

ONE YEAR AT THE 40 METER
(School of Hard Locks)

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**ELECTRONIC
COPY**

LIGO Science Seminar

Caltech - Pasadena California

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[†]Work at Caltech supported by LIGO Visitor's Program

Outline

- Summary of 40 Meter Status
- 40 Meter *vs* LIGO – Comparison
 - Optics Refresher
 - Instrument Comparison
- Why Can't We Align the IFO While Maintaining Lock?
(Snapshot of most important investigation underway)
- Wave Front Sensing at the 40 Meter
- Michigan Gravity Wave Group (MGWG)
 - Contributions
 - Plans

Summary of 40 Meter Status

Configuration

- LIGO-like topology
Recycling cavity with Fabry-Perot (FP) arms;
Schnupp asymmetry
- Three of six masses with LIGO-like core optics suspensions
 - Single-wire loop
 - Permanent Magnet actuation
 - Four-layer isolation stacks
- Low-loss optics (514 nm)
- Single-frequency frontal modulation servo scheme
- LIGO-like PSL system
- Wave Front Sensing (WFS) available for auto alignment
(Using hardware / software adapted from MIT FMI)
- Wide scale use of digital controls & filtering
- LIGO-like DAQ and data display programs in place

Summary of 40 Meter Status

Recycling Operation Accomplishments

- Power Recycled Michelson (PRM) cavity locked (2-servo bootstrap) – 11/97
- Full recycled IFO lock – 12/97
- PRM behavior confirmed to agree with design (Gains Γ alignment sensitivity Γ degeneracy)
- Investigation of modal structure via RF sideband resonances
- Full control of PRM alignment via WFS
- Control of single end-mass alignment DOF via WFS

Summary of 40 Meter Status

Work in Progress or Immediately Planned

- Investigate lock instability when IFO best aligned
- Confirm previous determination that IFO is under-coupled
(Due to anomalously high arm losses)
- Determine servo dynamic ranges / gain margin limitations
- Complete WFS control of end-mass alignments
(Expected to reduce large power fluctuations in arms)
- Identify and fix worst noise sources
- Take one week of data (December 12-18)
with all DAQ channels recorded

Summary of 40 Meter Status

The 40 Meter Crew in 1998[†]:

Caltech

Mark Coles¹ΓBill KellsΓJenny Logan²Γ
Nergis Mavalvala³ΓSteve Vass

U. Michigan

Dick GustafsonΓKeith RilesΓJamie Rollins⁴

Short-term Visitors

Raffaele Flaminio (VIRGO)ΓKoji Arai (TAMA)

¹Departed in June for Livingston

²Departed in September for JPL

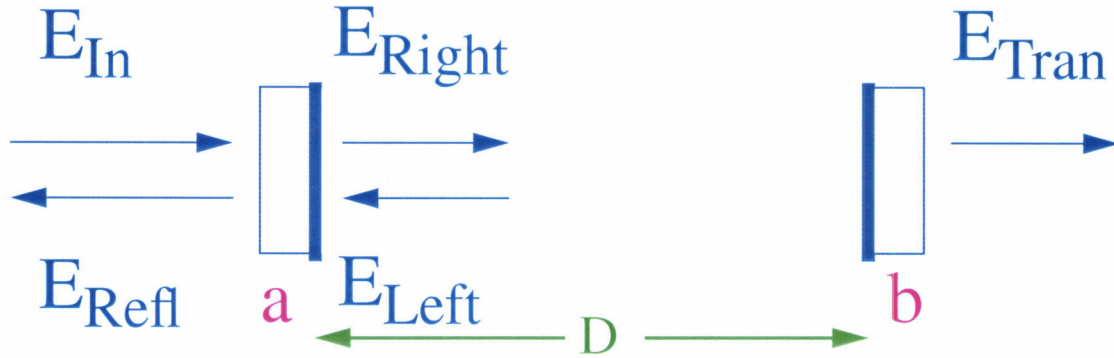
³Began 40M work in September

⁴Began 40M work in May

[†] Many thanks to S. AndersonΓR. BorkΓH. DingΓJ. HeefnerΓA. IvanovΓ
W. MajidΓS. TilavΓand L. Wallace

40 Meter *vs* LIGO – Comparison

Cavity Optics Refresher:



Conventions used:

$$R_i = r_i^2; \quad T_i = t_i^2; \quad L_i = 1 - R_i - T_i$$

$$r_a, r_b > 0; \quad \phi = 2kD - 2\phi_{\text{Guoy}}$$

Steady-state equations[†]:

$$E_{\text{Right}} = t_a E_{\text{In}} - r_a E_{\text{Left}} \qquad E_{\text{Left}} = -r_b e^{i\phi} E_{\text{Right}}$$

$$E_{\text{Refl}} = r_a E_{\text{In}} + t_a E_{\text{Left}} \qquad E_{\text{Tran}} = t_b e^{i\phi/2} E_{\text{Right}}$$

Solutions:

$$\frac{E_{\text{Refl}}}{E_{\text{In}}} = \frac{r_a - (1 - L_a)r_b e^{i\phi}}{1 - r_a r_b e^{i\phi}}$$

$$\frac{E_{\text{Tran}}}{E_{\text{In}}} = \frac{t_a t_b e^{i\phi/2}}{1 - r_a r_b e^{i\phi}}$$

Resonance (anti-resonance) when $\phi = 0$ (π)

[†]Time dependence discussed later

40 Meter *vs* LIGO – Comparison

Closer Look at Transmission

On resonance:

$$\frac{E_{Tran}}{E_{In}} = \frac{t_a t_b}{1 - r_a r_b}$$

Power away from resonance:

$$\left| \frac{E_{Tran}}{E_{In}} \right|^2 = \frac{t_a^2 t_b^2}{1 + r_a^2 r_b^2 - 2 r_a r_b \cos \phi}$$

For $r_a, r_b \approx 1\Gamma$

$$\text{FWHM}_\nu \approx \frac{c}{2D} \frac{1 - r_a r_b}{\pi \sqrt{r_a r_b}} \equiv \frac{\text{FSR}}{F}$$

where FSR = Frequency spacing between cavity resonances

and $F = \text{Finesse} \equiv \pi \sqrt{\frac{r_a r_b}{1 - r_a r_b}}$

For $(1 - r_b) \ll (1 - r_a) \ll 1\Gamma$

$$F \approx \frac{\pi}{1 - r_a}$$

High Finesse \implies Sharp Resonance

\implies Large Power Buildup

40 Meter *vs* LIGO – Comparison

40 Meter arms:

$$r_a \approx 0.997$$

$$r_b \approx 0.99994$$

$$\implies F \approx 1100$$

LIGO arms:

$$r_a \approx 0.985$$

$$r_b \approx 0.999960$$

$$\implies F \approx 207$$

40 Meter vs LIGO – Comparison

Closer Look at Reflection

On resonance:

$$\frac{E_{Refl}}{E_{In}} = \frac{r_a - (1 - L_a) r_b}{1 - r_a r_b}$$

For $(1 - r_a), (1 - r_b) \ll 1\Gamma$

expand $r_i = \sqrt{(1 - T_i - L_i)} \approx 1 - \frac{1}{2}(T_i + L_i)$

$$\begin{aligned} \frac{E_{Refl}}{E_{In}} &\approx -\frac{T_a - (L_a + T_b + L_b)}{T_a + (L_a + T_b + L_b)} \\ &\approx -\frac{T_a - \Sigma(\text{Losses})}{T_a + \Sigma(\text{Losses})} \end{aligned}$$

Some jargon:

“Overcoupled” means $\frac{E_{Refl}}{E_{In}} < 0$

“Undercoupled” means $\frac{E_{Refl}}{E_{In}} > 0$

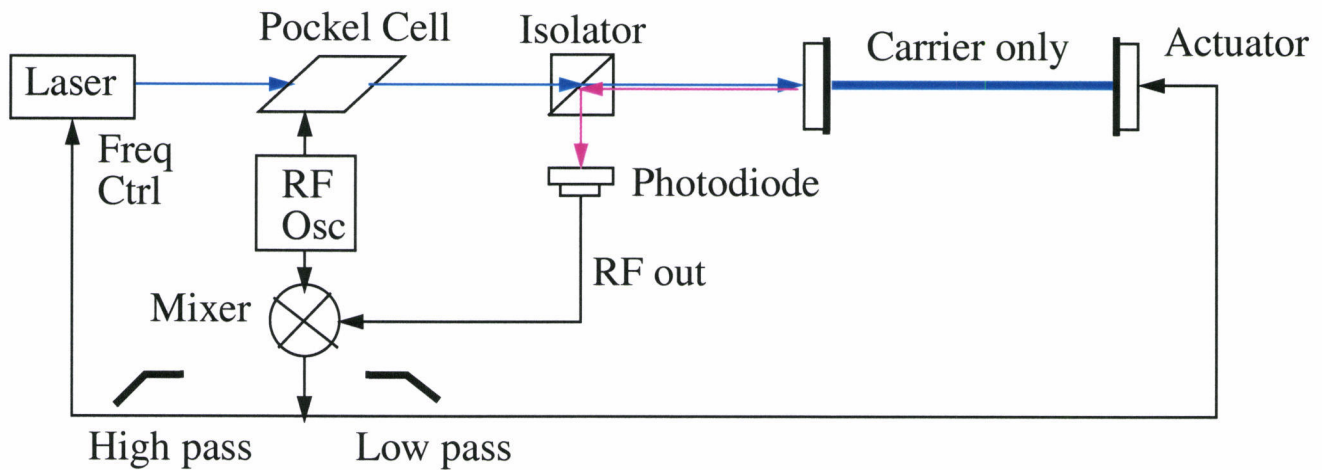
$\Sigma(\text{Losses}) < \text{input mirror transmission} \implies \text{Overcoupled}$

End mirror absent ($\frac{E_{Refl}}{E_{In}} = +r_a$) $\implies \text{Undercoupled}$

40 Meter vs LIGO – Comparison

How does one “lock” to resonance?

Pound-Drever-Hall technique:



Phase-modulate light such that

- Carrier resonates in cavity: $N\lambda_{CR} = 2D$
- Sidebands (nearly) anti-resonate: $(N \pm m + \frac{1}{2})\lambda_{SB} = 2D$

Requires:

$$\text{Modulation frequency } f_{mod} = (m + 1/2) \times \text{FSR}$$

$$(\text{or } D = \frac{1}{2}(m + \frac{1}{2})\lambda_{mod})$$

$$\text{40 Meter arms: } f_{mod} = 32.7 \text{ MHz } (m \approx 8)$$

$$\text{LIGO arms: } f_{mod} = 24.6 \text{ MHz } (m \approx 650)$$