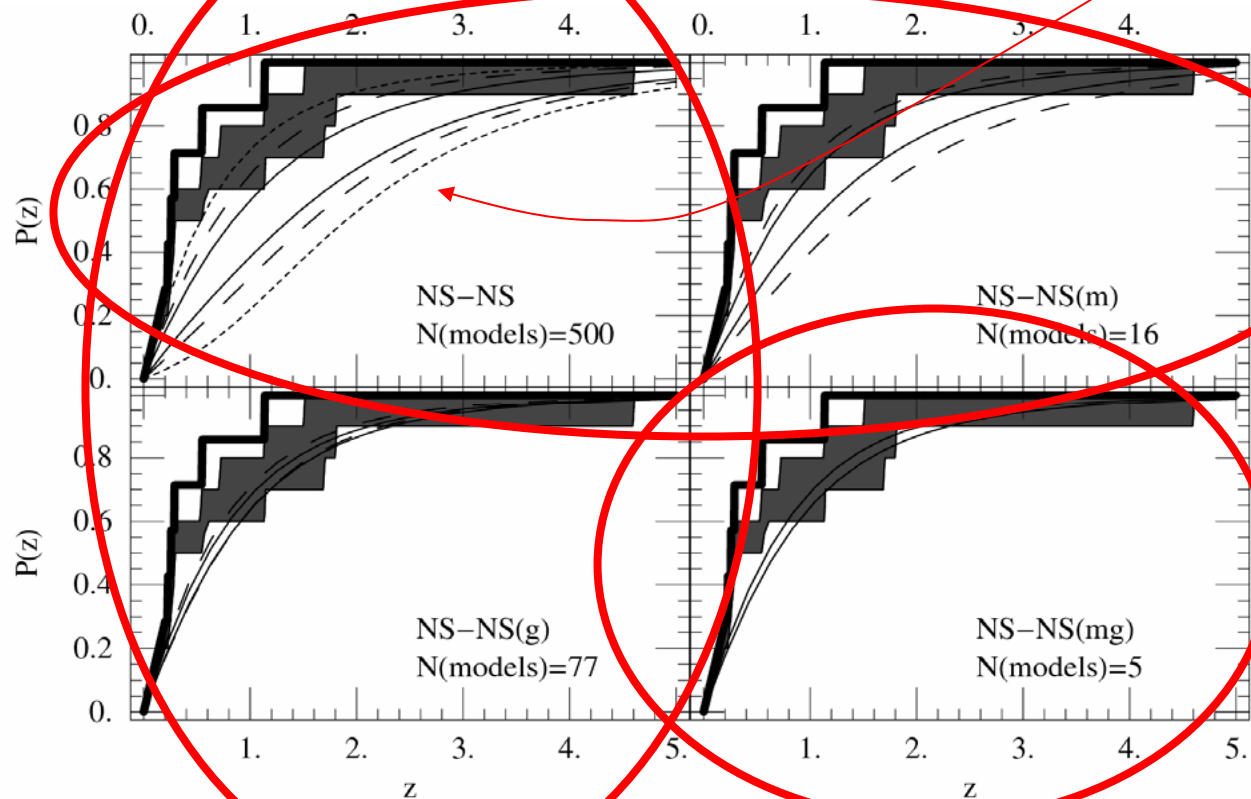
- Observed NS-NS
(Milky Way)

- All agree?

- **difficult**



Key
Solid: 25-75%
Dashed: 10-90%
Dotted: 1%-99%



O'Shaughnessy et al (in prep)

Merger predictions \leftrightarrow short GRBs?

NS-NS?:

- Physical interpretation

- Observations : GRBs
 - Dominated by **recent** events

- Expect:

- Recent spirals dominate or
- **or** Ellipticals dominate, with long delays

Plot: f_s : fraction of mergers in spirals ($z=0$)

- **Consistent...but...**

Short GRBs appear in ellipticals!

NS-NS hard to reconcile with GRBs

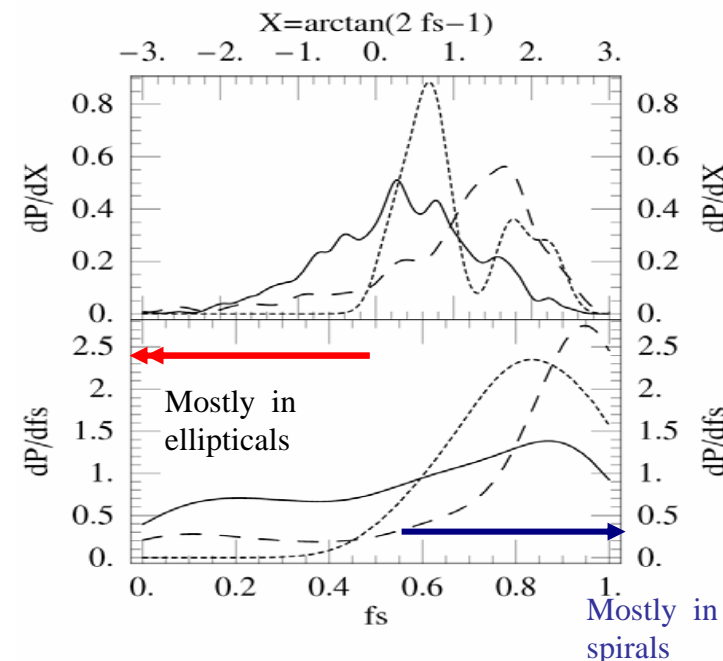
and problem *worse* if redshifts are biased low!

-Observations: Galactic NS-NS

- High merger rate

-Expect

-High merger rate in spirals



Conclusions

Present:

- Useful comparison method **despite** large uncertainties
- Preliminary results

- Via comparing to pulsar binaries in Milky Way
 - Low mass transfer efficiencies forbidden
 - Supernovae kicks \sim pulsar proper motions
 - BH-NS rate closely tied to min NS mass/CE
- Via comparing to short GRBs?

- Conventional popsyn **works** : weak constraints
- Expect GRBs in **either host** : spirals favored
 - Spirals now favored; may change with new models
- Short GRBs = NS-NS? **hard** : few candidates
- Short GRBs = BH-NS? **easier** : fewer candidates

- Observational recommendations

- Galactic :
 - Minimum pulsar luminosity & updated selection
 - Pulsar opening angles
 - Model : Size and SFR history

- Short GRBs :

- Ratio of spiral to elliptical hosts at $z \leq 0.5$

(Long term) Wishes

(critical)

- reliable GRB classification
- short burst selection bias?
- deep afterglow searches

(less critical)

- formation history
- formation properties
(Z , imf) [mean+statistics]
for **all** star-forming
structures

Conclusions

Future (model) directions:

- More comparisons

- Milky Way

- Pulsar masses
- Binary **parameters** (orbits!)
- Supernova kick consistency?

- Extragalactic

- Supernova rates

- Broader model space

- Polar kicks?

- Different maximum NS mass

- [**important**: BH-NS merger rate sensitive to it!]

- Different accretion physics

Goal:

- show predictions *robust* to physics changes
- if changes matter, understand why
(and devise tests to constrain physics)

Some examples:
Belczynski et al. (in prep)

