Modal Damping of a Quad Pendulum for Advanced Gravitational Wave Detectors

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Abstract

Motivation: Observe gravitational waves from astrophysical sources (supernovae, pulsars, black hole mergers, etc) using the LIGO observatories.

Problem: Multi-DOF isolation systems enhance ground motion at high Q resonances. Damped using active feedback. This control introduces additional noise. Optimal control required achieve adequate trade-off.

Solution: Modal damping to simplify and decouple optimization of each mode's damping. Also permits real-time tuning.

Outline

- 1. LIGO and gravitational waves
- 2. Seismic (vibration) isolation
- 3. Competing damping control goals
- 4. Method of modal damping
- 5. Optimization of modal damping
- 6. Results



Gravitational Waves



• Supernovae

LIGO

- Asymmetry required
- Coalescing Binaries
 - Black Holes or Neutron Stars Mergers
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- Pulsars
 - Asymmetry required
- Stochastic Background (Big bang, etc.)

LIGO The Laser Interferometer Gravitational-wave Observatory (LIGO)





Hanford, WA



Livingston, LA

5

- 3, 4 km interferometers at 2 sites in the US
- Michelson interferometers with Fabry-Pérot arms
- Optical path enclosed in vacuum
- Sensitive to strains around 10⁻²² -> 10⁻¹⁹m_{rms}
- LIGO Budget ≈ \$60 Million per year from NSF.
- Operated by MIT and Caltech.



If we put LIGO in Cambridge, MA



LIGO spans 16 km². Cambridge, MA covers 16.65 km² (wikipedia http://en.wikipedia.org/wiki/Cambridge_Massachusetts).

LIGO Scientific Collaboration LIGO •University of Michigan University of Minnesota

- The University of Mississippi Massachusetts Inst. of Technology

 - Monash University
 - Montana State University
 - Moscow State University
 - National Astronomical Observatory
 - Northwestern University
 - •University of Oregon
 - Pennsylvania State University
 - •Rochester Inst. of Technology
 - Rutherford Appleton Lab
 - •University of Rochester
 - •San Jose State University
 - •Univ. of Sannio at Benevento, and Univ. of Salerno
 - •University of Sheffield
 - •University of Southampton
 - •Southeastern Louisiana Univ.
 - •Southern Univ. and A&M College
 - Stanford University
 - •University of Strathclyde
 - •Syracuse University
 - •Univ. of Texas at Austin
 - •Univ. of Texas at Brownsville
 - Trinity University
 - •Tsinghua University
 - •Universitat de les Illes Balears
 - •Univ. of Massachusetts Amherst
 - •University of Western Australia
 - •Univ. of Wisconsin-Milwaukee
 - •Washington State University
 - University of Washington

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Projected Sensitivity for Advanced LIGO



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LIGO

Suspensions and Seismic Isolation

Advanced LIGO test mass isolation

active isolation platform (2 stages of isolation) hydraulic external preisolator (HEPI) (one stage of isolation) quadruple pendulum (four stages of isolation) with monolithic silica final stage



active isolation platform (2 stages of isolation)

quadruple pendulum (four stages of isolation)

Installing prototype quad pendulum with glass optic on metal wires, Jan 2009 at MIT.

Quadruple Pendulum



LIGO



Purpose

• Test mass (stage 4) isolation. the test mass consists of a 40 kg high reflective mirror

Control

- Damping -stage 1
- Cavity length all stages

Sensors/Actuators

- BOSEMs at stage 1 & 2
- AOSEMs at stage 3
- Opt. levs. and interf. sigs. at stage 2
- Electrostatic drive (ESD) at stage 4

Multi-stage Isolation Performance



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Two Competing Goals



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Modal Damping with State Estimation



Modal Feedback Design



Damped Response to Impulse from Gnd.



0.018

0.009

0.001

ζ

0.040

16

Estimator Design



Choosing Q and R: Not Unique

$$J = \int_{0}^{\infty} \left(\begin{bmatrix} \widetilde{\mathbf{q}}^{T} & \dot{\mathbf{q}}^{T} \end{bmatrix} \mathbf{p} \begin{bmatrix} \widetilde{\mathbf{q}} \\ \dot{\mathbf{q}} \end{bmatrix} + \mathbf{z}_{m}^{T} \mathbf{R} \mathbf{z}_{m} \right) dt$$

$$\mathbf{L}_{m} = \arg \min(J)$$

$$\mathbf{Q}$$

$$\begin{bmatrix} \widetilde{q}_{1}^{T} & \dots & \dot{q}_{n-1}^{T} & \dot{q}_{n}^{T} \end{bmatrix} \begin{bmatrix} \mathbf{0} & \mathbf{0} \\ \dots & \mathbf{0} \\ \dots & \dots & \dots \\ \mathbf{0} & \mathbf{m}_{n-1}^{-2} \end{bmatrix} \begin{bmatrix} \widetilde{q}_{1} \\ \dots \\ \widetilde{q}_{n} \end{bmatrix} \qquad \mathbf{R} = \begin{bmatrix} R_{1} & \mathbf{0} \\ R_{2} & \dots \\ \mathbf{0} & \dots & R_{m} \end{bmatrix}$$

 m_i = modal mass of mode i

 m_i^{-1} = modal velocity impulse response amplitude

R is still to be determined

Solving the R matrix for MIMO Modal Damping

Try a bunch of R matrices and see what works best

$$J_{R}(R) = \max_{i} (T_{s,i}^{2}) + \max_{i} (N_{i}^{2})$$
$$R = \arg\min(J_{R})$$

Measure 'best' with an auxiliary cost function.

$$T_{s,i} = \frac{\text{Stage 4 settling time for DOF } i}{10 \text{ seconds}}$$

• $N_i = \frac{\text{Stage 4 sensor noise for DOF } i \text{ at 10 Hz}}{\text{Stage 4 noise requirement for DOF } i \text{ at 10 Hz}}$

DOFs *i* are: x, y, z, yaw, pitch, roll



Modal Estimation Cost

x Estimator Cost vs. **R** (x is the laser axis)



Optimal Noise Amplification





Conclusions

LIGO

- Modal damping provides an intuitive way to optimize a highly coupled, many DOF system, with strict noise performance.
- Real-time or adaptive tuning possible by adjusting gains on each mode.
- Future work to involve implementation on a true Advanced LIGO interferometer.

Backups



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Five Pendulum Designs



LIGO

LIGOBackups: Optical Sensor ElectroMagnet (OSEM)





Birmingham OSEM (BOSEM)



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BOSEM Schematic

Advanced LIGO OSEM (AOSEM) - modified iLIGO OSEM

> Magnet Types (M0900034) • BOSEM – 10 X 10 mm, NdFeB , SmCo

> > 10 X 5 mm, NdFeB, SmCo

• AOSEM – 2 X 3 mm, SmCo

2 X 6 mm, SmCo

2 X 0.5 mm, SmCo ₂₅

Backups: Quadruple Suspension ESD





The electrostatic drive (ESD) acts directly on the test ITM and ETM test masses.

- ± 400 V (ΔV 800 V) ≈ 100 μN
- Each quadrant has an independent control channel
 Common bias channel over all quadrants

Backups: Quadruple Suspension



MIT monolithic quad in BSC

June 2010