



# Dynamics of Mixed Binaries

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# Outline

- ⑥ Motivation(s)
- ⑥ Previous Work
- ⑥ Recent Results
- ⑥ Future Plans



# Motivation(s)



- ⑥ Dynamical details of mergers unknown
  - △ hard to observe directly
  - △ equation of state (EOS) and structure of neutron stars (NS) not known exactly
- ⑥ Gravitational wave signal expected to be visible: expected detection rate of  $> 1/y$  (advanced detectors)



# Previous Work - Overview

Typical binary systems in GR:

- ⑥ Binary black hole systems (BBH)
- ⑥ Binary neutron star systems (BNS)
- ⑥ Neutron star - black hole systems (BHNS)

	BBH	BNS	BHNS
General Relativity	X	X	X
Hydrodynamics		X	X
Singularity problems	X	?	X

→ need experience from BBH **and** BNS simulations



# Previous Work - Newtonian

First studies: Newtonian physics:

- ⑥ Zwart et al. (1998), analytical  
Stable mass transfer from NS to BH
- ⑥ Janka et al. (1999), numerical  
Short mass transfer (few cycles) for mass ratio  $\gg 1$
- ⑥ Lee et al. (1999), numerical  
Mass transfer only in certain cases

Newtonian studies with relativistic modifications  
(Paczynsky)

- ⑥ Rosswog et al. (2005), numerical  
Complete disruption, no stable mass transfer



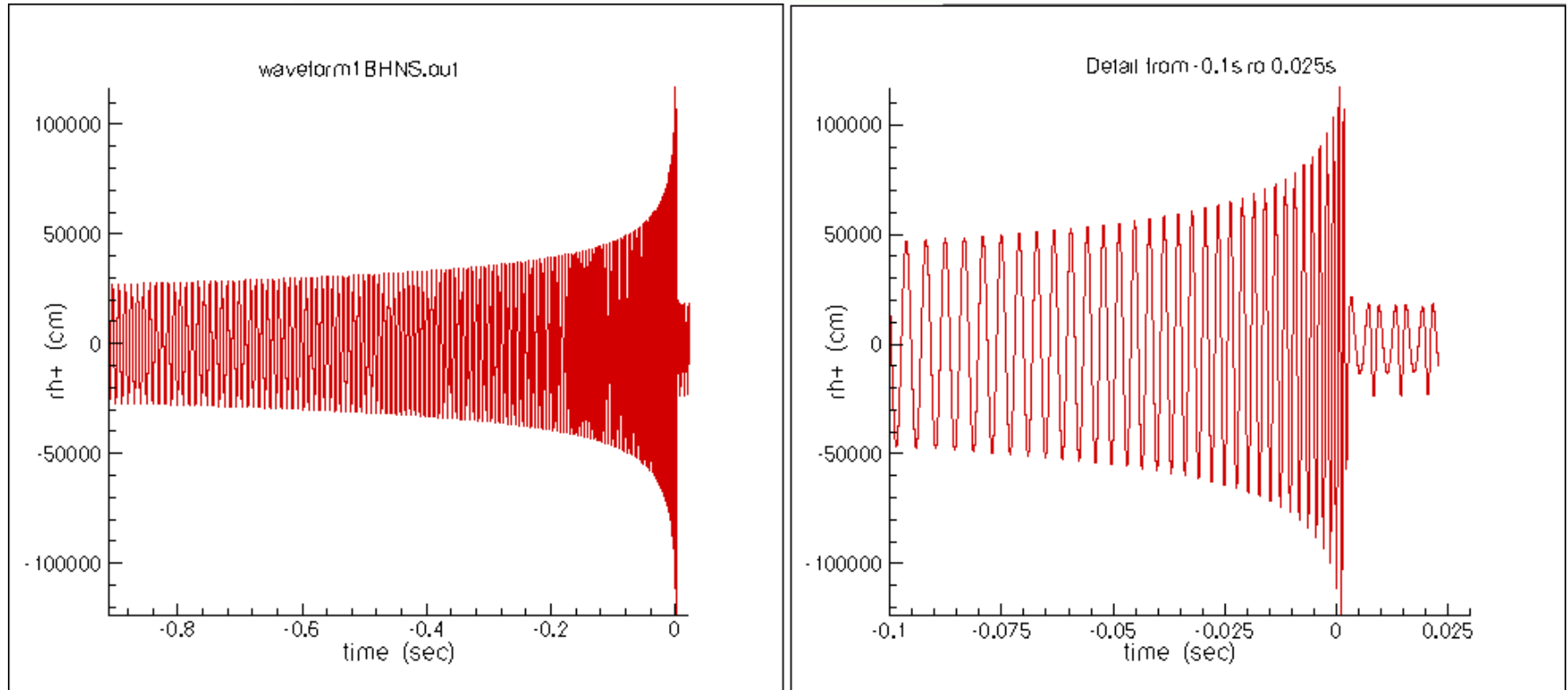
# Previous Work - Relativistic

## Relativistic studies:

- ⑥ Baumgarte et al. (2004), Taniguchi et al. (2005), num.  
No disruption before merger, however: limited to big BH/NS mass ratios, quasi-stationary sequence
- ⑥ Bishop et al. (2005), numerical  
Full evolution, but only short-term
- ⑥ Miller et al. (2005), analytical  
Prompt merger for  $M_{NS} < M_{BH}$  and slowly spinning BH because of angular momentum loss due to GW
- ⑥ Sopuerta et al. (2006), numerical  
Full evolution, but restricted to large mass ratios and/or large separations



# Previous Work - Typical Waveform



Lee et al. (1999)



# Recent Work - Setup

Used “tools” from other simulations:

- ⑥ “3+1” split of GR
- ⑥ Computational infrastructure: Cactus
- ⑥ Mesh refinement: Carpet
- ⑥ Conformal formulation of GR equations (BSSN)
- ⑥ Formulation and implementation of hydrodynamics equations (Euler, HRSC): Whisky
- ⑥ Analysis tools and vacuum excision technique





# Recent Work - Setup

New “tools” for a BHNS simulation:

- ⑥ Initial data for a BHNS system
- ⑥ Excision of Hydrodynamics at BH horizons  
(Phys. Rev. D 71:104006), applied also to  
Neutron star collapse (Phys. Rev. D 71:024035)
- ⑥ Special Gauge conditions for evolution



# Recent Work - Initial data

## Procedure:

- ⑥ Specify sources (NS, BH), separation, velocities ect.
- ⑥ Solve for constraint equation(s)
- ⑥ Check for physical parameters

## Constraint equations:

- ⑥ Analog to energy and momentum conservation
- ⑥ Nonlinear, elliptic equations (4)

## Solver:

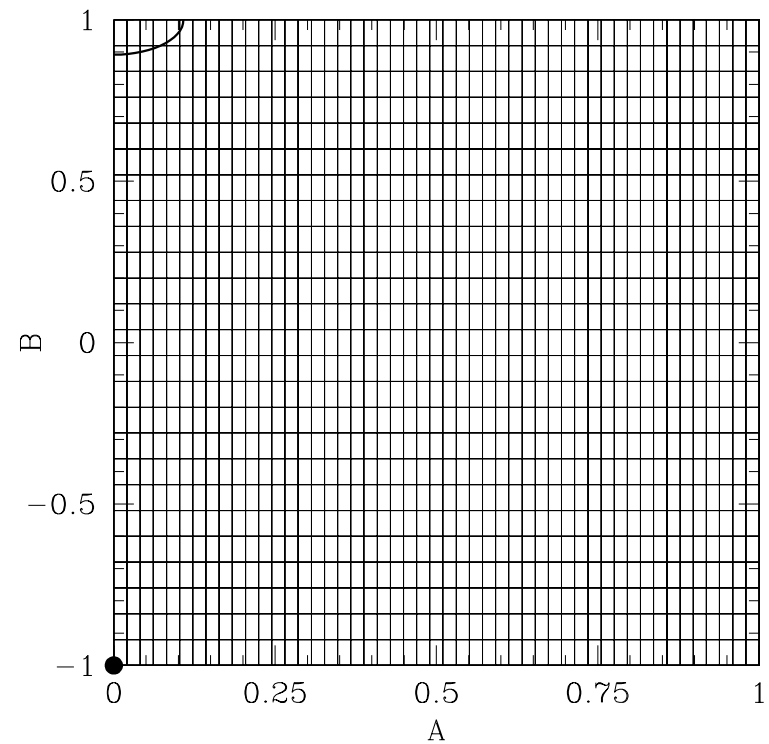
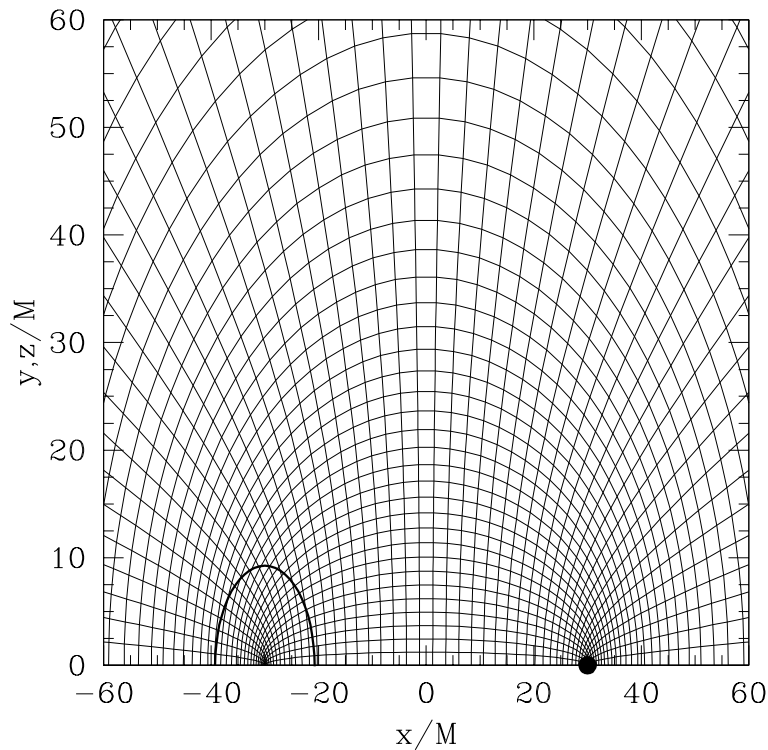
- ⑥ spectral, compactified domain
- ⑥ modified version of BBH solver by Ansorg



# Recent Work - Initial data



Example for spectral grid setup:



## Recent Work - Initial data

Simplification: zero (initial) velocities, time-symmetry:

- ⑥ Only one elliptic equation left
- ⑥ Limitation to headon collisions

Problems:

- ⑥ Slow convergence (for a spectral method)
- ⑥ Slow evaluation of data onto the evolution grid

Particular system:

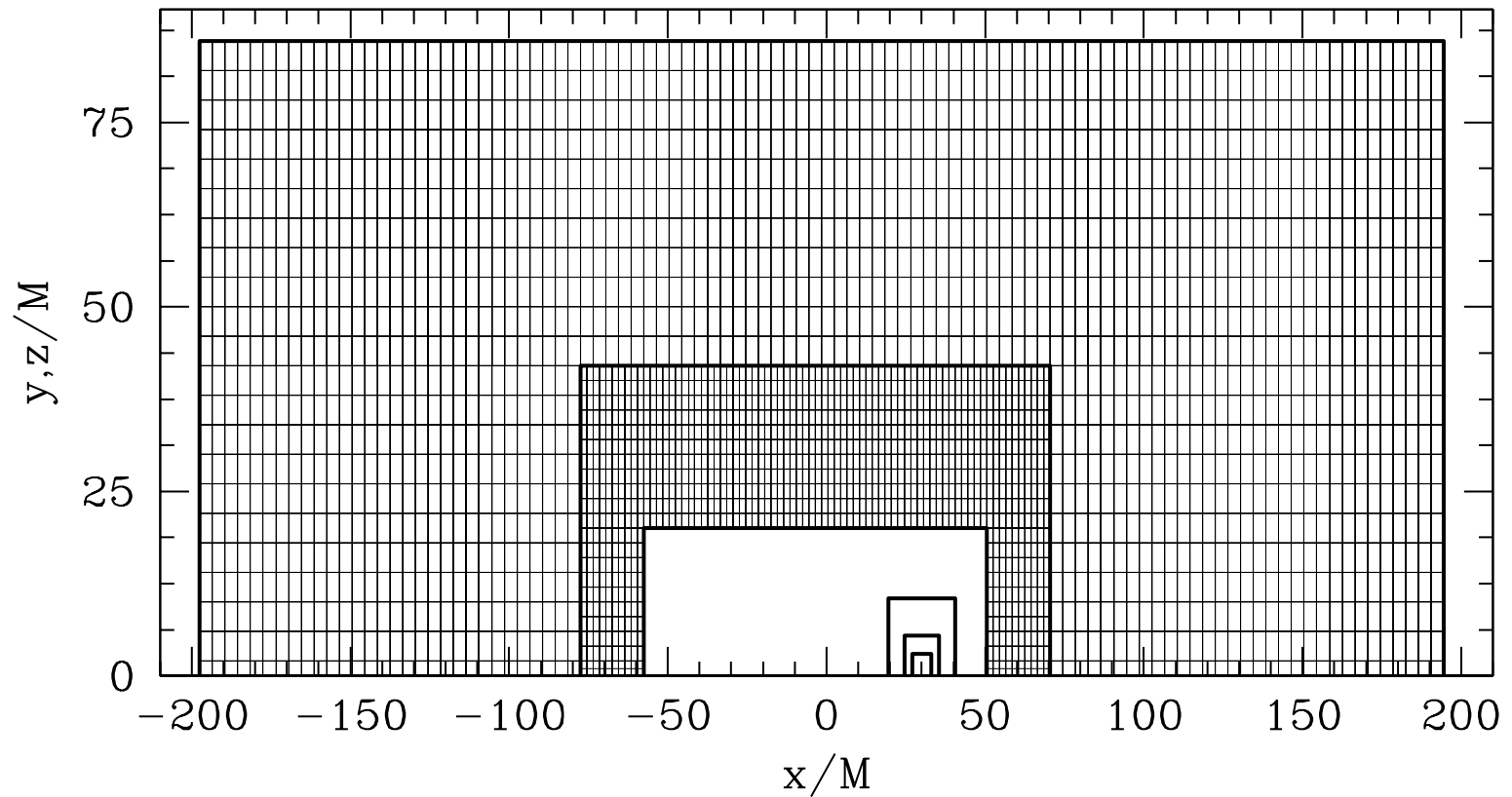
- ⑥  $M_{NS} \approx 5M_{\odot}$  (TOV, polytropic EOS)
- ⑥  $M_{BH} \approx 1M_{\odot}$
- ⑥ separation  $d \approx 90\text{km}$



# Recent Work - Evolution details

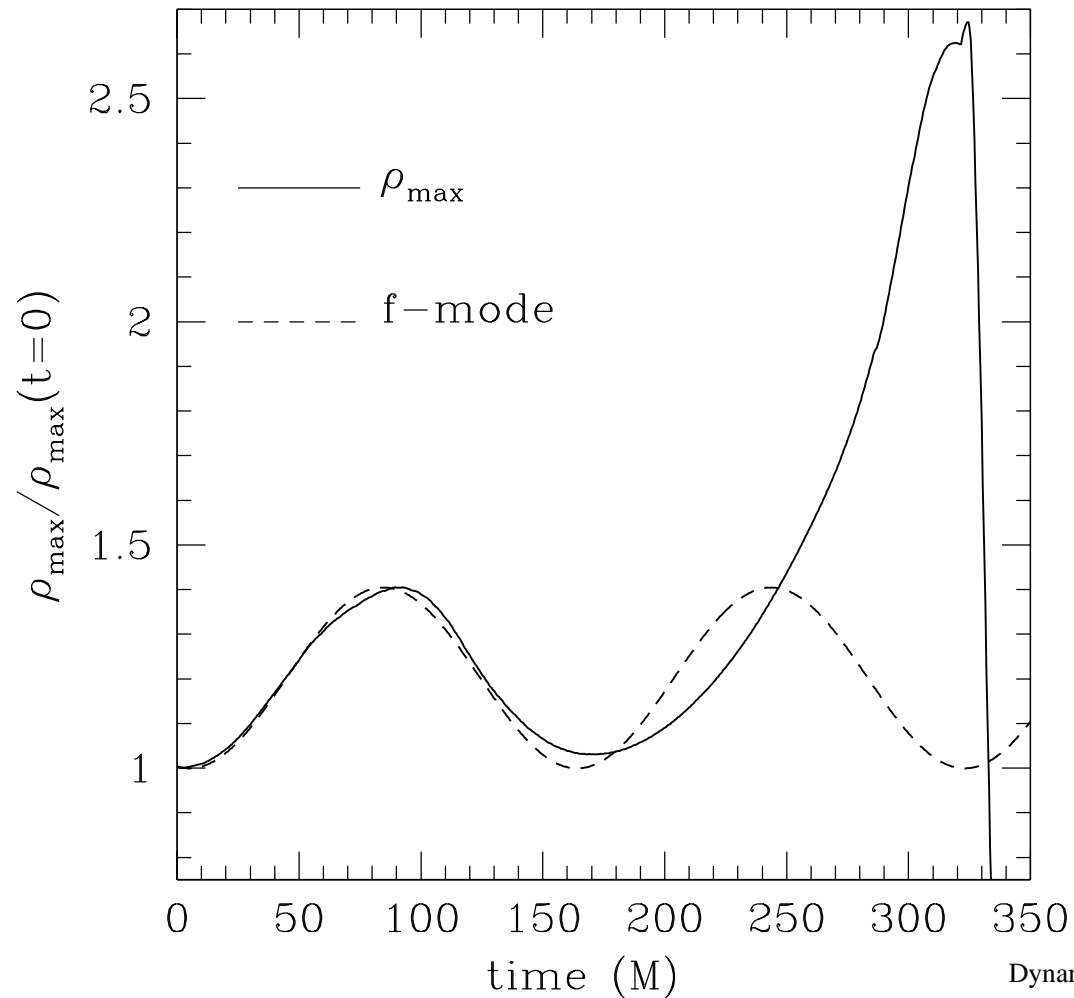


Example for evolution grid setup:



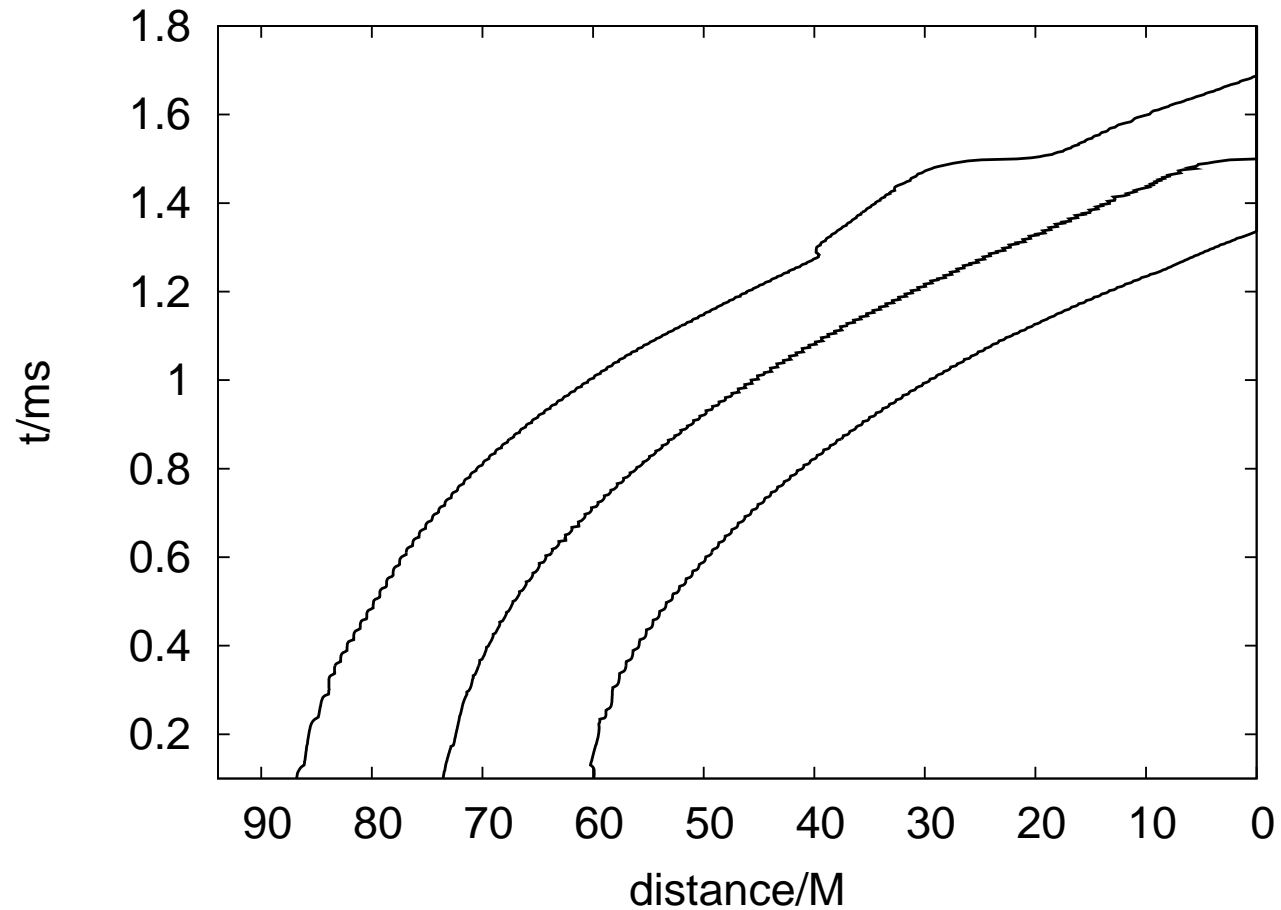
# Recent Work - Evolution details

Maximum density evolution ( $f_F \approx 1.28\text{kHz}$ ):



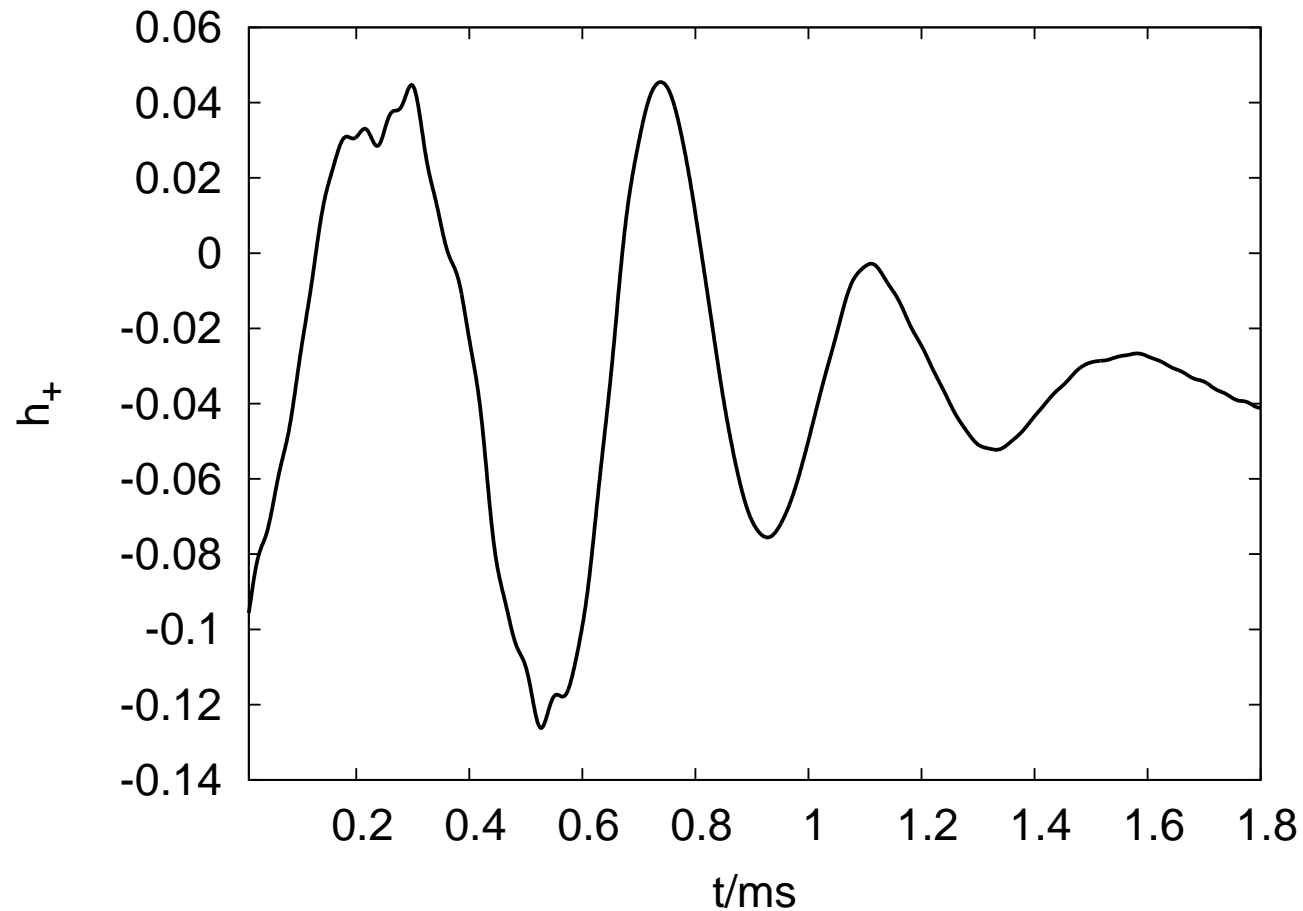
# Recent Work - Evolution details

Spacetime diagram:



# Recent Work - GWs

Gravitational waves ( $f \approx 2.06\text{kHz}$ ):



Movie



# Results / Future Plans

## Results:

- ⑥ Initial data suitable for long evolutions
- ⑥ Used evolution techniques allow for long evolutions
- ⑥ Gravitational waves can be obtained

## Future plans:

- ⑥ More realistic initial data: velocities  $\neq 0$  (orbiting systems)
- ⑥ Improved handling of BH interior
- ⑥ Better gauge conditions for really long term simulations
- ⑥ More realistic EOS

