



Optical Simulation vs Reality at LLO

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- Introduction

- Arm loss

- » Loss by COC data and modeling
- » Measured loss to total loss
- » Effect of LMA coating

- Arm modes

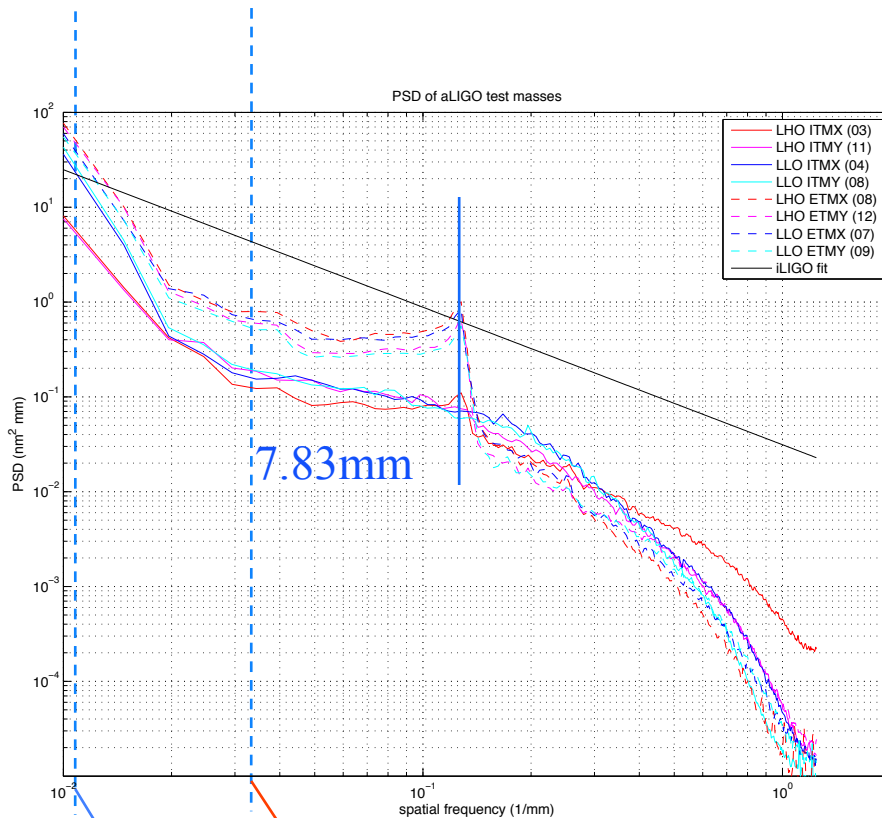
- » Effective RoC and locations of HOM peaks

- Contrast Defect

- » 400ppm measurement vs 300ppm model
 - Various sources of CD, what's missing?
- » ITMY lens and transmission maps, BS maps etc

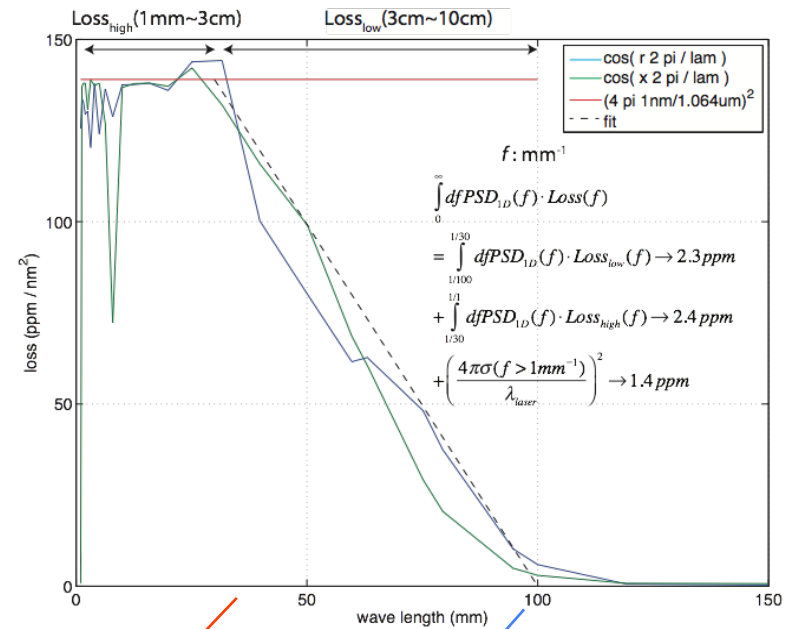


aLIGO optics scattering loss by wavelength



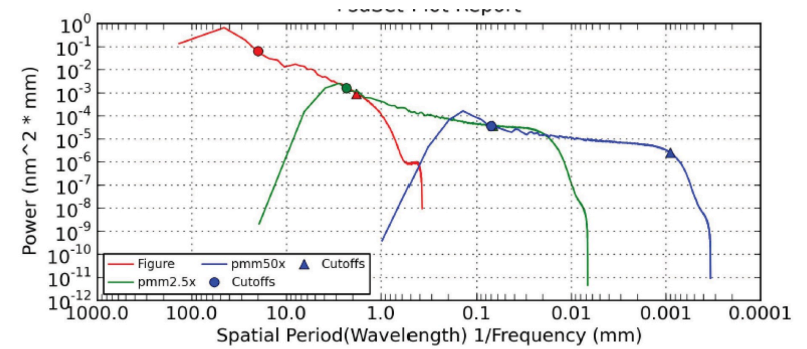
$$\theta = \frac{1.7\text{cm}}{4\text{km}}$$

$$\frac{\lambda}{2.5\text{cm}} = \frac{1.7\text{cm}}{4\text{km}}$$





COC data and modeling

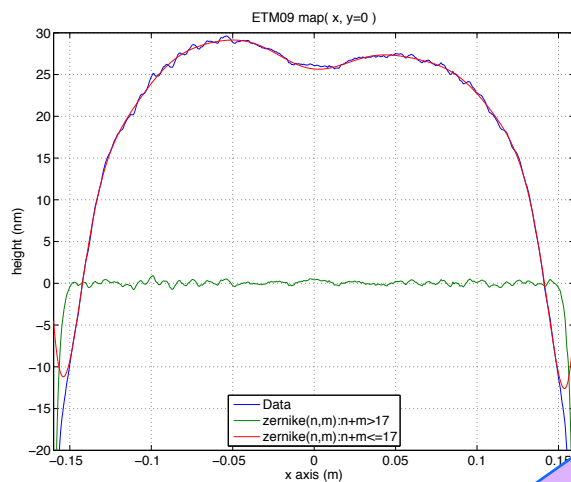


	Spatial resolution	coverage	Main use
Phase map	> 1mm	$< 2 \times 10^{-4}$ rad, < 1m at 4km	Field in cavity and near the outer edge of mirror, cavity mode
PSD, RMS	1 μ m ~ a few mm by PMM, + phase map	~ large angle	Characterization of continuous structure, field scattered at large angle
Integrating sphere	fraction of mm	> 5 degree	Total scattering to all angle, effects of non contiguous structures captured. Hole at forward is covered by others.

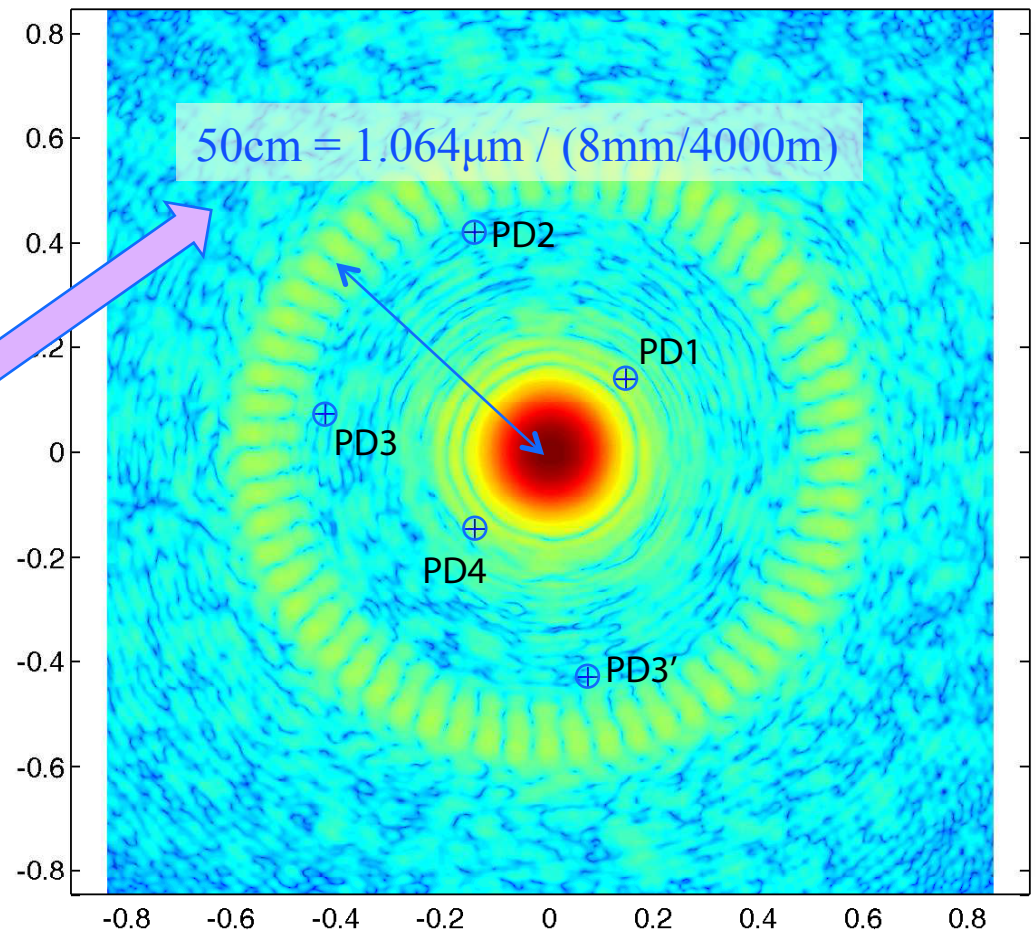
COC data (characteristics of mirror) +
 appr. Maxwell eq. with rigorous boundary cond.
 \Rightarrow IFO observable

Details of ETM09 spiral effect

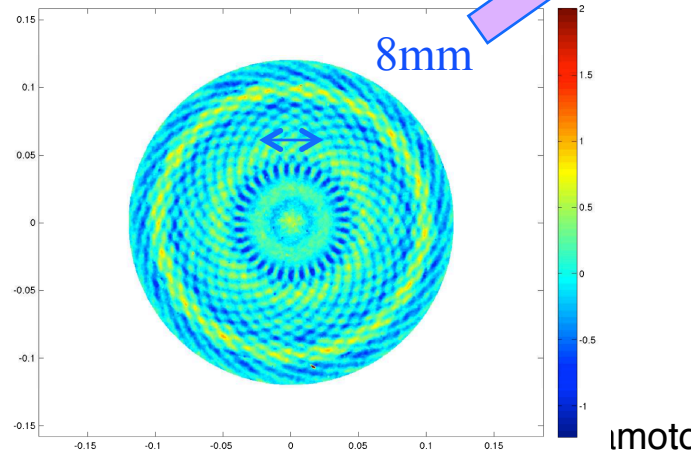
ETM09 map



Field going to ITM



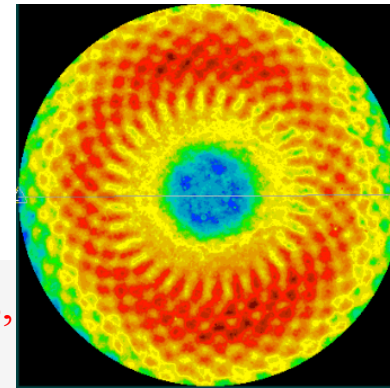
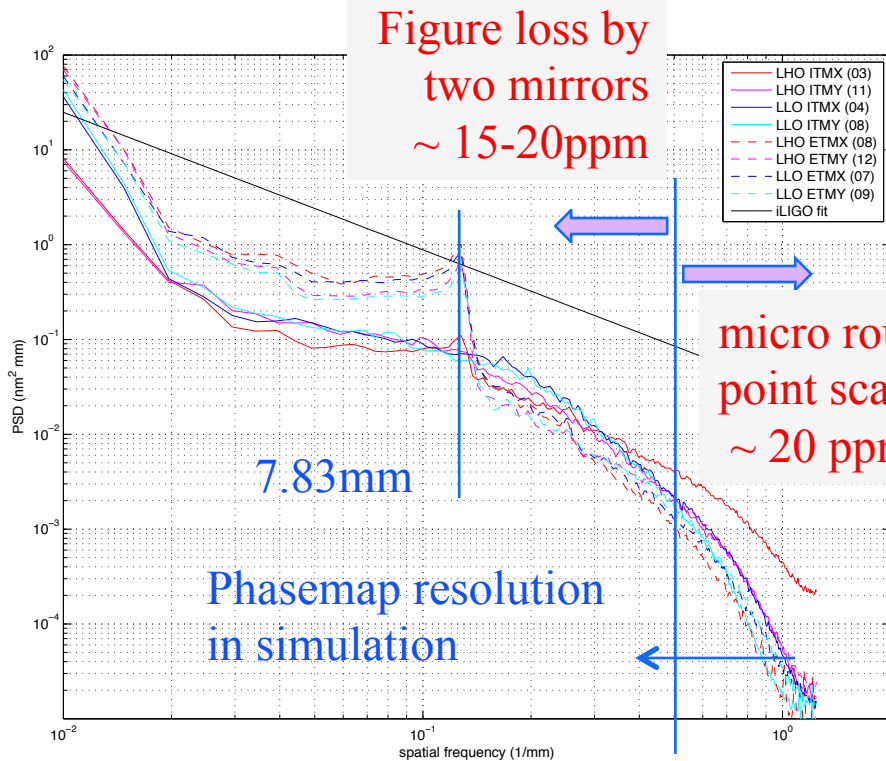
Spiral component



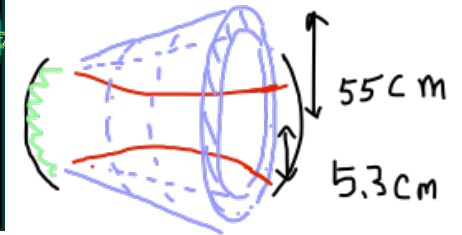
Real PD diameter is $\frac{1}{4}$ of \circ



Noise injection by the spiral pattern on test mass coatings

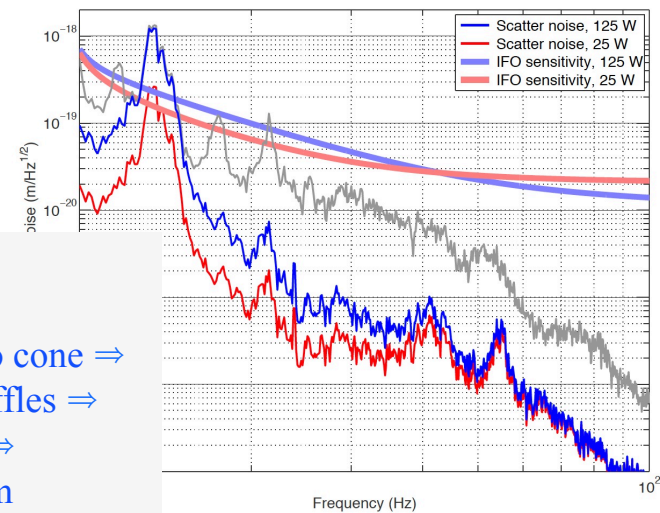


ETM07 map



main beam ⇒
ETM reflection ⇒
larger angle scattering into cone ⇒
reflected by beam tube baffles ⇒
back scattered into ETM ⇒
merged into the main beam

T1300354 by PF, HY

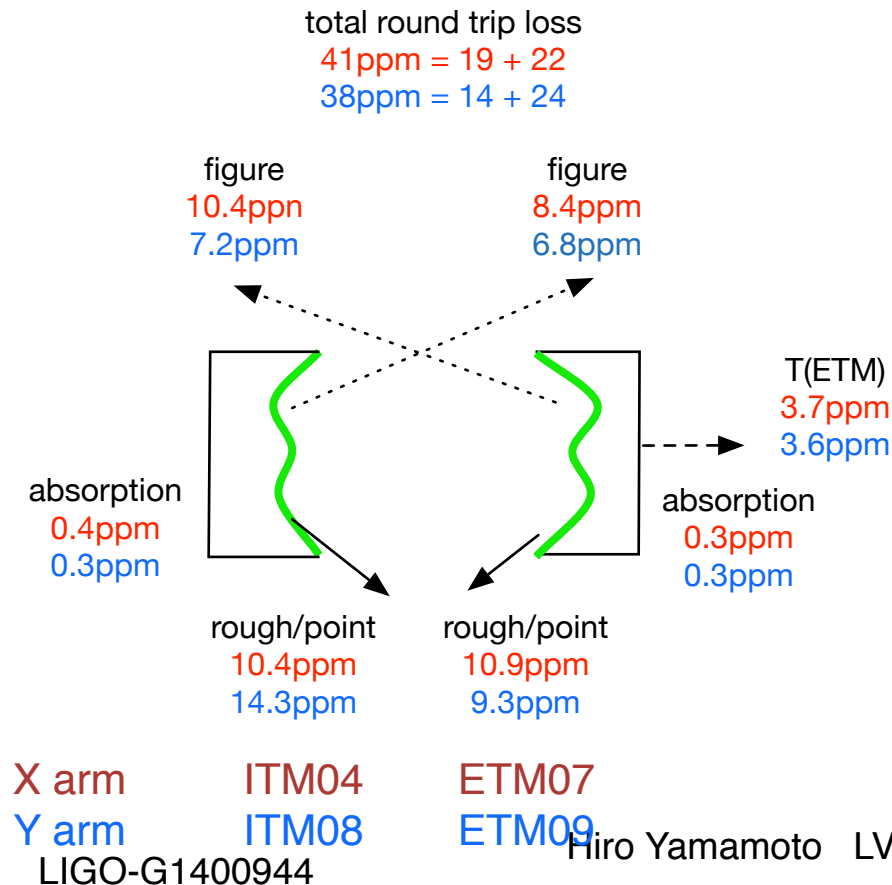




Loss :

measurement vs model with COC data

Phasemap and Caltech/LMA scattering loss measurements

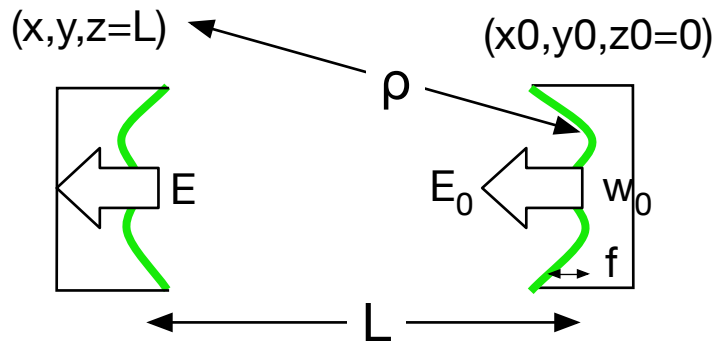


- alog13414 ETMY scattering
 - » Total : 36ppm
 - » Point scattering : 18ppm
- alog13769 Best round trip loss 85ppm
 - » Extra 30-40ppm, where???
- COC data + Model
 - » Round trip loss error < 14ppm
 - » Integrated scattering
 - 7.5ppm by LMA
 - 9.3ppm by Caltech
 - » Zygo rms \Rightarrow loss(<1mm) < 1ppm
 - » PSD \Rightarrow loss(<5mm) < 1ppm



Analytic formula in the forward region

Huygen's integral with Fresnel appr.



$$E(x, y, z) \equiv \frac{i}{\lambda} \iint dx_0 dy_0 E_0(x_0, y_0, z_0) \frac{\exp(-ik\rho)}{\rho} \cos\theta = F_0 + dF$$

$$\Delta x = x - x_0, \Delta y = y - y_0, L = z - z_0, k = 2\pi / \lambda$$

$$\rho = \sqrt{\Delta x^2 + \Delta y^2 + L^2}, \cos\theta = \frac{L}{\rho}$$

$$dF(x, y, z) \approx \sqrt{\frac{2}{\pi}} \frac{1}{w_0} \frac{i}{L \cdot \lambda} \iint dx_0 dy_0 2ikf(x_0, y_0) \exp(-ik \frac{\Delta x^2 + \Delta y^2}{2L}) \exp(-\frac{x_0^2 + y_0^2}{w_0^2}) \quad \text{small aberration}$$

$$\approx \sqrt{\frac{2}{\pi}} \frac{1}{w_0} \frac{i}{L \cdot \lambda} \exp(-ik \frac{x^2 + y^2}{2L}) 2ik \iint dx_0 dy_0 f(x_0, y_0) \exp(ik \frac{x \cdot x_0 + y \cdot y_0}{L}) \quad \text{Fresnel approx}$$

Tiny source : $dF \Rightarrow \text{const BRDF} \Rightarrow 2\pi dS / \lambda^2 \times \text{true scattering}$

$$\text{PSD to } dF : |dF[x, y, z]|^2 = \frac{32\pi^2}{w^2 \lambda^4 L^2} \left| \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \Delta[f_u, f_v] \delta\left[f_u - \frac{x}{\lambda L}, \varepsilon\right] \delta\left[f_v - \frac{y}{\lambda L}, \varepsilon\right] df_u df_v \right|^2$$

Δ : 2D amplitude spectral density, $\varepsilon \sim 1/\text{a few cm}$



Baffle PD capturing ETMY scatter

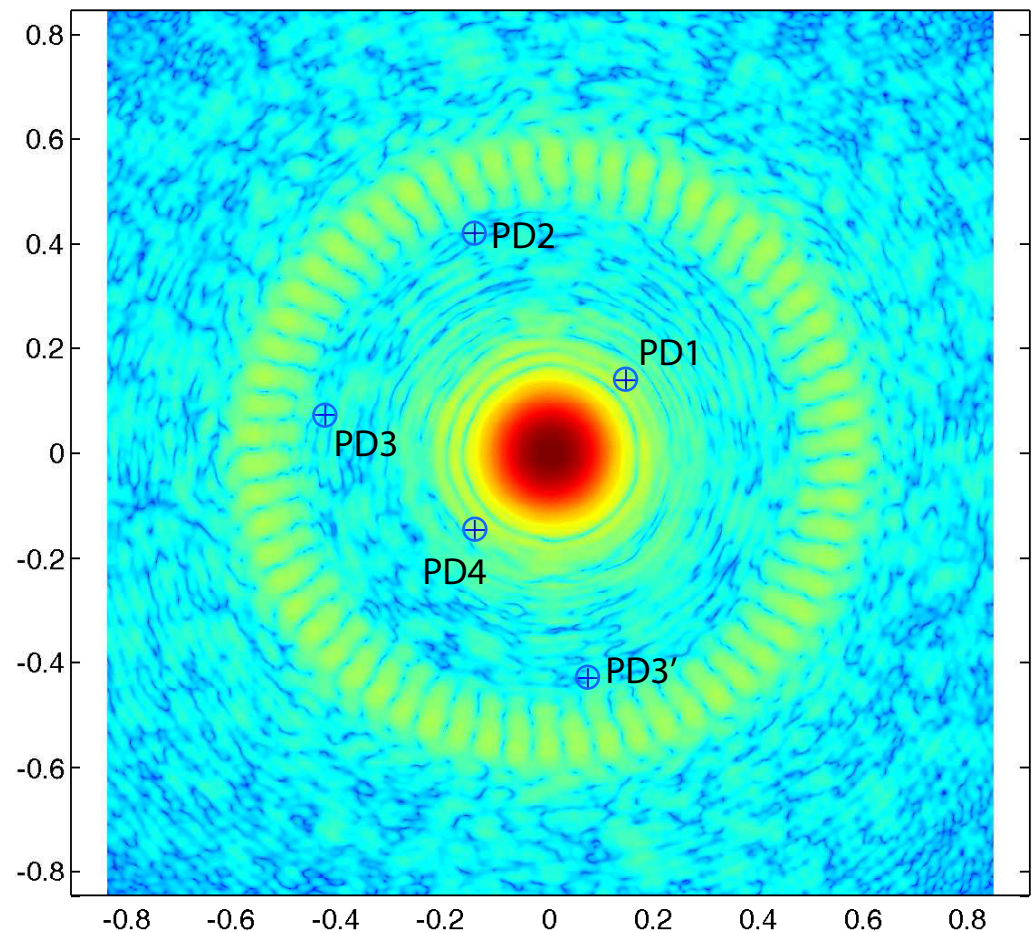
phasemap resolution $\sim 2\text{mm} \Rightarrow$ covers 1m

BRDF on ITMY baffle PD

	PD1	PD2	PD3	PD4
location (mm)	200	438	435	217
data	768	118	48	352
FOGP	863	15	3 (5)	625

$\text{PSD}(f) = 2500 f(m)^{-2} \text{ nm}^2 \text{ mm}$
 $\Rightarrow \text{BRDF} = 20$ (big error) at 45cm
 by using Huygen+Fresnel

Field going to ITM

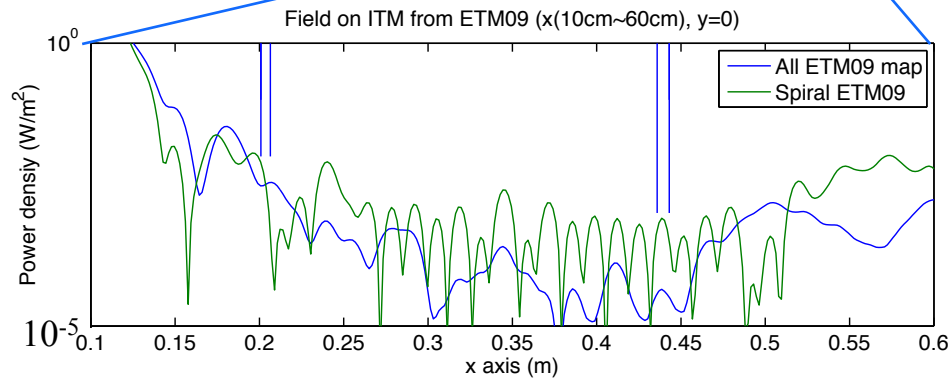
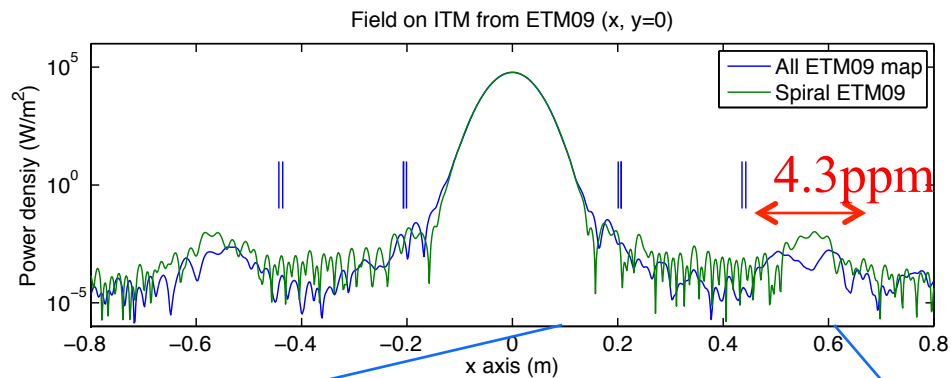
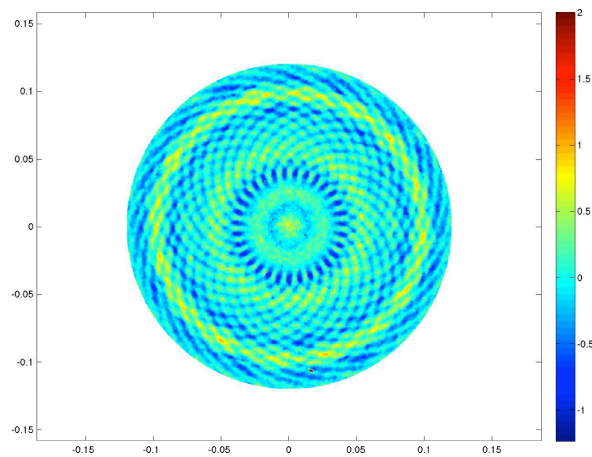
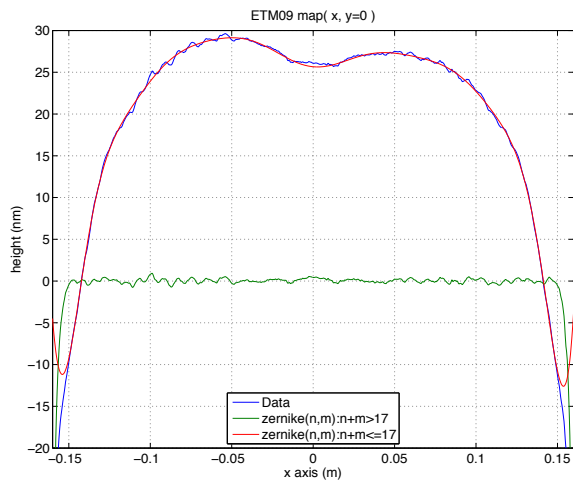


Real PD diameter is $\frac{1}{4}$ of \circ



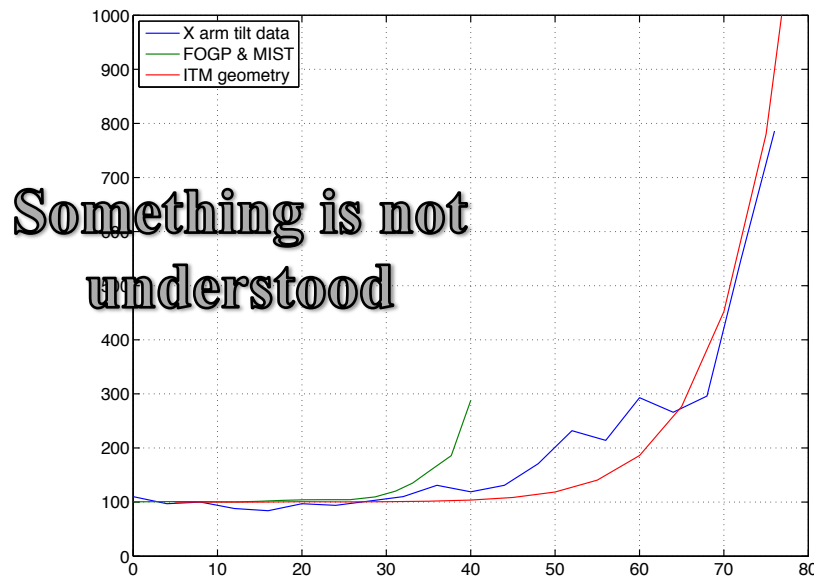
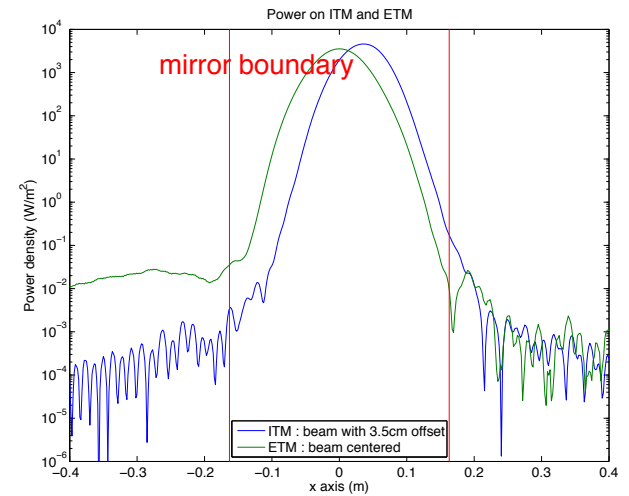
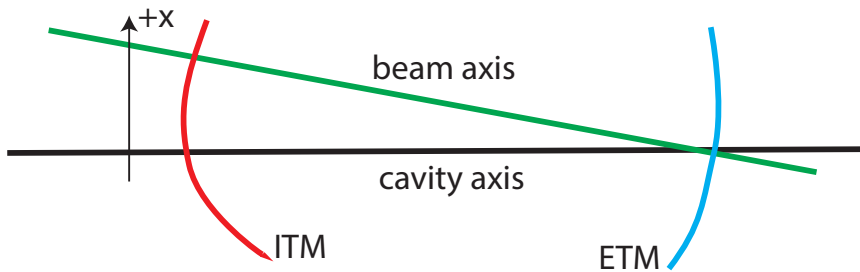
Details of ETM09 spiral effect

PD1,4 edge of central peak, PD 2,3 edge of 50cm ring

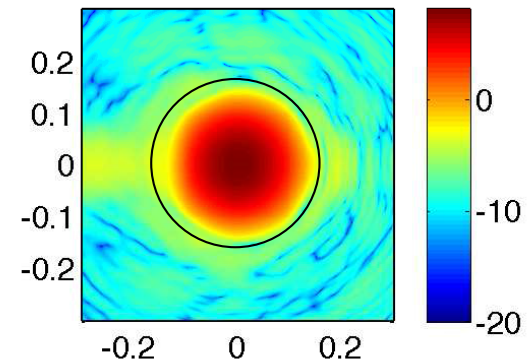
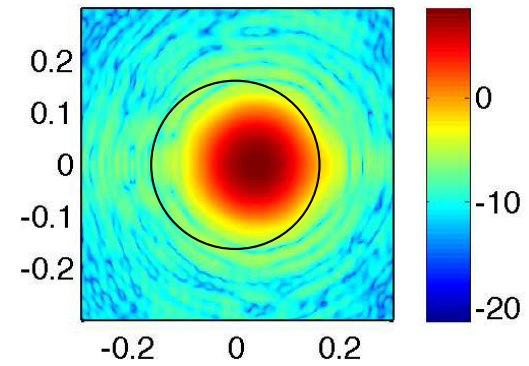




Loss vs ITM tilt alog14171

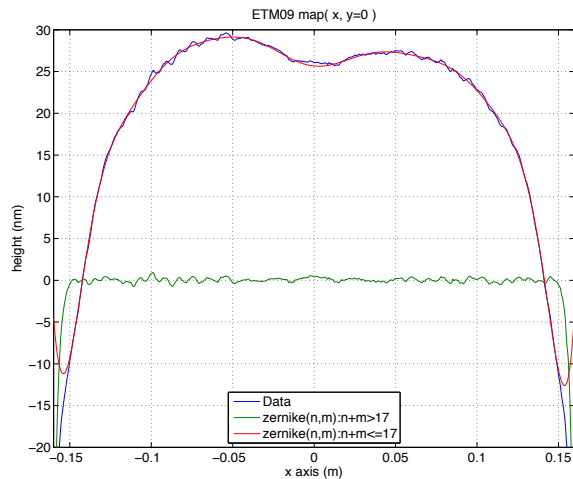


Log(P) on ITM
Log(P) on ETM

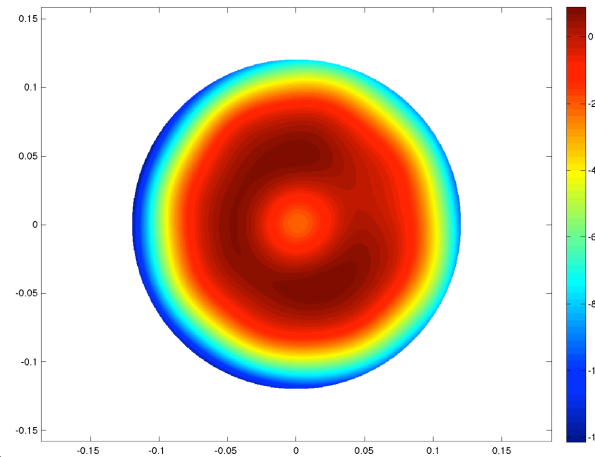


LMA coating and arm modes

ETM09 map

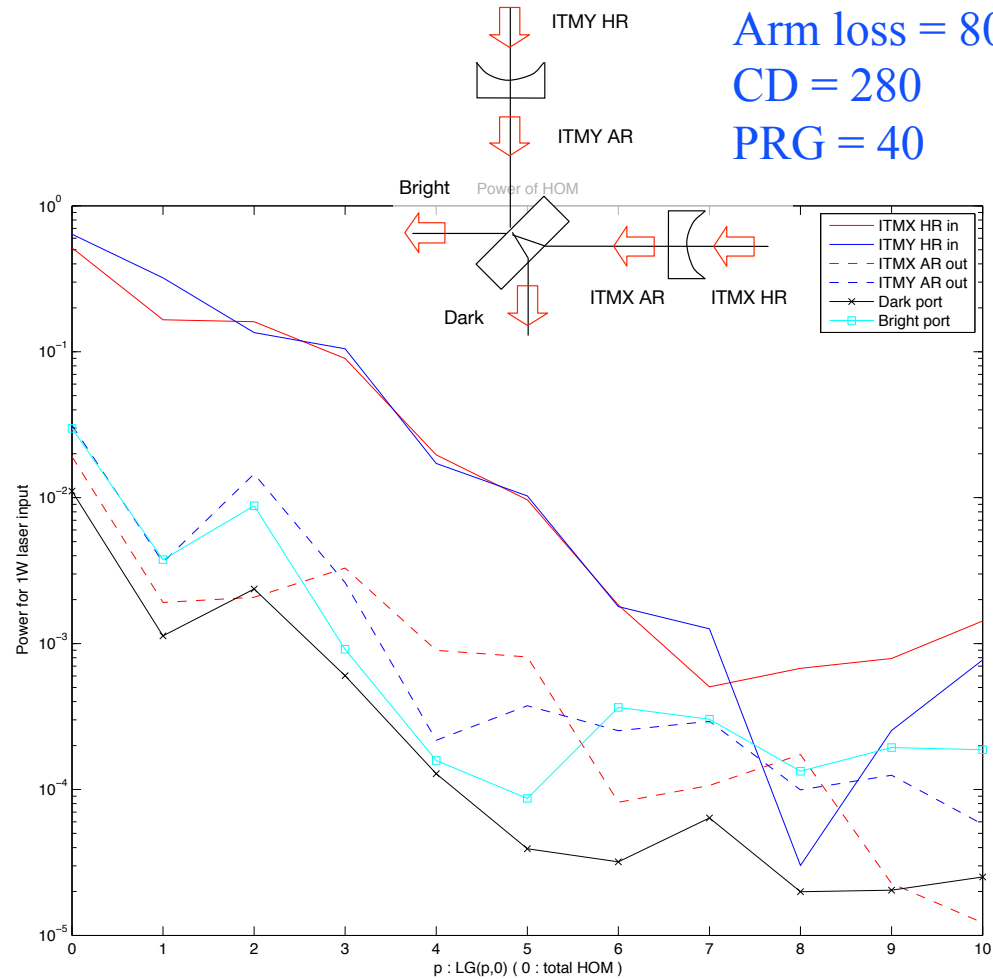


Zernike(n+m≤17)



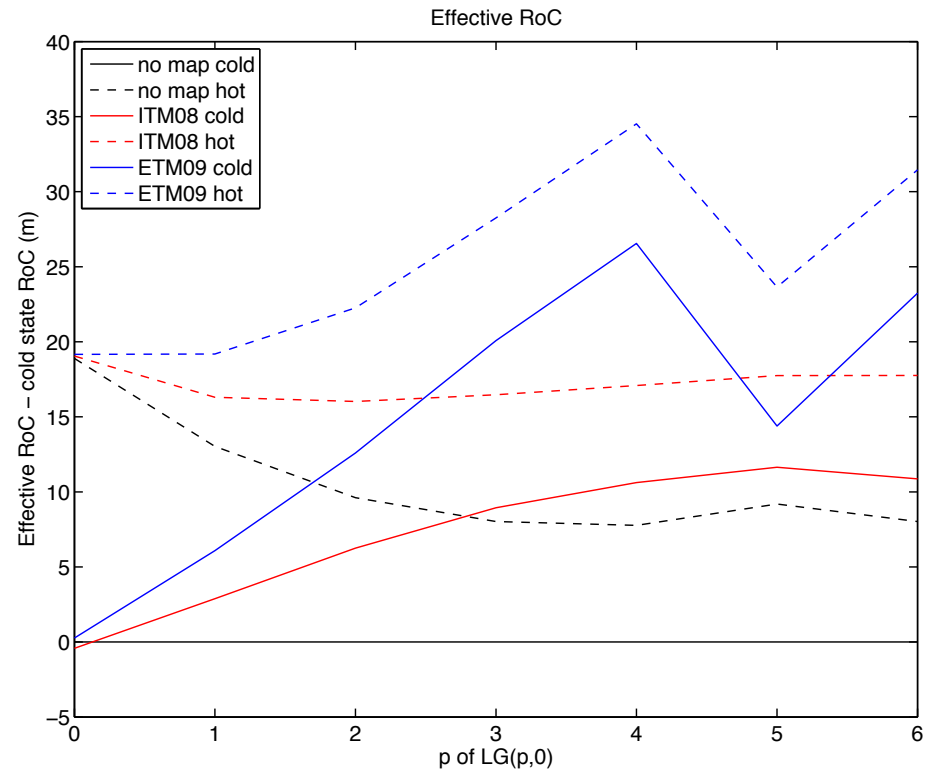
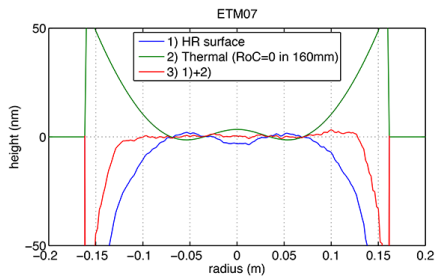
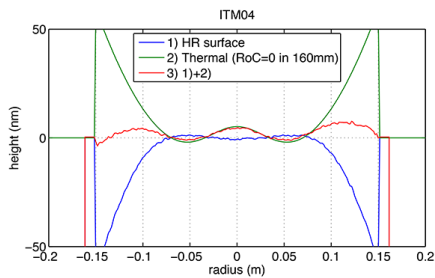
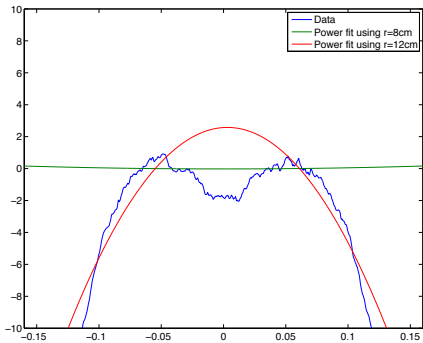
LIGO-G1400944

Arm loss = 80ppm
CD = 280
PRG = 40

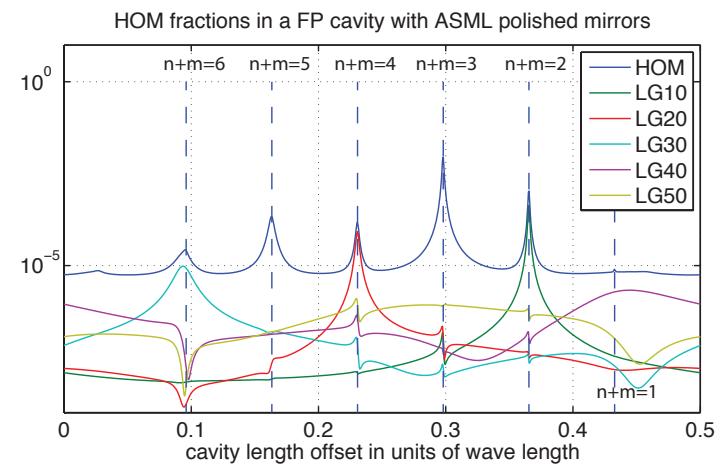
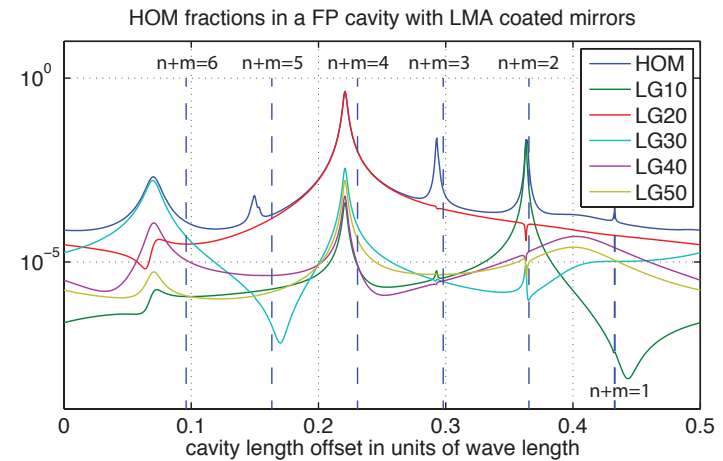
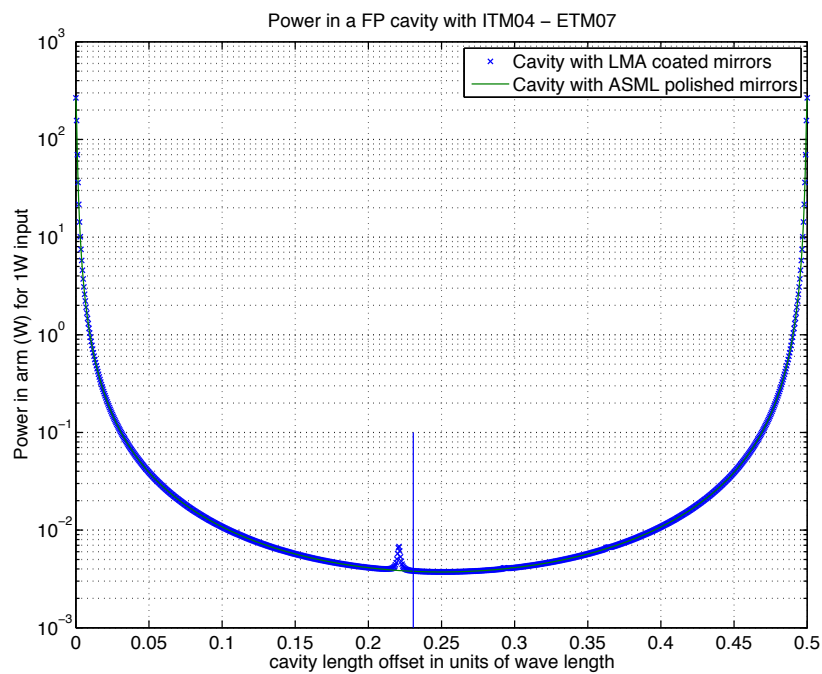




Effective RoC and modes



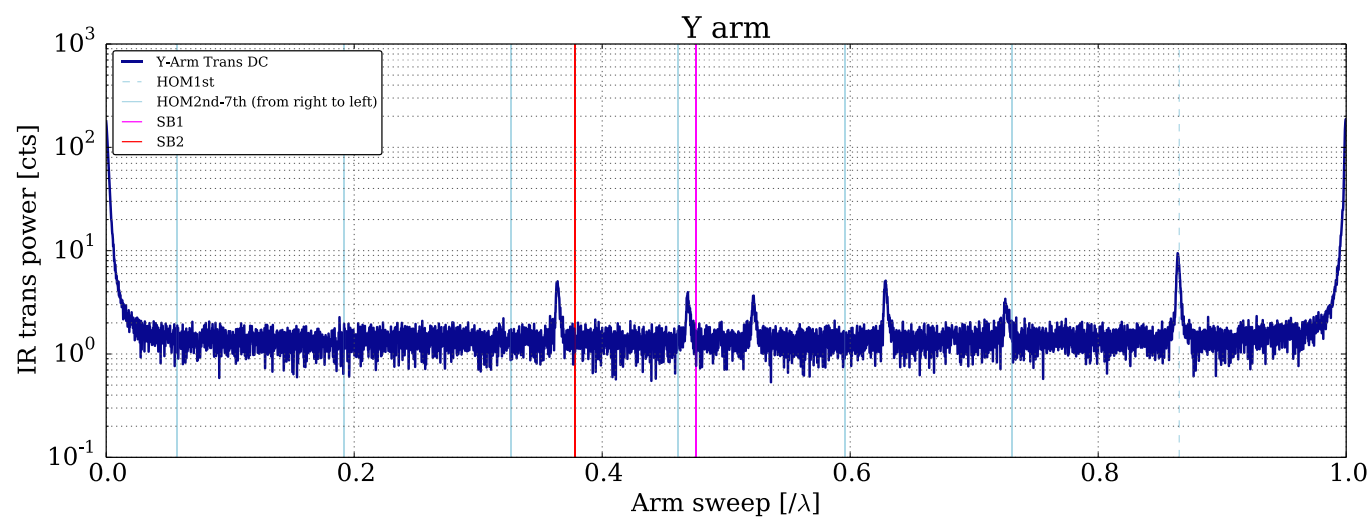
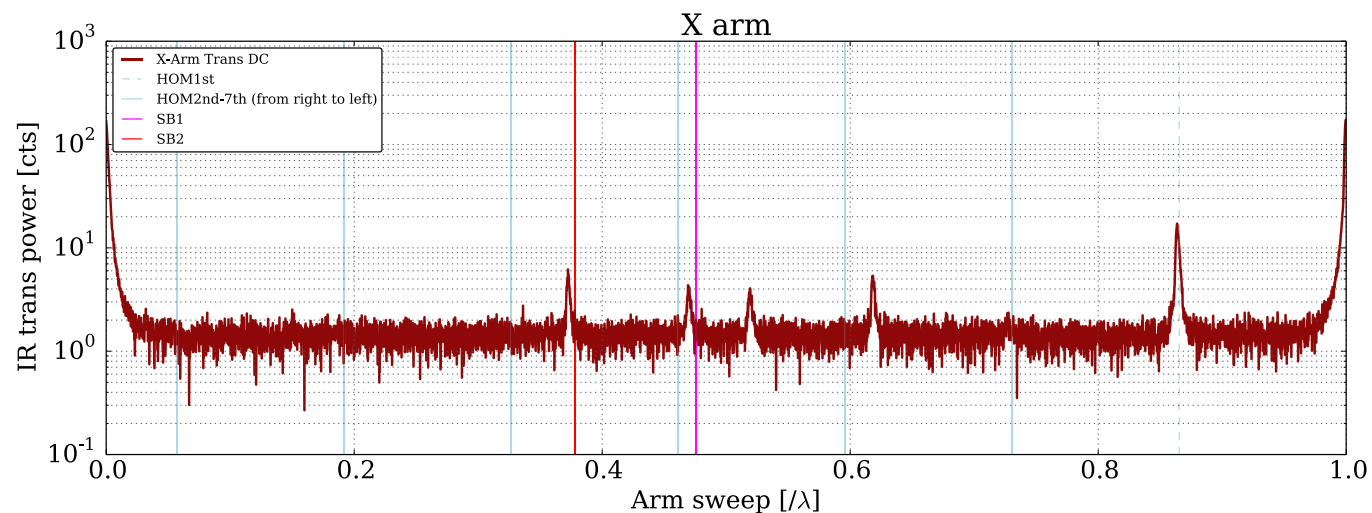
HOM peak and effective RoC





Arm scan : alog 14022

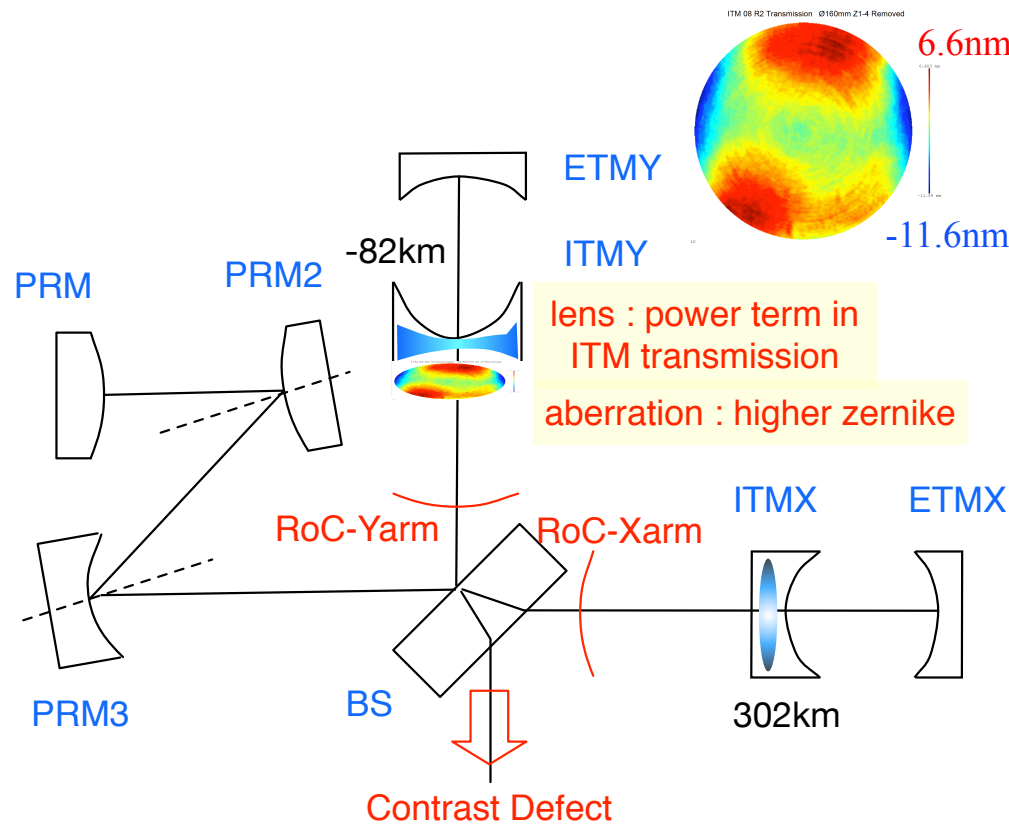
To do : [calibrate the VCO linearity](#) and refine (and add errors to) the data analysis. VCO sweep was not completely nice and linear.



Contrast Defect

412ppm : alog13916

CR only CD, no TCS



	No BS aperture	BS02	BS05
no lens no abr	44	200	82
lens abr	165	280	300
lens no abr	120	260	230
no lens abr	60	200	100

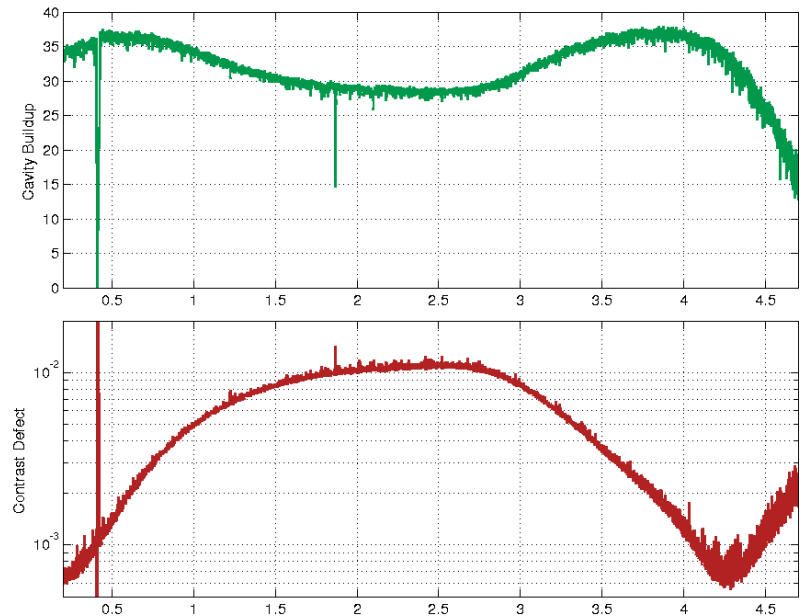
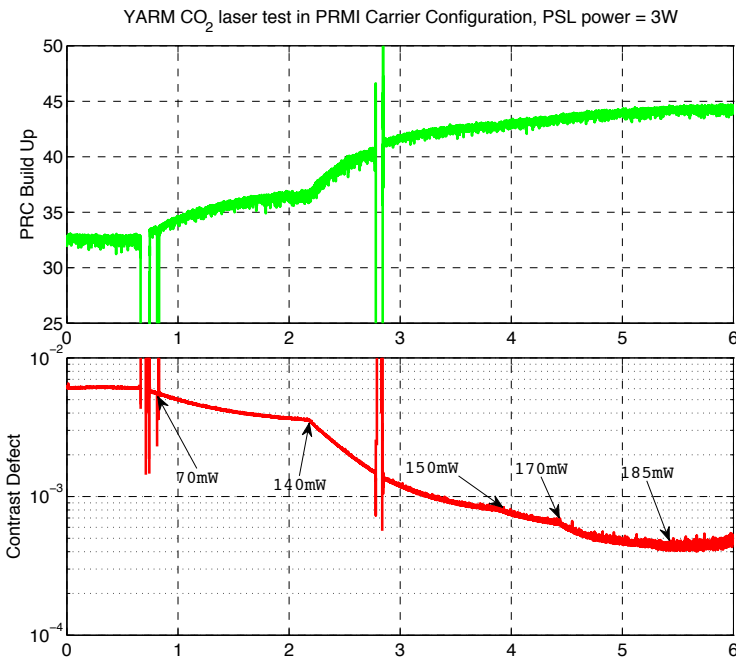
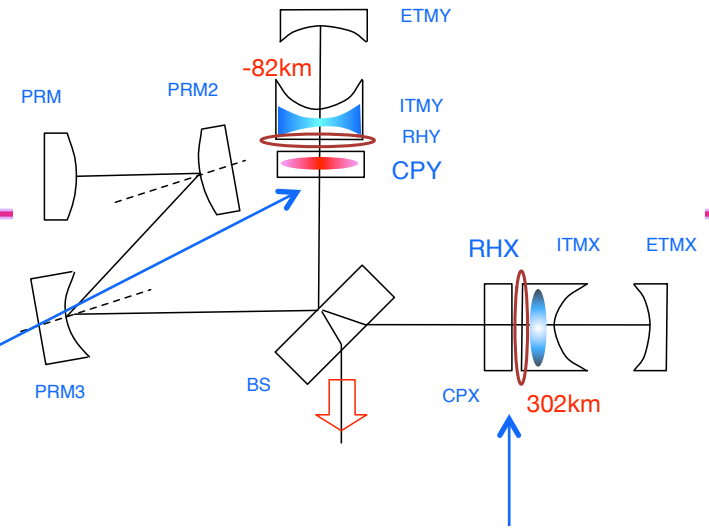
Beam center mismatch $\Rightarrow (a / 2w)^2 = 100\text{ppm}$ for $a=1\text{mm}$



TCS corrections for LLO PRMI

RH optimal lens = $n(\text{SiO}_2) \times 82\text{km} = 1/0.84 \times 10^{-5}$

CP optimal lens = $82\text{km} = 1/1.22 \times 10^{-5}$

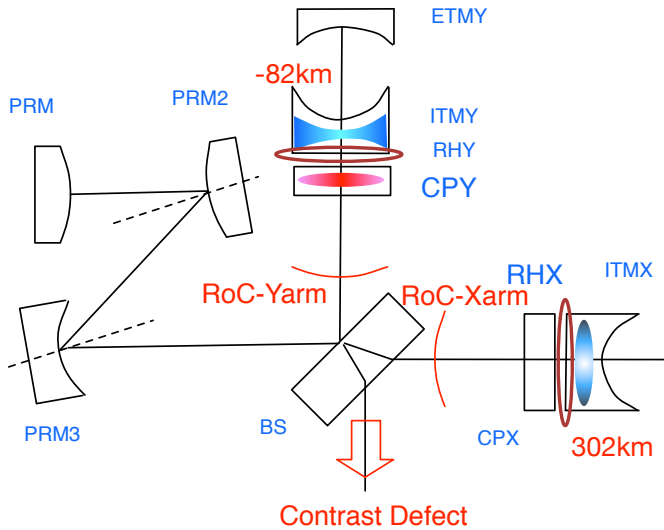
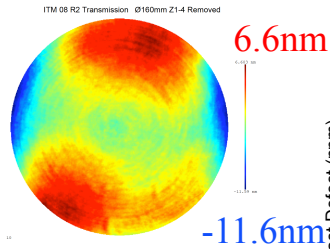


log11140 CD~400ppm, PRG~45

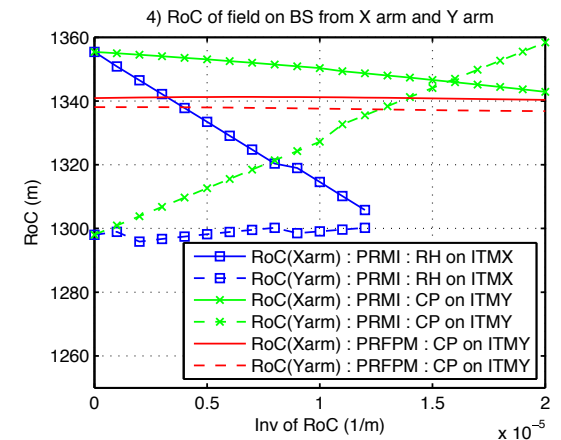
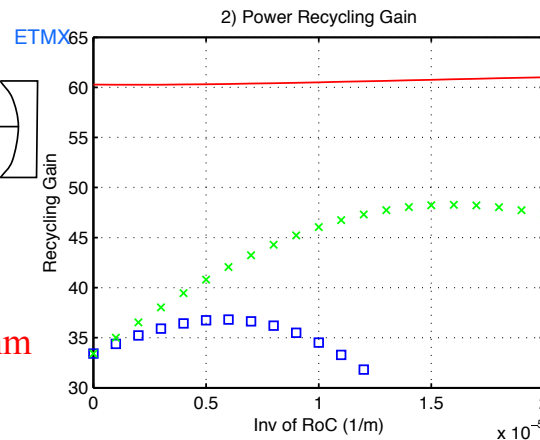
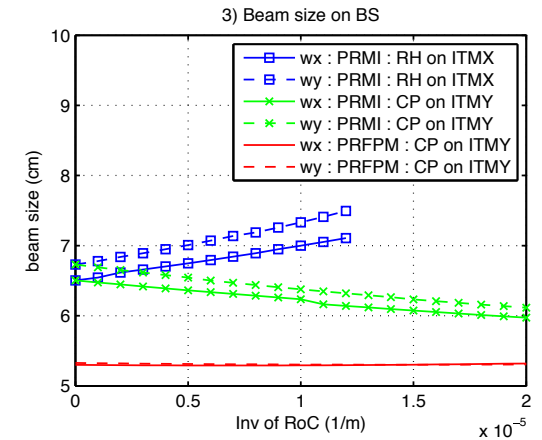
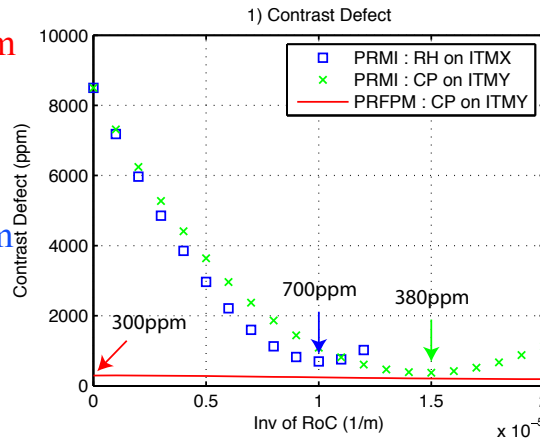
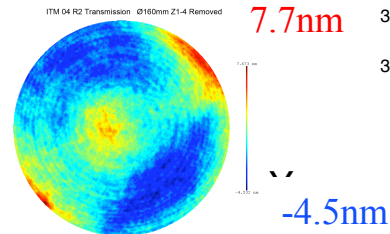
log#9733 CD~600ppm, PRG~35

(In)Sensitivity on ITM SPTWE + CP lens

ITM08 / ITMY
transmission
map in 160mm
w/o power

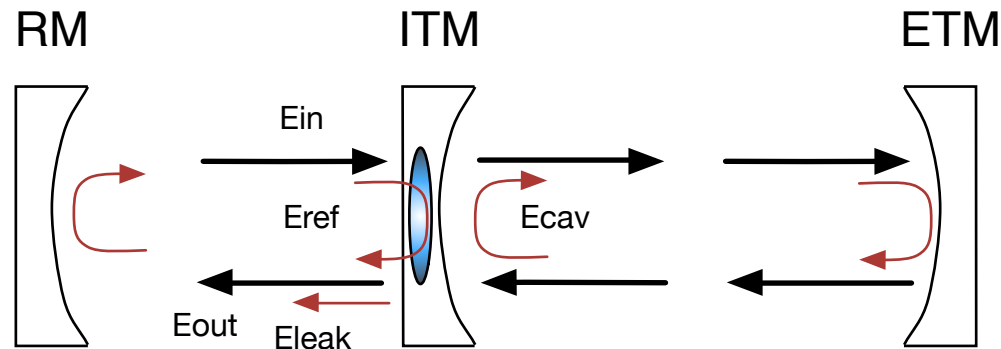


ITM04 / ITMX



LIGO-G1400944

Cavity mode



- Recycling cavity mode is defined by RM HR reflection and ITM reflection, E_{in} to E_{out} , not E_{in} to E_{ref} , just the same as length case
- Optimal coupling is $mode(E_{ref}) = mode(E_{leak})$, which makes $mode(CR \text{ in } RC) = mode(SB \text{ in } RC)$
- When thermal lens changes, $mode(CR \text{ in } RC)$ does not change in the first order, but the $mode(SB \text{ in } RC)$ changes in the first order
- But, CR suffers in the second order