

## Goals of isolation and suspension subsystem modeling:

- aid in the overall structure design.
- aid in the local control system overall design.
- allow some optimization of design parameters:
  - natural resonance frequencies.
  - masses.
  - wire/spring sizes and attachment points.
  - local control compensation functions.
- allow prediction of local electronic and thermal noise propagation
- allow prediction of vibration transfer functions.

## Goals of combined system modeling:

- aid in selection of cascaded component systems.
- aid in ordering of systems.
- allow better optimization of design parameters.
- allow better prediction of total noise.

Example problem: high- $Q$  pendulum mounted on low- $Q$  active system.

- Coupling to outer stage thermal loss depends on loop gain in active system.
- Loop gain in active system affects isolation from outer noises.

- Unity gain point frequency regions of active stages can. exaggerate coupling to thermal losses.
- Perhaps we need to model complete. isolation/suspension system to calculate noise of last stage.

## Collaboration in system modeling:

- Various groups are developing suspension/isolation candidate subsystems for advanced LIGO.
- Each group best able to create and test subsystem models against. experimental measurement.
- Ideally, these models should be developed with a goal of combining them with others.

## Two ways to cascade models:

- Use individual state-space (or other) models to calculate matrices of frequency-dependant admittances among all connection points, then exchange results and combine. (likely to be too much work.).
- Write individual state-space models in a way that allows them to be cascaded.

## Requirements for cascading state-space dynamic models with Matlab:

- Standard coordinate systems and units
- Equations of motion that are used to derive state spaces must be robust to (usually) small displacements and rotations of entire system.
- Inputs and outputs for inner and outer attachment points should be in standard places (indices) in each model, and have standard meanings.

## Cascading systems with “soft connections.”

When one system ends in a compliant member and the other is a rigid mass, it is sufficient to use the positions of the attachment points:

- input and output vectors each begin with the 6 DOFs of the upper (outer, “o”) connection point, and the 6 DOFs of the lower (inner, “i”) connection point. Write  $A, B, C, D$  for each subsystem such that:

$$u = [x^o, y^o, z^o, \phi_x^o, \phi_y^o, \phi_z^o, x^i, y^i, z^i, \phi_x^i, \phi_y^i, \phi_z^i, \dots]^T$$

$$y = [x^o, y^o, z^o, \phi_x^o, \phi_y^o, \phi_z^o, x^i, y^i, z^i, \phi_x^i, \phi_y^i, \phi_z^i, \dots]^T$$

- Use the Matlab `append` command to combine all state spaces (as independent subspaces).
- Use Matlab `connect` command to connect each system's attachment point outputs to the neighboring system's inputs, and defining which outputs and inputs are retained in the complete system.
- Use resulting  $A, B, C, D$  for desired purpose.

## Arbitrary connection types:

When it is necessary to connect systems with other interface conditions, pairs of input/output variables must be connected, such as  $\{F, v\}$  or  $\{\tau, \theta\}$ .



*Note 1, Linda Turner, 04/20/98 04:27:18 PM*  
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