



Searching for Gravitational Waves

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Outline

- 1 Gravitational Waves
 - Crash Course in Gravitational Wave Physics
 - Gravitational-Wave Sources & Signals
 - Gravitational-Wave Observations & Detectors
- 2 Upper Limit Results from Initial Detectors
 - Gamma-Ray Bursts
 - Known Pulsars
 - Gravitational-Wave Backgrounds
- 3 Prospects for Detections with Advanced Detectors
 - Compact Binaries
 - Unknown Neutron Stars
 - Accreting Neutron Stars



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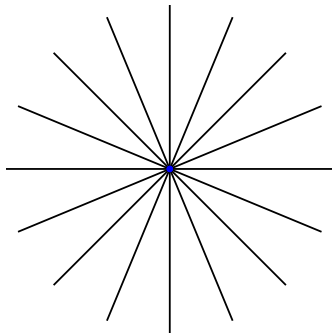


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Action at a Distance

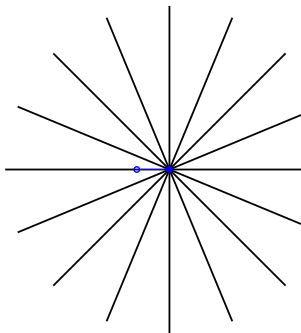
- Newtonian gravity:
mass generates
gravitational field
- Lines of force point
towards object





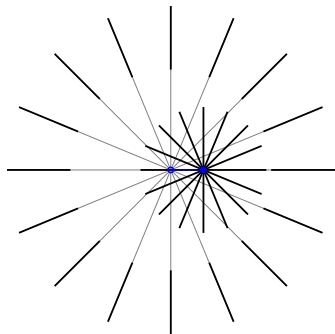
Issues with Causality

- Move object; Newton says:
lines point to new location
- Relativity says:
can't communicate
faster than light
to avoid paradoxes
- You could send me
supraluminal messages
via grav field



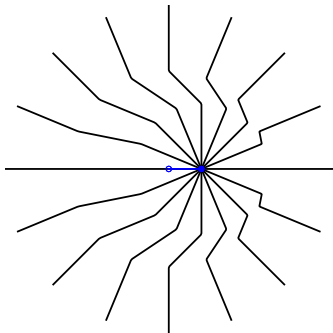
Gravitational Speed Limit

- If I'm 10 light years away, I can't know you moved the object 6 years ago
- Far away, gravitational field lines have to point to old location of the object



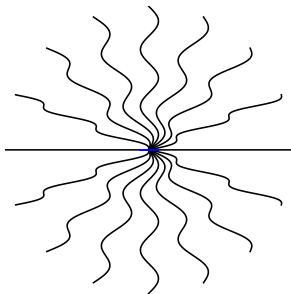
Gravitational Shock Wave

- Sudden motion (acceleration) of object generates gravitational shock wave expanding at speed of light

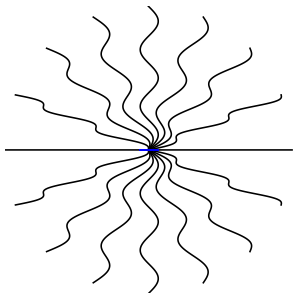
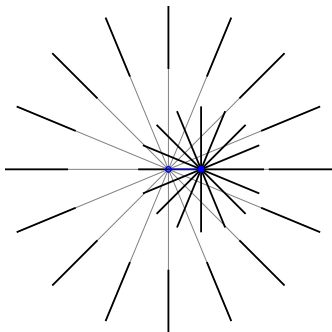


Ripples in the Gravitational Field

- Move object back & forth
→ gravitational wave
- Same argument applies to electricity:
 - can derive magnetism as relativistic effect
 - accelerating charges generate electromagnetic waves propagating @ speed of light



Gravity + Causality = Gravitational Waves



- In **Newtonian gravity**, force dep on distance btwn objects
- If massive object suddenly moved, grav field **at a distance** would change **instantaneously**
- In relativity, **no** signal can travel faster than light
 → time-dep grav fields must propagate like light waves

Gravity as Geometry

- Minkowski Spacetime (Special Relativity):
 Invariant spacetime interval (all inertial observers agree):

$$\begin{aligned}
 ds^2 &= -c^2(dt)^2 + (dx)^2 + (dy)^2 + (dz)^2 \\
 &= \begin{pmatrix} dt \\ dx \\ dy \\ dz \end{pmatrix}^{\text{tr}} \begin{pmatrix} -c^2 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} dt \\ dx \\ dy \\ dz \end{pmatrix} = \sum_{\mu=0}^3 \sum_{\nu=0}^3 \eta_{\mu\nu} dx^\mu dx^\nu
 \end{aligned}$$

- General Spacetime:

$$ds^2 = \begin{pmatrix} dx^0 \\ dx^1 \\ dx^2 \\ dx^3 \end{pmatrix}^{\text{tr}} \begin{pmatrix} g_{00} & g_{01} & g_{02} & g_{03} \\ g_{10} & g_{11} & g_{12} & g_{13} \\ g_{20} & g_{21} & g_{22} & g_{23} \\ g_{30} & g_{31} & g_{32} & g_{33} \end{pmatrix} \begin{pmatrix} dx^0 \\ dx^1 \\ dx^2 \\ dx^3 \end{pmatrix} = \sum_{\mu=0}^3 \sum_{\nu=0}^3 g_{\mu\nu} dx^\mu dx^\nu$$

Metric tensor $\{g_{\mu\nu}(\{x^\lambda\})\}$ determined by masses via Einstein's equations. (10 non-linear PDEs!)

Gravitational Wave as Metric Perturbation

- For GW propagation & detection, work to 1st order in $h_{\mu\nu} \equiv$ difference btwn actual metric $g_{\mu\nu}$ & flat metric $\eta_{\mu\nu}$:

$$g_{\mu\nu} = \eta_{\mu\nu} + h_{\mu\nu}$$

($h_{\mu\nu}$ “small” in weak-field regime, e.g. for GW detection)

- $h_{\mu\nu}$ is like electromagnetic potentials φ , \vec{A} ;
small coordinate changes like gauge transformations
- Convenient choice of gauge is **transverse-traceless**:
In this gauge:
 - Test particles w/constant coords are **freely falling**
 - Vacuum Einstein eqns \implies wave equation for $\{h_{ij}\}$:

$$\left(-\frac{1}{c^2} \frac{\partial^2}{\partial t^2} + \nabla^2 \right) h_{ij} = 0$$



Gravitational Wave Polarization States

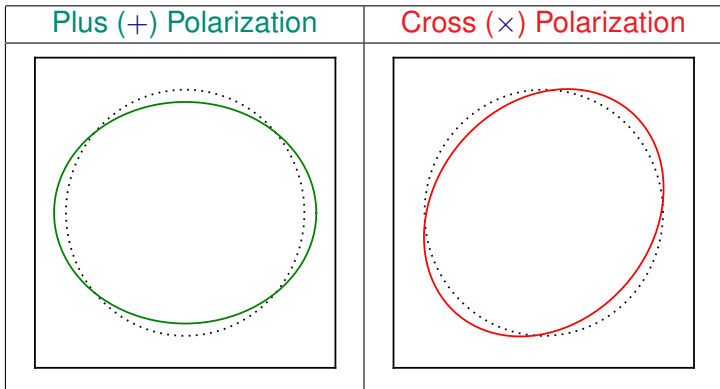
Far from source, GW looks like plane wave prop along \vec{k}
TT conditions mean, in convenient basis,

$$\{k_i\} \equiv \mathbf{k} = \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} \quad \{h_{ij}\} \equiv \mathbf{h} = \begin{pmatrix} h_+ & h_\times & 0 \\ h_\times & -h_+ & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

where $h_+ \left(t - \frac{x^3}{c}\right)$ and $h_\times \left(t - \frac{x^3}{c}\right)$ are components
in “plus” and “cross” polarization states

Effects of Gravitational Wave

Fluctuating geom changes distances btwn particles in free-fall:

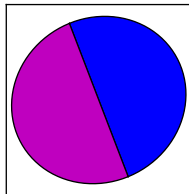
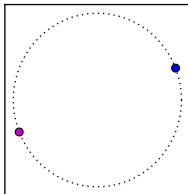


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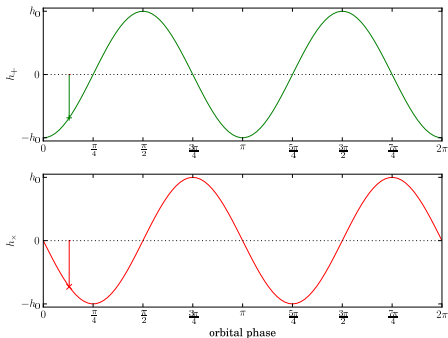
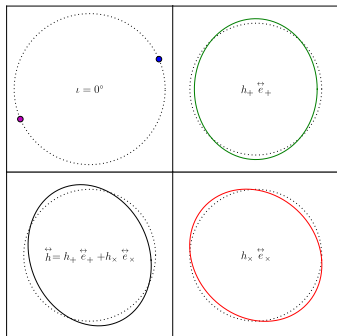
Generation of Gravitational Waves

- EM waves generated by **moving/oscillating** charges
- GW generated by **moving/oscillating** masses
- Lowest **multipole** is **quadrupole**
- Different types of signals:
 - Burst (transient, unmodelled)
 - Stochastic (long-lived, unmodelled)
 - **Binary coalescence** (transient, modelled)
 - **Periodic** (long-lived, modelled)



Gravitational Waves from Binary Orbit

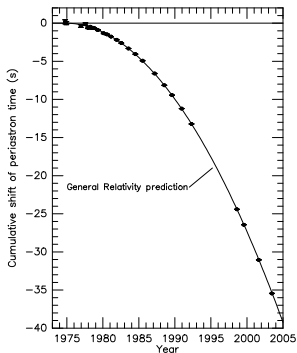
- Orbital motion \rightarrow oscillating quadrupole moment \rightarrow GWs





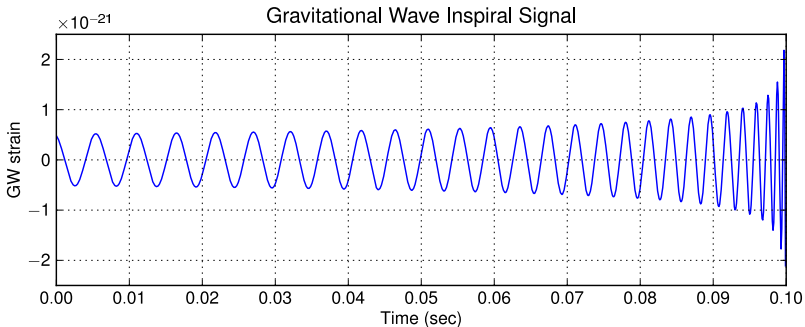
Gravitational Waves from Binary Orbit

- Orbital motion \rightarrow oscillating quadrupole moment \rightarrow GWs
- GW emission removes energy \rightarrow orbit gets tighter
 \rightarrow amplitude & freq increase in “chirp”
- Hulse & Taylor saw this evolution in binary pulsar
1993 Nobel Prize



Gravitational Waves from Binary Orbit

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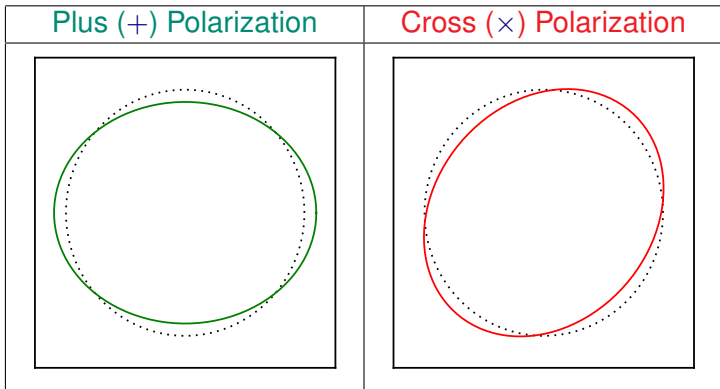


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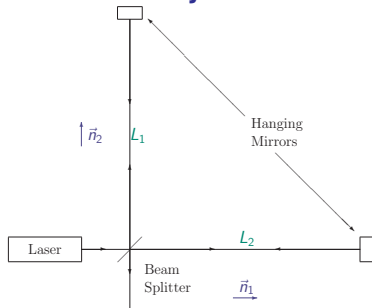
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Fluctuating geom changes distances btwn particles in free-fall:



Measuring GWs w/Laser Interferometry

Interferometry: Measure GW-induced distance changes

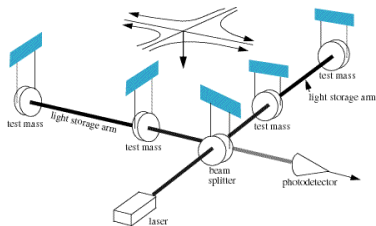


- Measure small change in

$$L_1 - L_2 \approx L_0 \frac{h_{11} - h_{22}}{2} \sim L_0 h_+$$
- Plausible signals: $h \lesssim 10^{-20}$
 → need L_0 very big!
- For LIGO, $L_0 = 4 \text{ km} = 2.5 \text{ mi}$

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Rogues' Gallery of Ground-Based Interferometers



LIGO Hanford (Wash.)



LIGO Livingston (La.)



GEO-600 (Germany)



Virgo (Italy)

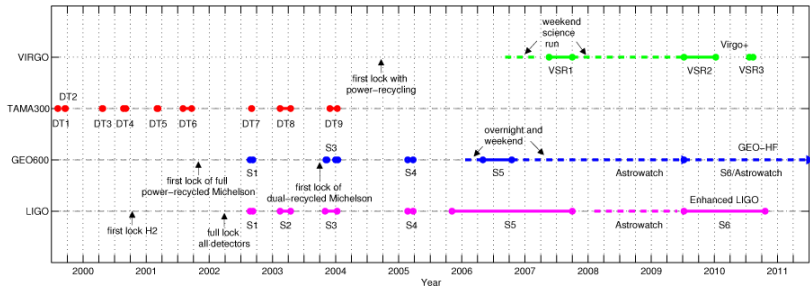


Initial Gravitational Wave Detector Network

- “1st generation” ground-based interferometric GW detectors (kilometer scale):
 - TAMA 300 (Tokyo, Japan) first online, late 90s; now offline
 - LSC (LIGO Scientific Collaboration) detectors conducting science runs since 2002
 - LIGO Hanford (4km H1 & 2km H2)
 - LIGO Livingston (4km L1)
 - GEO-600 (600m G1)
 - Virgo (3km V1) started science runs in 2007
 - LSC-Virgo long joint runs @ design sensitivity 2005-2010
- LIGO and Virgo being upgraded to 2nd generation “advanced” detectors (10× improvement in sensitivity)
- GEO-600 remains operational in “astrowatch” mode in case there’s a nearby supernova



Initial Gravitational Wave Detector Network



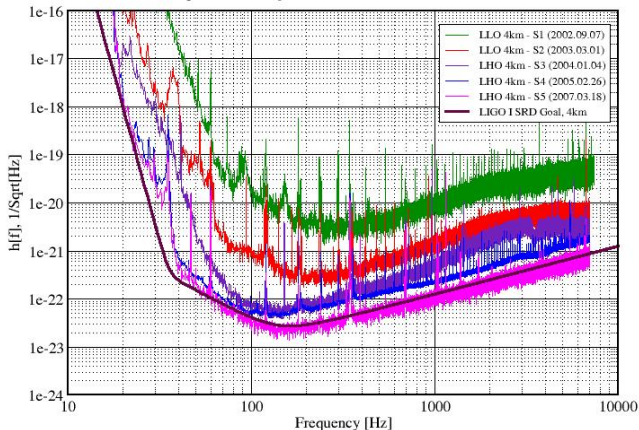
Living Reviews in Relativity 14, 5 (2011)



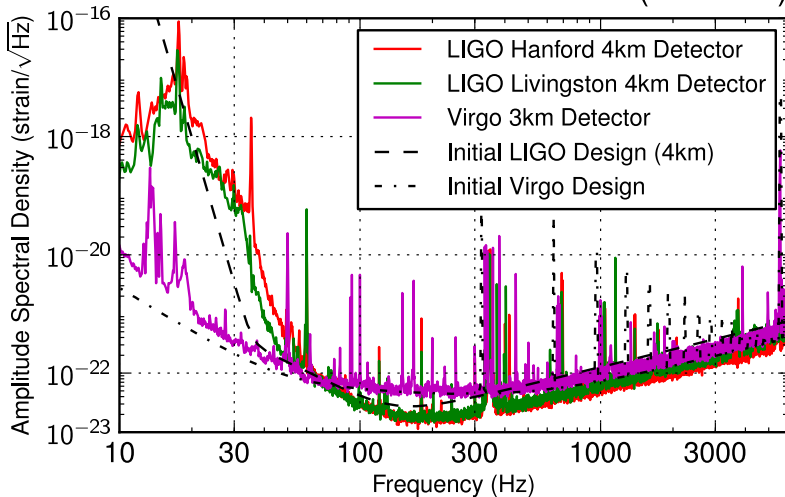
Evolution of LIGO Sensitivity S1-S5

Best Strain Sensivities for the LIGO Interferometers

Comparisons among S1 - S5 Runs LIGO-G060009-03-Z



S6/VSR2 Best Strain Sensivities (PRELIM)





Advanced Gravitational Wave Detector Network

- “2nd generation” ground-based interferometric GW detectors:
 - Adv LIGO expected to take science data from 2015
4km detectors in Livingston, La. & Hanford, Wa.
 - Advanced Virgo should be on comparable timescale
 - KAGRA (cryogenic detector in Kamioka mine, Japan)
uses 2.5-generation technology
 - Third advanced LIGO detector (4km)
may be installed in India, taking data c.2019+
Big payoff for sky localization via triangulation
- Planning for 3rd generation already underway:
 - Einstein Telescope in Europe
 - USA 3G plans still under development



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Results of Initial Detector Observations

- 70+ Observational papers from initial LIGO/Virgo/GEO:
<https://www.lsc-group.phys.uwm.edu/ppcomm/Papers.html>
- No detections (although some analyses still trickling out)
- Assortment of null results and upper limits
- As sensitivity improves, some of these results give new information to complement astronomical observations:
“Multi-Messenger Astronomy”
- Some highlights . . .

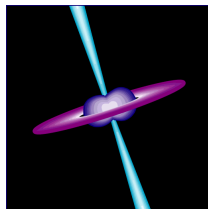
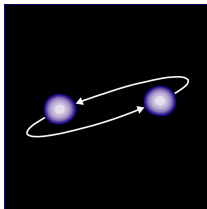


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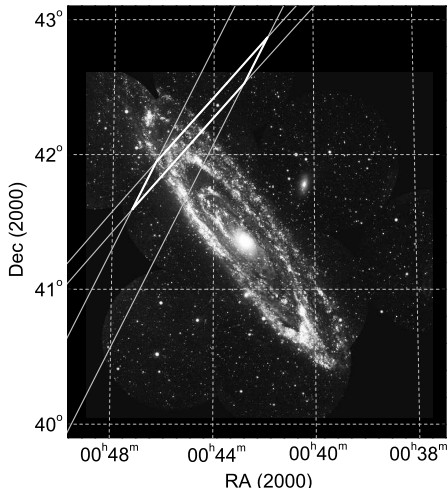
Gravitational Waves from Gamma-Ray Bursts



- GRBs are bursts of high energy photons observed by orbiting satellites like [Swift](#) and [Fermi](#)
- One possible source is the merger of a neutron star w/another neutron star or a black hole
- Search for the GWs emitted by the neutron star as it inspirals; search is “triggered” by the GRB, so can compare data at GRB time to data at other times

GRB070201

- 2007 Feb 1: short GRB whose **error box** overlapped spiral arm of **M31** (770 kpc* away)
- LHO **4 km** & **2 km** detectors operating & sensitive to inspiral out to **35.7** & **15.3 Mpc**
- No GW seen; **rule out** binary progenitor in M31 w/ > **99%** conf
- *ApJ* **681**, 1419 (2008)



Similar result for GRB051103 & M81; *ApJ* **755**, 2 (2012)

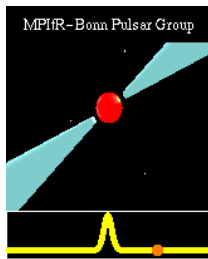
* 1 parsec (pc) = 3.26 light years



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Searching for Known Pulsars



- Pulsar=rapidly rotating neutron star emitting radio or X-ray “pulses” as it spins (pulse comes when magnetic pole points at Earth)
- Pulsars spin down mostly due to drag of magnetic field through nebula
- If pulsar has small bump, will emit GWs
- Can search for periodic GW signal modulated by Doppler effect as Earth rotates & orbits Sun
- Parameters like freq, sky position, etc known from pulsar
- Spindown produces **indirect upper limit**
 - GW emission above limit → more spindown than seen
 - Pulsars w/rapid spindown have “more room” for GW
 - LIGO/Virgo have **surpassed spindown** limit for **Crab** & **Vela**

Crab Pulsar Upper Limit



- Pulsar in Crab Nebula
- Created by SN 1054
- ~ 2 kpc away
- $f_{\text{rot}} = 29.7$ Hz
- $f_{\text{gw}} = 59.4$ Hz

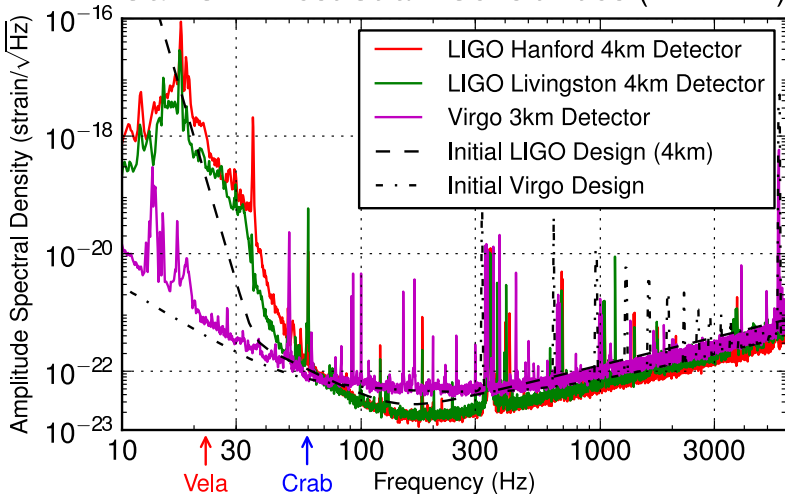
Image credit: [Hubble](#)/[Chandra](#)

- Initial LIGO (S5) upper limit beats spindown limit
- Abbott et al (LSC) [ApJL 683, L45 \(2008\)](#)
- Abbott et al (LSC & Virgo) + Bégin et al [ApJ 713, 671 \(2010\)](#)
- No more than 2% of spindown energy loss can be in GW

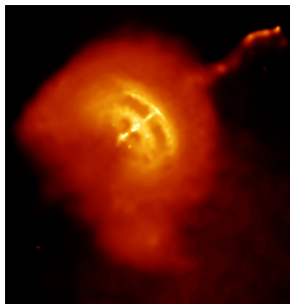


Initial Virgo Targets the Vela Pulsar

S6/VSR2 Best Strain Sensivities (PRELIM)



Vela Pulsar Upper Limit



- Pulsar in Vela SN remnant
- Created $\sim 12,000$ years ago
- ~ 300 pc away
- $f_{\text{rot}} = 11.2$ Hz
- $f_{\text{gw}} = 22.4$ Hz

Image credit: **Chandra**

- GW frequency below initial LIGO “seismic wall”
- Virgo has better low-frequency sensitivity
- VSR2 upper limit beats spindown limit
- No more than 10% of spindown energy loss can be in GW

Abadie et al (LSC & Virgo) + Buchner et al *ApJ* **737**, 93 (2011)



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Searching for a Stochastic Background

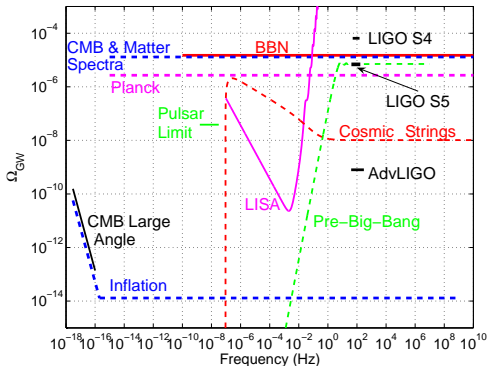
- Expect a random (stochastic) background of GWs left over from Big Bang (like the cosmic microwave background radiation) or from confusions of many faint sources
- Need to find a random signal in random noise!
- Noisy data from GW Detector:
 $x(t) = n(t) + h(t) = n(t) + \overset{\leftrightarrow}{h}(t) : \overset{\leftrightarrow}{d}$
- Look for correlations between detectors

$$\langle x_1 x_2 \rangle = \overbrace{\langle n_1 n_2 \rangle}^{\text{avgto0}} + \overbrace{\langle n_1 h_2 \rangle}^{\text{avgto0}} + \overbrace{\langle h_1 n_2 \rangle}^{\text{avgto0}} + \langle h_1 h_2 \rangle$$

- Details of expected correlation will depend on sky distribution of background

Allen & Romano *PRD* **59**, 102001 (1999)

Isotropic Stochastic Background Limit



$$S5 \text{ limit } \Omega_{\text{gw}}(f) < 6.9 \times 10^{-6} \left(\frac{72 \text{ km/s/Mpc}}{H_0} \right)^2$$
 [Abbott et al (LSC & Virgo) *Nature* **460**, 990 (2009)]
 surpasses indirect limit from Big-Bang Nucleosynthesis



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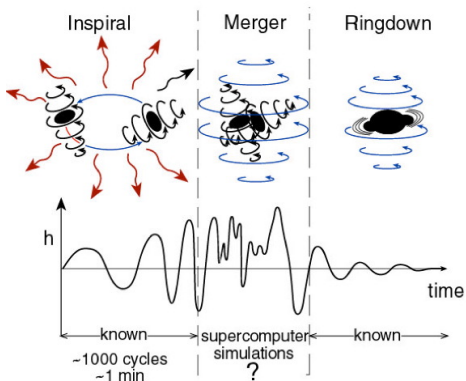


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Template Waveforms for Binary Coalescence

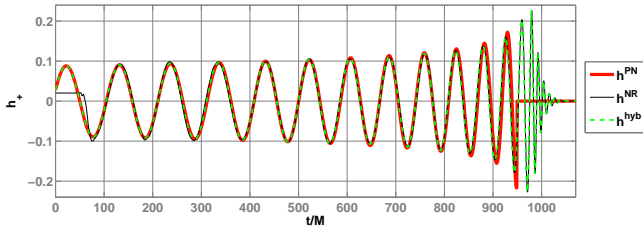
- Inspiralling binaries produce **well-modelled** GW signals;
Search with **pattern-match filter**
- Compact object binary coalescence consists of
inspiral / **plunge** / **merger** / **ringdown**



Cartoon by Kip Thorne

Template Waveforms for Binary Coalescence

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 Search with **pattern-match filter**
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Ajith et al, *CQG* **24**, S689 (2007)



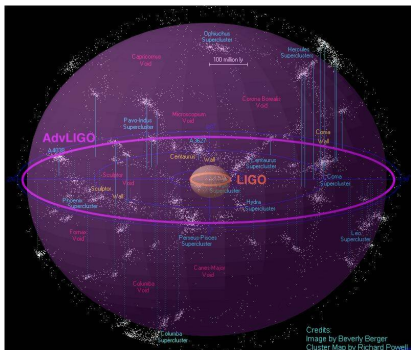
Template Waveforms for Binary Coalescence

- Compact object binary coalescence consists of **inspiral** / **plunge** / **merger** / **ringdown**
- For first part of **inspiral**, orbits **not too relativistic**
can expand in powers of $\frac{v}{c}$ \rightarrow **post-Newtonian** methods
Can estimate **orb vel** from Kepler's 3rd law: $v \approx (\pi GMf)^{1/3}$
 - **Low Mass** \rightarrow plunge @ **high freq**
 $1.4M_{\odot}/1.4M_{\odot}$ NS/NS binary has $v \approx 0.3c$ @ 800 Hz;
PN OK in LIGO band
 - **High Mass** \rightarrow plunge @ **low freq**
 $10M_{\odot}/10M_{\odot}$ BH/BH binary has $v \approx 0.4c$ @ 200 Hz;
merges in LIGO band
- Different **template families** used for different **mass ranges**

Expected Event Rates w/Advanced Detectors

CQG 27, 173001 (2010)

- Advanced detectors should see NS binary inspiral up to 400 Mpc & BH binary coalescence up to 2 Gpc away
- \implies Expect between a few and hundreds of events/year





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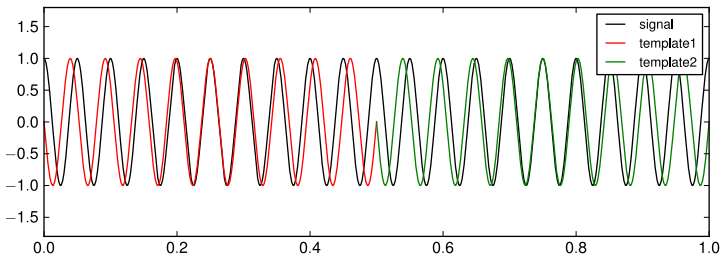
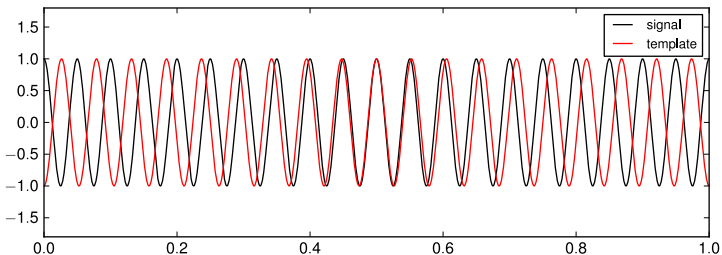
Searching for Unknown Neutron Stars

- Look for GWs from NSs not seen as pulsars
- Since freq, spindown, sky position, etc unknown, need to try different guesses in matched filter “template bank”
- Need to make bank dense enough so that true signal close to some template
- The longer you observe, the finer the needed resolution in frequency, sky position, etc
E.g, for all-sky search with one spindown,

$$N_{\text{tplts}} \sim \frac{1}{\Delta f} \frac{1}{\Delta \dot{f}} \frac{1}{\Delta \text{sky}} \sim T \cdot T^2 \cdot (fT)^2 \propto T^5$$

- Need to combine shorter coherent searches semicoherently

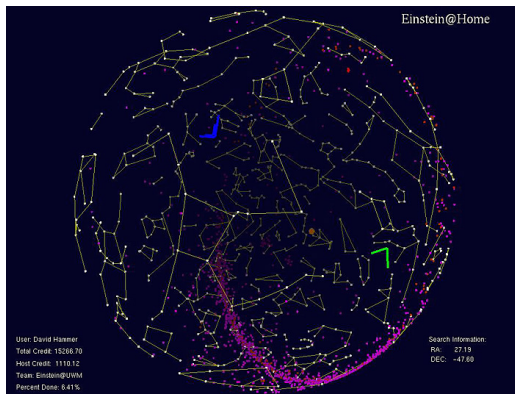
Coherent vs Semicoherent Searches





Searching for Unknown NSs: Einstein@Home

Semicoherent methods needed to handle phase param space;
Increase computing resources by enlisting volunteers
Distributed using BOINC & run as screensaver



<http://www.einsteinathome.org/>



Outline

- 1 Gravitational Waves
 - Crash Course in Gravitational Wave Physics
 - Gravitational-Wave Sources & Signals
 - Gravitational-Wave Observations & Detectors
- 2 Upper Limit Results from Initial Detectors
 - Gamma-Ray Bursts
 - Known Pulsars
 - Gravitational-Wave Backgrounds
- 3 Prospects for Detections with Advanced Detectors
 - Compact Binaries
 - Unknown Neutron Stars
 - **Accreting Neutron Stars**

Gravitational Waves from Low-Mass X-Ray Binaries



- LMXB: compact object (neutron star or black hole) in binary orbit w/companion star
- If NS, accretion from companion provides “hot spot”; rotating non-axisymmetric NS emits gravitational waves
- Bildsten *ApJL* **501**, L89 (1998)
 suggested GW spindown may balance accretion spinup;
 GW strength can be estimated from X-ray flux
- Torque balance would give \approx constant GW freq
- Signal at solar system modulated by binary orbit



Brightest LMXB: Scorpius X-1

- Scorpius X-1
 - $1.4M_{\odot}$ NS w/ $0.4M_{\odot}$ companion
 - **unknown params** are f_0 , $a \sin i$, orbital phase
- LSC/Virgo searches for **Scorpius X-1**:
 - **Coherent \mathcal{F} -stat search** w/6 hr of S2 data
Abbott et al (LSC) *PRD* **76**, 082001 (2007)
 - **Directed stochastic (“radiometer”) search** (unmodelled)
Abbott et al (LSC) *PRD* **76**, 082003 (2007)
Abbott et al (LSC) [arXiv:1109.1809](https://arxiv.org/abs/1109.1809)
- Proposed directed search methods:
 - Look for **comb of lines** produced by orbital modulation
Messenger & Woan, *CQG* **24**, 469 (2007)
 - **Cross-correlation** specialized to periodic signal
Dhurandhar et al *PRD* **77**, 082001 (2008)
- Promising source for **Advanced Detectors**



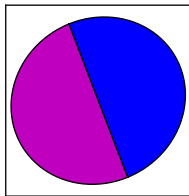
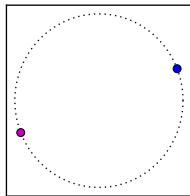
Resources for Further Investigation

- LIGO Science Pages:
<http://www.ligo.org/science/overview.php>
- List of LSC and Virgo papers:
<https://www.lsc-group.phys.uwm.edu/ppcomm/Papers.html>
Includes links to free versions of papers on [arXiv.org](http://arxiv.org)
- Summaries of recent LIGO science publications:
<http://www.ligo.org/science/outreach.php>
- LIGO data releases:
<http://www.ligo.org/science/data-releases.php>

EXTRA SLIDES

Multipole Expansion for Gravitational Radiation

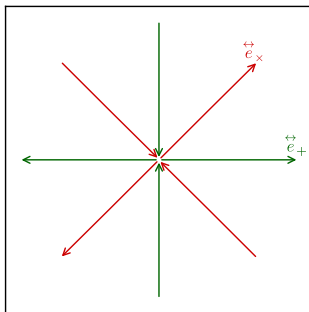
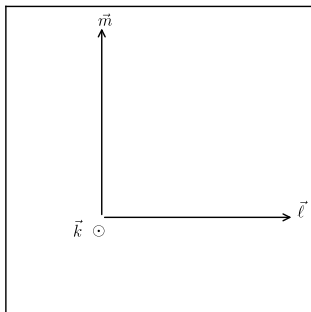
- **“Electric Dipole”?**
 No, “dipole moment” $\int \vec{r} dm \propto$ ctr of mass
 COM can’t oscillate (also no **negative “charge”** in GR)
- **“Magnetic Dipole”?** No, “mag moment”
 $\frac{1}{2} \int \vec{r} \times \vec{v} dm \propto$ spin, another conserved quantity
- **“Electric Quadrupole”?** Yes! E.g., orbiting/rotating system w/ang vel Ω has GW frequency $f_{\text{gw}} = 2\frac{\Omega}{2\pi}$



The Polarization Basis

- wave propagating along \vec{k} ;
 construct $\vec{e}_{+,x}$ from \perp unit vectors \vec{l} & \vec{m} :

$$\vec{e}_+ = \vec{l} \otimes \vec{l} - \vec{m} \otimes \vec{m} \quad \vec{e}_x = \vec{l} \otimes \vec{m} + \vec{m} \otimes \vec{l}$$

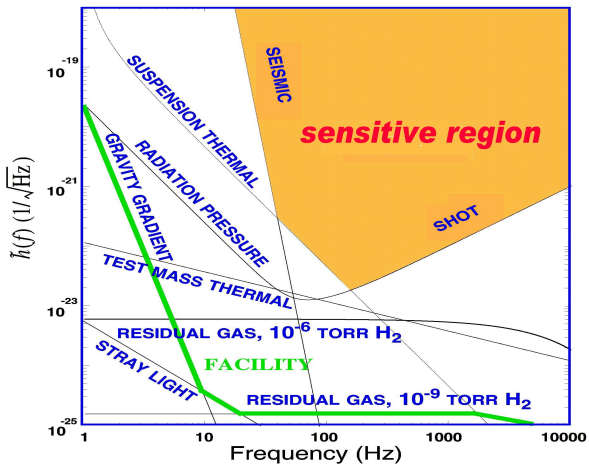


Some Sources of Gravitational Waves

Useful to divide up by frequency band:

- **Very Low Freq** ($10^{-9} \text{ Hz} \lesssim f_{\text{gw}} \lesssim 10^{-7} \text{ Hz}$)
- **Low Freq** ($10^{-3} \text{ Hz} \lesssim f_{\text{gw}} \lesssim 10^{-1} \text{ Hz}$)
- **High Freq** ($10^1 \text{ Hz} \lesssim f_{\text{gw}} \lesssim 10^3 \text{ Hz}$)
- **Binary coalescence (inspiral+merger+ringdown):**
 - **Supermassive black hole binary**
 - **extreme mass ratio (stellar mass + SMBH)**
 - **Stellar mass BH and/or neutron star**
- **Galactic white dwarf binary orbit (continuous source)**
- **Rotating neutron star (pulsar, LMXB, etc)**
- **Supernova, Soft Gamma Repeater**
- **Cosmological background**
(primordial, phase transitions, cosmic superstrings, etc)
- **SMBH flyby**

LIGO's Sensitive Frequency Band



S5/VSR1 Best Strain Sensivities

