



# AdvLIGO

## Static Interferometer Simulation

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- AdvLIGO simulation tools
  - » Stationary, frequency domain and time domain
- Stationary Interferometer Simulation, SIS, basic
  - » Motivation
  - » physics
- SIS applications
  - » Stationary Michelson cavity
  - » Beam splitter Wedge angle effect
  - » Surface aberration



# Advanced LIGO Interferometer Simulation Tools

model	Description	Applications
Stationary Interferometer Simulation a.k.a. FFT	Stationary field simulation with detailed optics	<ul style="list-style-type: none"><li>◆ Effect of realistic optics<ul style="list-style-type: none"><li>» Finite size, surface aberration, thermal deformation</li></ul></li><li>◆ Effect of realistic fields<ul style="list-style-type: none"><li>» Diffraction, scattering, excitation by complex mirror motion</li></ul></li></ul>
Opticle	Frequency domain simulation with optical springs and quantum noises	<ul style="list-style-type: none"><li>◆ Control system design</li><li>◆ Trade study of optical system design</li><li>◆ Noise analysis with full control systems</li></ul>
End to End model	Time domain simulation of opto-mechanical system with realistic controls	<ul style="list-style-type: none"><li>◆ Lock acquisition design and test</li><li>◆ Study of transient and stability issues</li><li>◆ Analysis of subsystems with strong correlations</li></ul>



# SIS Basic Motivation

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- AdvLIGO design tool
- Interferometer configuration trade study
- Effect of finite size optics
  - » BS, flat, wedge angle, baffle, etc
- Tolerance of radius of curvature of COC mirrors
- Surface aberration
  - » Requirements of the surface quality to satisfy the limit of loss in arm, total of 75ppm
- Subsystem performance simulation
  - » TCS, ISC, COC, AOC, ...
- Parametric instability
  - » highly distorted field, hard to be expressed by simple functions

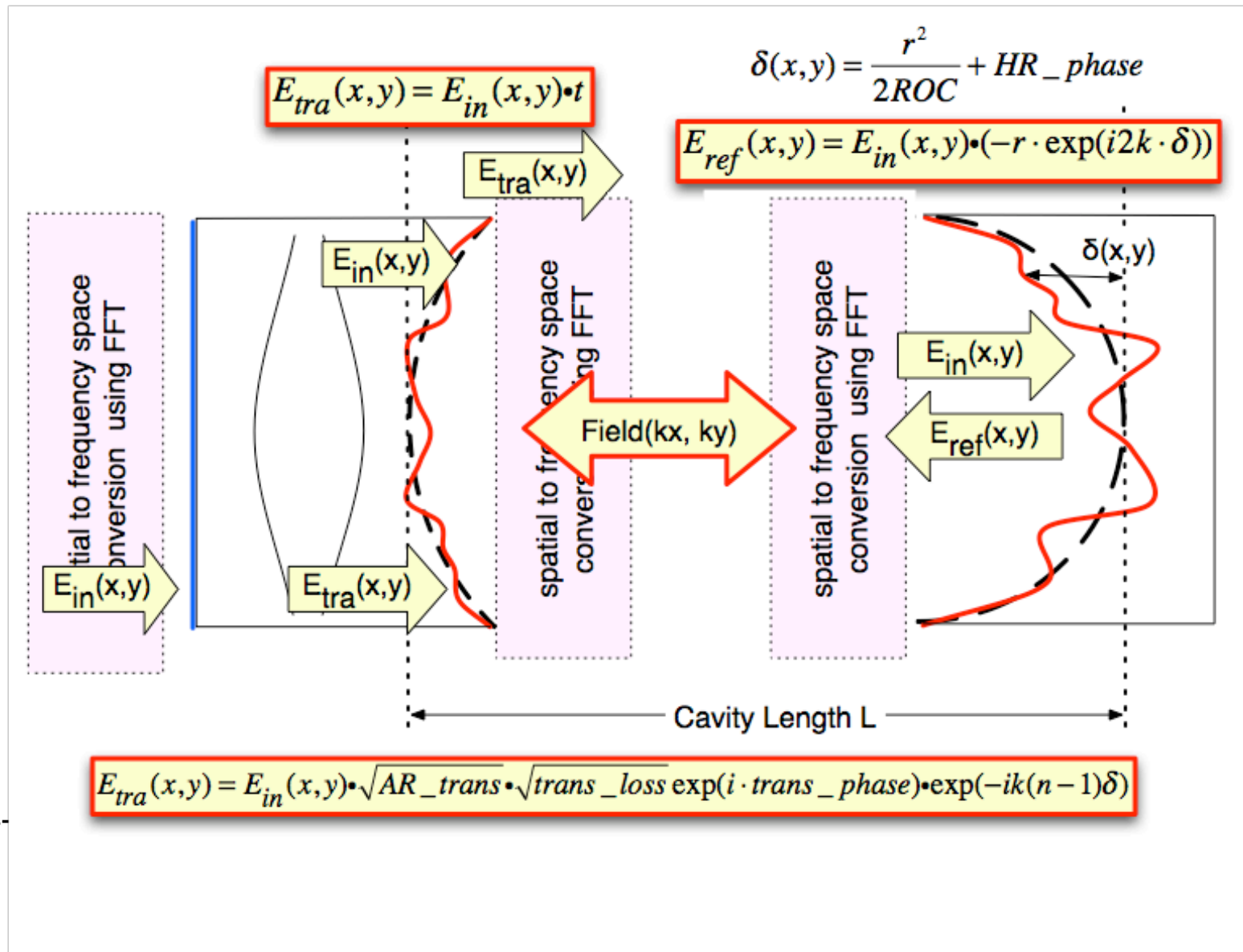


# SIS Basic Ingredient Requirements

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- Details of Optics
  - » surface map, size, flat, wedge angle, etc
- Flexibility
  - » Various optics configurations
  - » Now, only FP and couple cavity with BS
- Physics
  - » Realistic locking by using error signals
  - » Signal sideband generation
  - » Built-in thermal deformation function
- Analysis tool
  - » beam profiler
  - » mode analysis

# SIS Basic Optics and fields





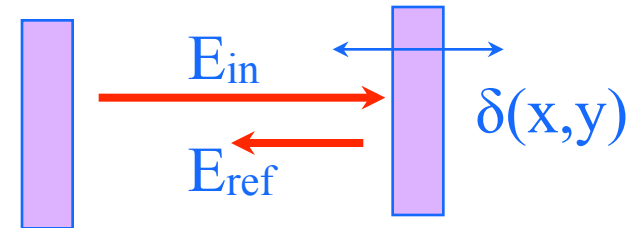
# SIS Basic Ingredients- 1

- Lock

$$\text{Error signal} = \text{imag}( CR * SB ) \sim \text{imag}( CR * \text{promptly reflected CR} )$$

- Signal Sideband Generation : any periodic motion of mirror surface

$$\begin{aligned} E_{ref}(x,y,t) &= \exp(2ik\delta(x,y) \cdot \sin(\Omega_{AF}t)) \cdot \exp(i\omega_0 t) \cdot E_{in}(x,y) \\ &\approx \{ \exp(i(\omega_0 + \Omega_{AF})t) - \exp(i(\omega_0 - \Omega_{AF})t) \} \cdot k\delta(x,y) \cdot E_{in}(x,y) \\ &\quad + \exp(i\omega_0 t) \cdot E_{in}(x,y) \end{aligned}$$



- Thermal deformation : Hello, Vinet

Stored beam is used to calculate thermal effects

```
THERMOELASTIC( beamSize, Psubs, Pcoat [, T0] )  
THERMALPHASE( beamSize, Psubs, Pcoat [, T0] )
```

# SIS Basic Ingredients - 2

- Random surface - 2D surface with f<sup>power</sup>
  - » NOISESPEC( rand\_seed, rms, power, WykoIndex )
- Wedge angle of beam splitter

$$ROC' = (1 + 2\varepsilon)ROC$$

$$w' = (1 + \varepsilon)w$$

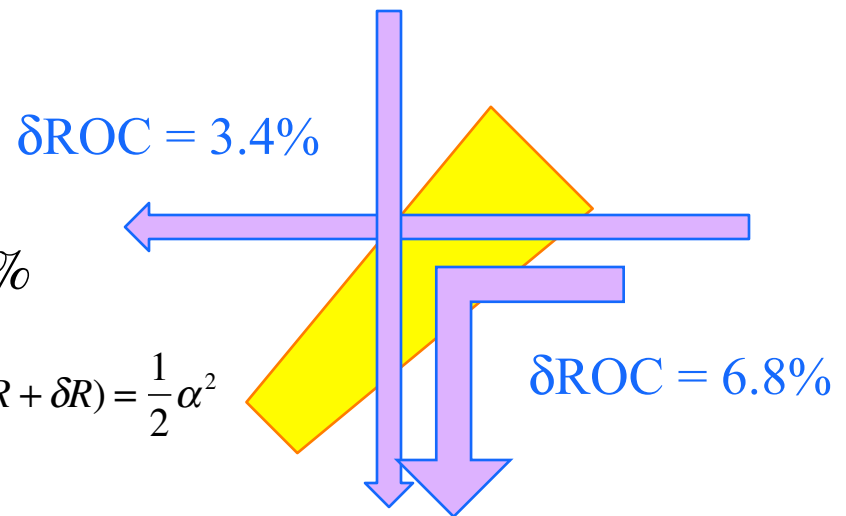
$$\varepsilon = \frac{2(n^2 - 1)}{\sqrt{2n^2 - 1}} \vartheta_w = 1.23\vartheta_w = 1.7\%$$

$$ModeMismatch(R, R + \delta R) = \frac{1}{2}\alpha^2$$

$$\alpha = k \frac{w^2}{4} \frac{\delta R}{R}$$

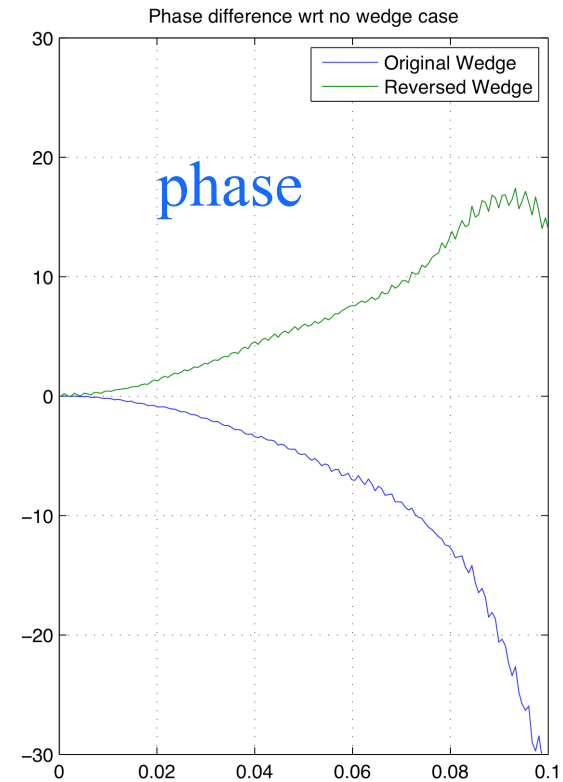
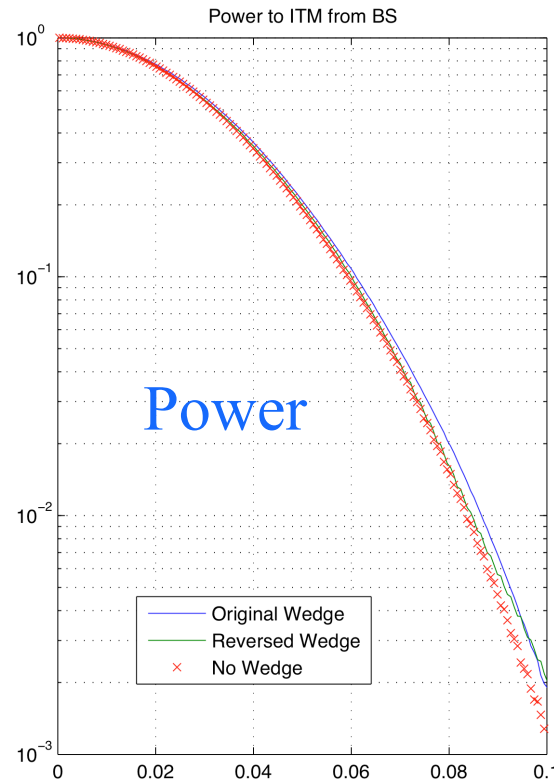
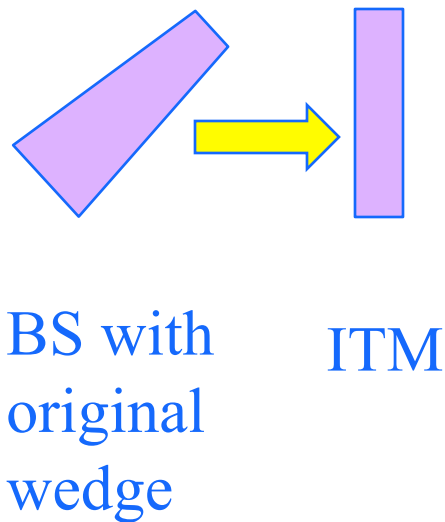
$$= 0.1 \text{ advLIGO}$$

$$= 0.004 \text{ LIGO I}$$



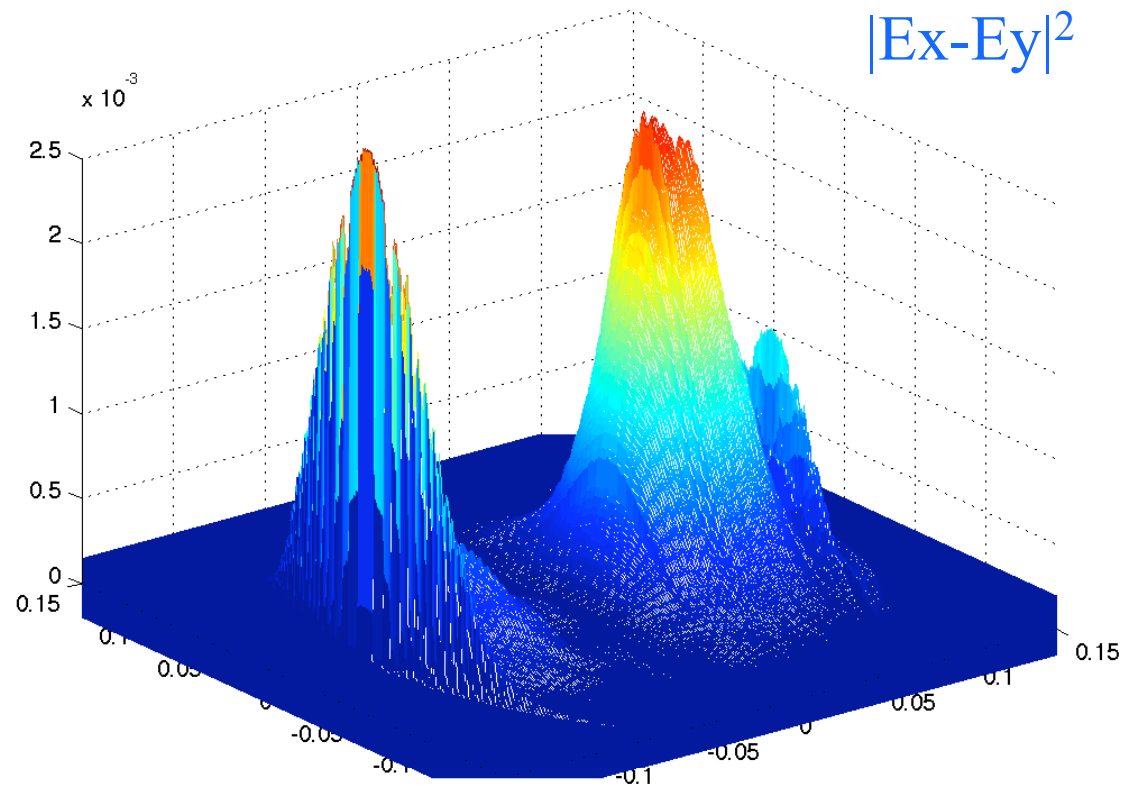
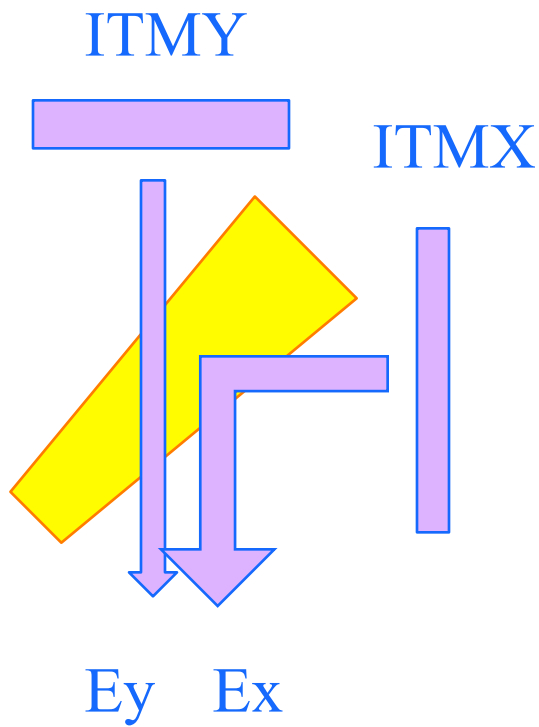
# Using SIS to study wedge angle effect - 1

## Beam profile going to ITM from BS





# Using SIS to study wedge angle effect - 2



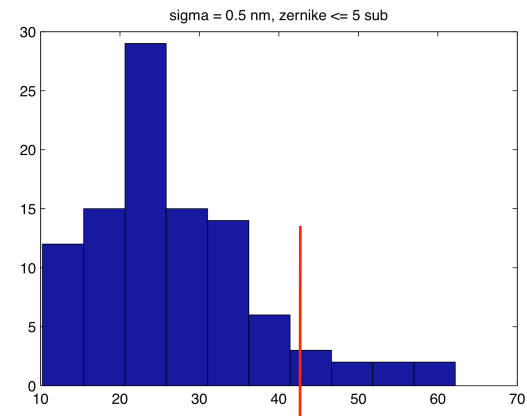
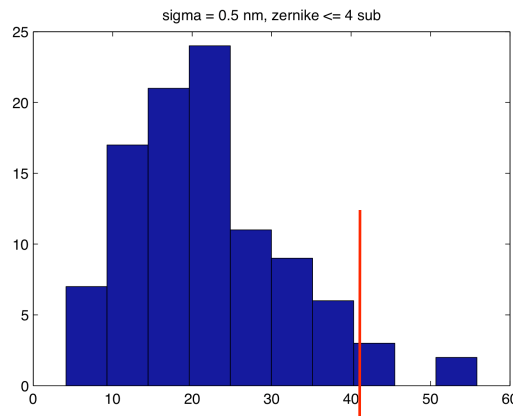


# Using SIS to study mirror rms requirement

Zernike  $\leq 4$  subtracted

Zernike  $\leq 5$  subtracted

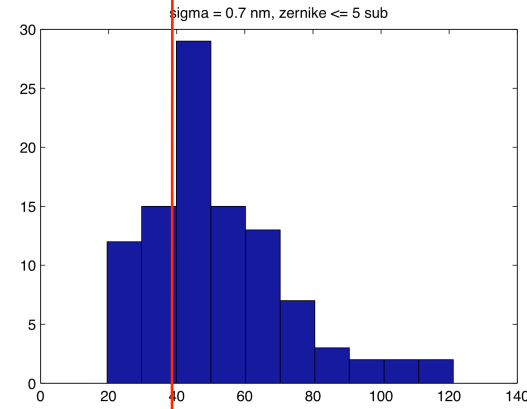
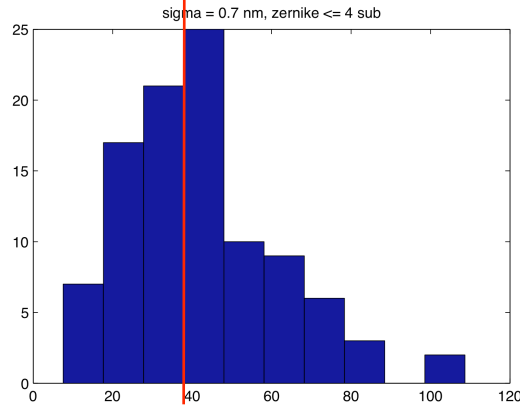
rms = 0.5nm



40ppm

40ppm

rms = 0.7nm

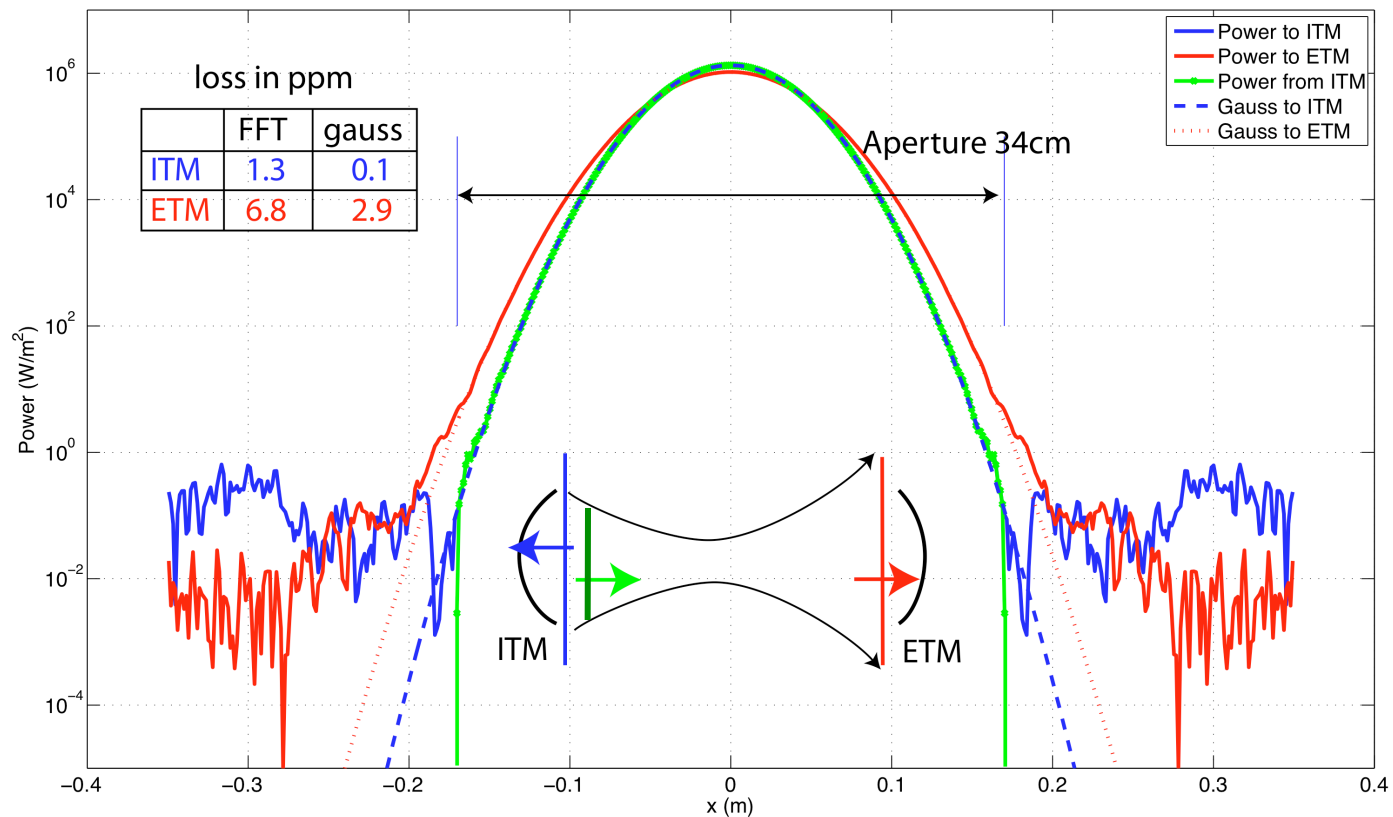


40ppm

40ppm



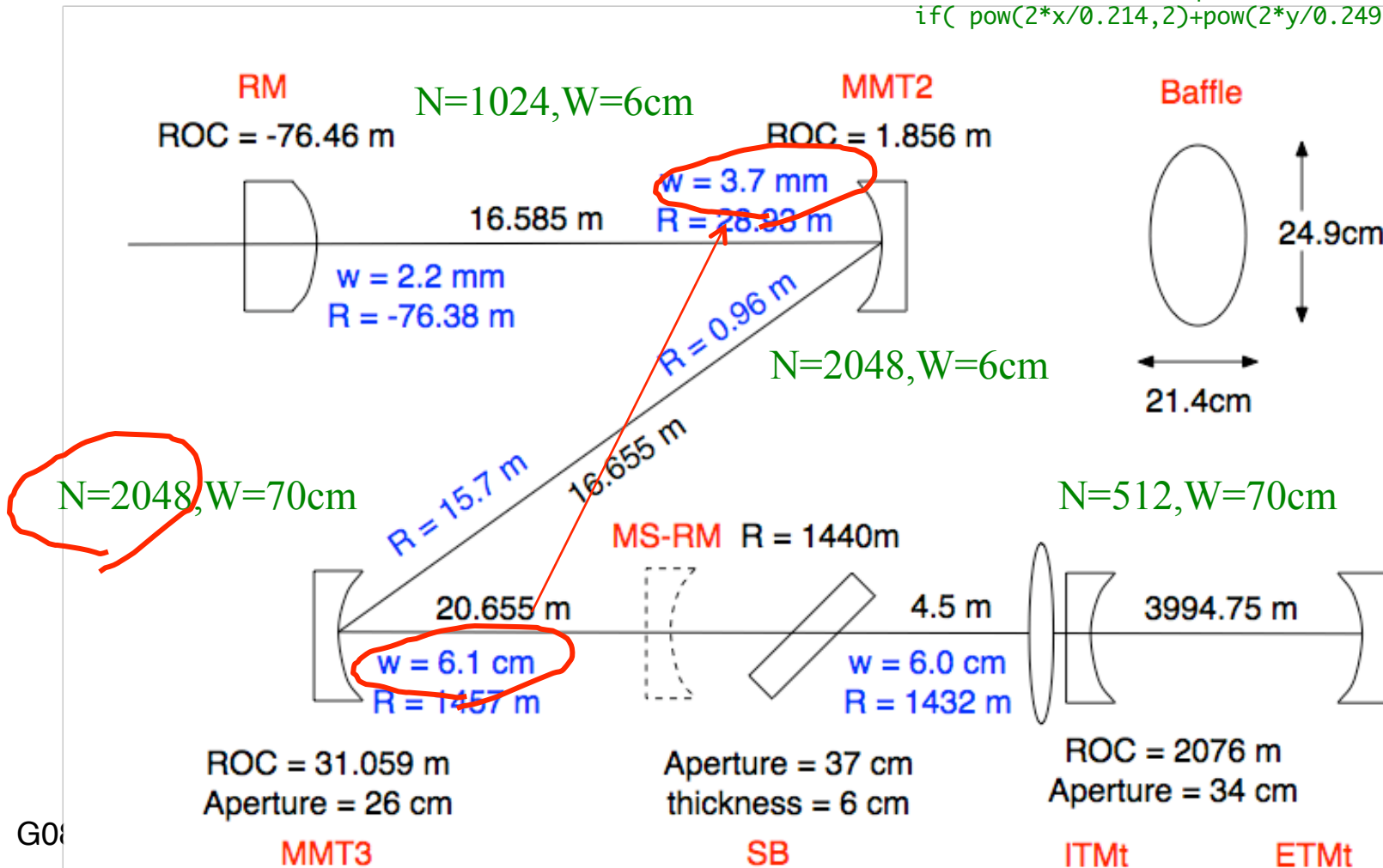
# Diffraction effect in FP cavity





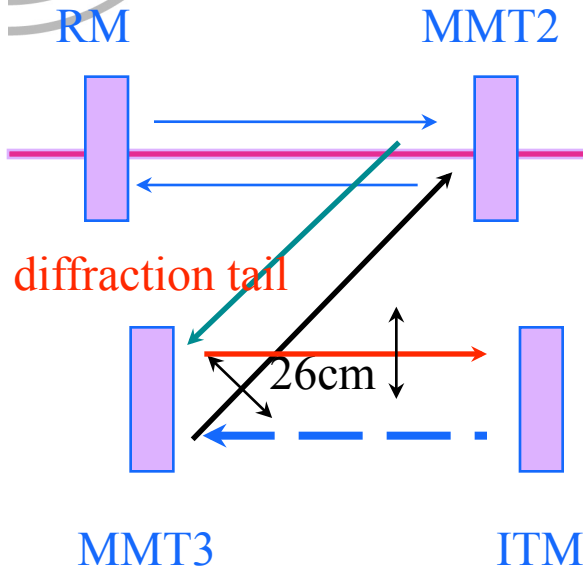
# Diffraction effect in Stable Michelson cavity

```
ITM.opt.AR_trans =  
if( pow(2*x/0.214,2)+pow(2*y/0.249,2) < 1, 1, 0 )
```

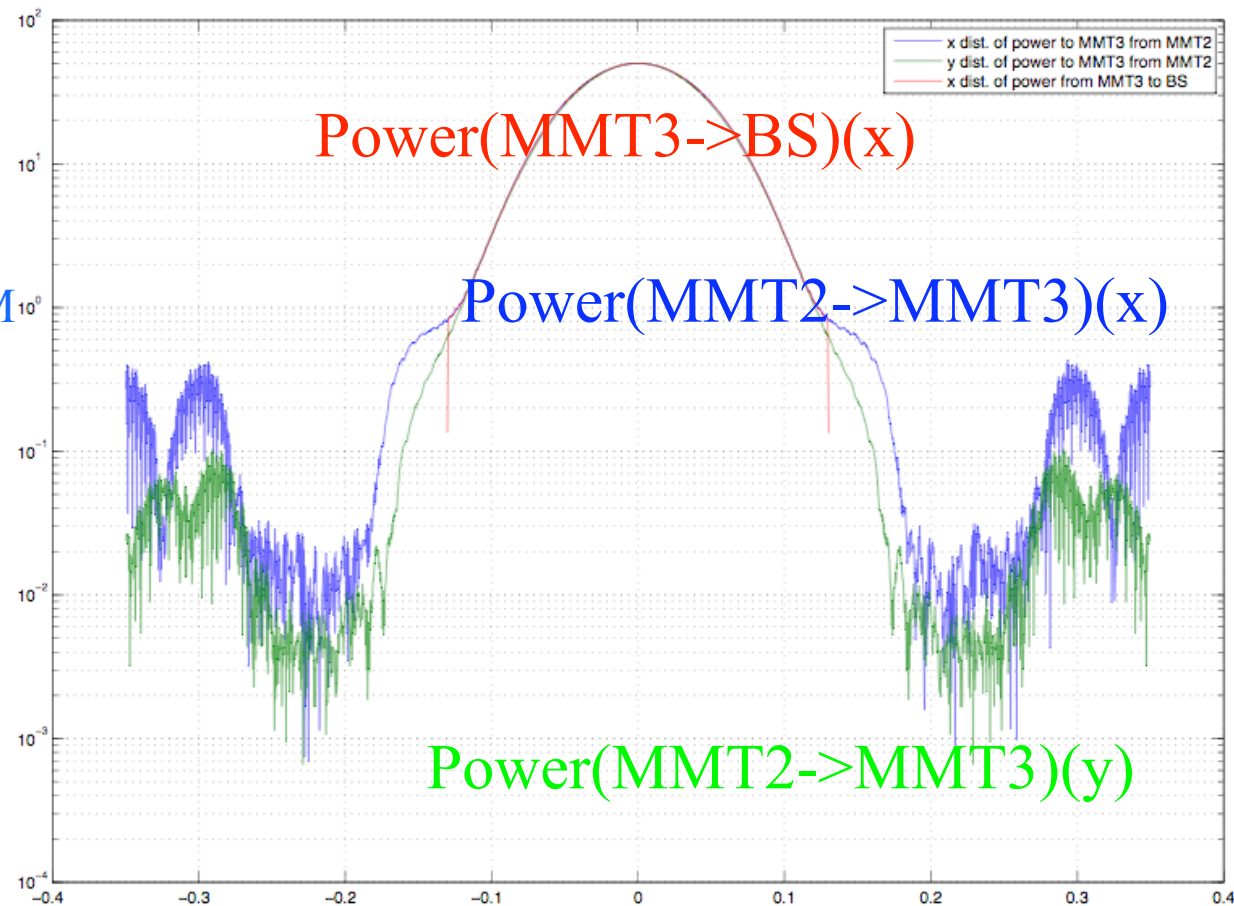




# Power loss on MMT3 (ITMY $\leftrightarrow$ SRM case)



loss = 330ppm  
(energy outside of  
MMT3 surface)





# Loss under different conditions

MMT aperture (cm)		beam size on ITM (cm)	Coupled cavity	loss on MMT3 (ppm)
26cm	ETM ROC	6cm	Y-arm + SRM(*)	330
26cm	ITM ROC	6cm	X-arm + SRM(*)	600
28cm	ITM ROC	6cm	Y-arm + SRM	140
26cm	ETM ROC	5.5cm (**)	Y-arm + SRM	47
26cm	ETM ROC	5.5cm (**)	X-arm + SRM	60

(\*) When a baffle is placed in front of ITMY, Y-arm+SRM configuration comes very close to X-arm+SRM case.

(\*\*) [http://ilog.ligo-wa.csiro.au:7285/advligo/Test\\_Mass\\_Beam\\_Sizes](http://ilog.ligo-wa.csiro.au:7285/advligo/Test_Mass_Beam_Sizes), asymmetric case with 5.5cm on ITM and 6.2cm on ETM.

With the baffle size of Mike's choice - 214mm x 249mm - the beam going through a baffle is cut off by 250ppm. If the baffle size of 1cm larger in both direction (224mm x 259mm), the cutoff is 55ppm. The numbers in the above table were calculated without baffles.



# Using SIS to study PI

## Signal generation by surface map

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- Investigating a Parametric Instability
- SUFR project by Hans Bantilan, mentored by Bill Kells
  - » G060385-00-Z
- Simulate a stationary field for a given acoustic mode, instead of using modal expansion, to calculate the overlapping integral
- Combined with Dennis' FEM package to calculate acoustic modes
- 9061 modes for  $f < 90\text{KHz}$



# What you need to run SIS

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- gcc compiler + fftw library
- or use program on Caltech machine
- SIS manual T070039
- Patience to simulate stable cavity – 2048 grids