



NORTHWESTERN
UNIVERSITY



UNIVERSITY
OF WISCONSIN

Rapid Compact Binary Coalescence Parameter Estimation in the Advanced LIGO Era

Chris Pankow (CIERA / Northwestern University)

Patrick Brady (CGCA / University of Wisconsin-Milwaukee)

Richard O'Shaughnessy (CCRG / Rochester Institute of Technology)

Evan Ochsner (CGCA / University of Wisconsin-Milwaukee)

Hong Qi (CGCA / University of Wisconsin-Milwaukee)

LIGO-G1601044

Based on PRD 92 (023002) / 1502.04370v1

AMR gridding paper to be submitted to CQG

Gravitational Waves: From Detection to Follow-Up

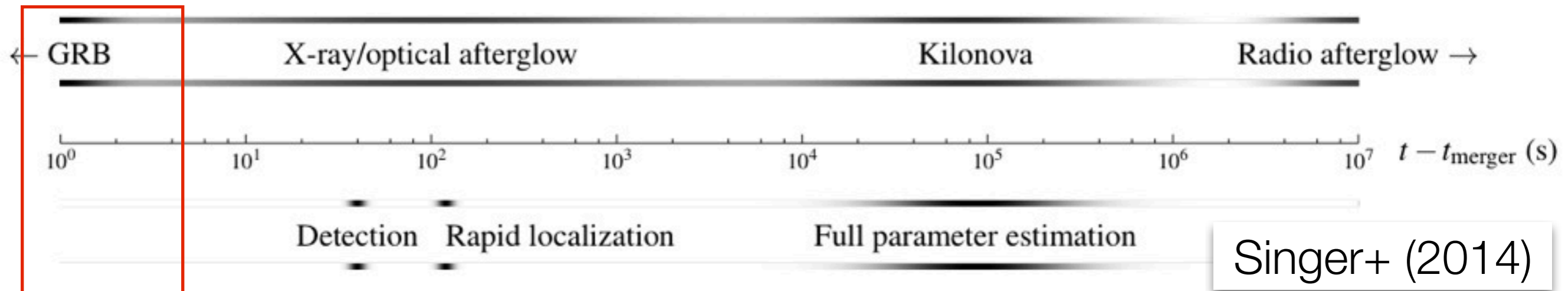


Figure 2. Rough timeline of compact binary merger electromagnetic emissions in relation to the timescale of the Advanced LIGO/Virgo analysis described in this paper. The time axis measures seconds after the merger.

- NSBH / BNS sources main candidate for joint observations between GW and EM facilities
- GW detection could inform how we observe with EM and vice-versa
 - Early coincidence and informed follow up of EM+GW candidates already in play (talk by **M. Cho**)
- Discovery opens up rich field of astrophysics associated with joint GW + EM emission and modeling (GRBs, kilonovae, SNe, etc...)

Gravitational Waves: From Detection to Follow-Up

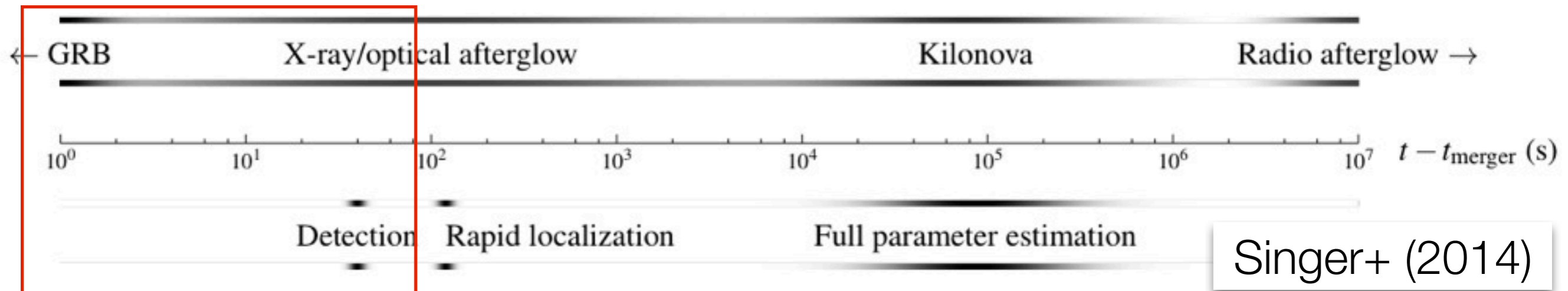
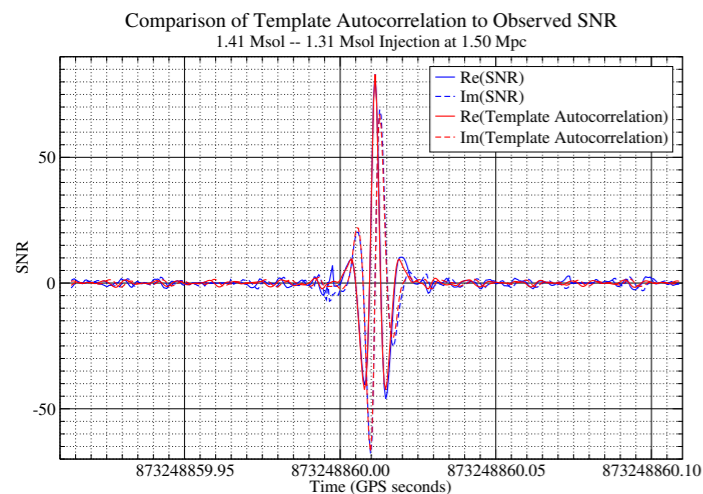


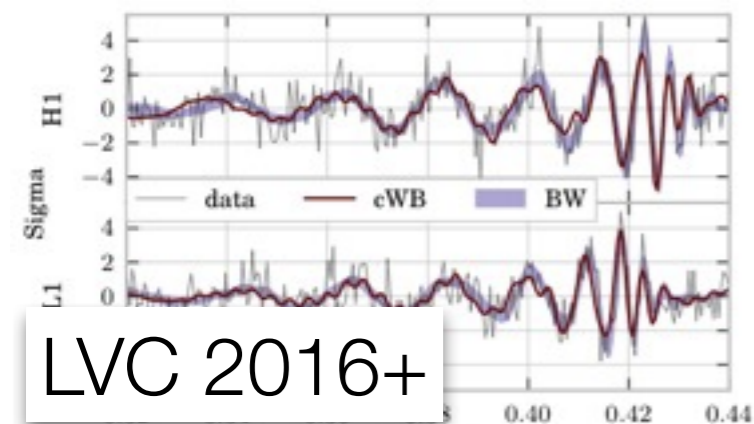
Figure 2. Rough timeline of compact binary merger electromagnetic emissions in relation to the timescale of the Advanced LIGO/Virgo analysis described in this paper. The time axis measures seconds after the merger.



- Low latency searches **produce candidate event times in O(min)**

- **Large template banks to search a wide space of parameters (mass/spins)**

- **Great for detection, not so great for parameter estimation: No modeled facility for sky localization, distance estimation is poor**



Gravitational Waves: From Detection to Follow-Up

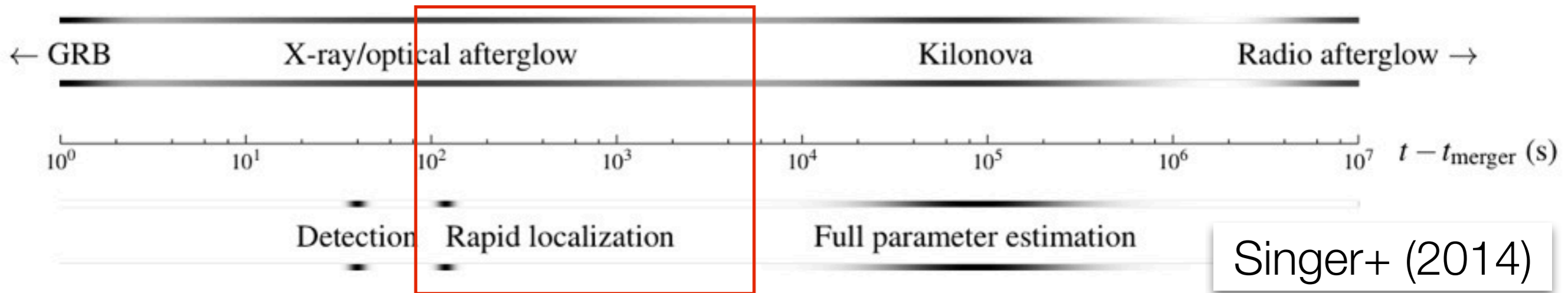
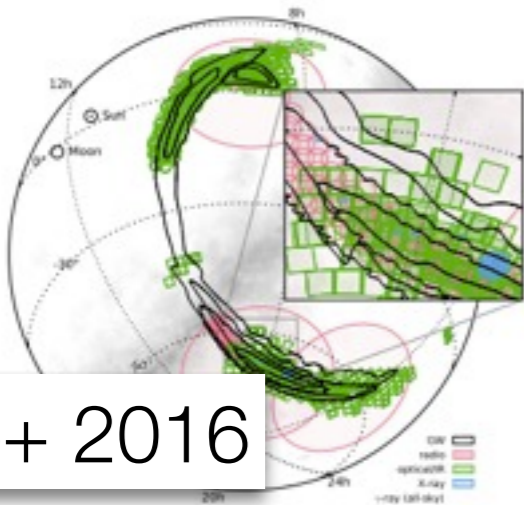


Figure 2. Rough timeline of compact binary merger electromagnetic emissions in relation to the timescale of the Advanced LIGO/Virgo analysis described in this paper. The time axis measures seconds after the merger.

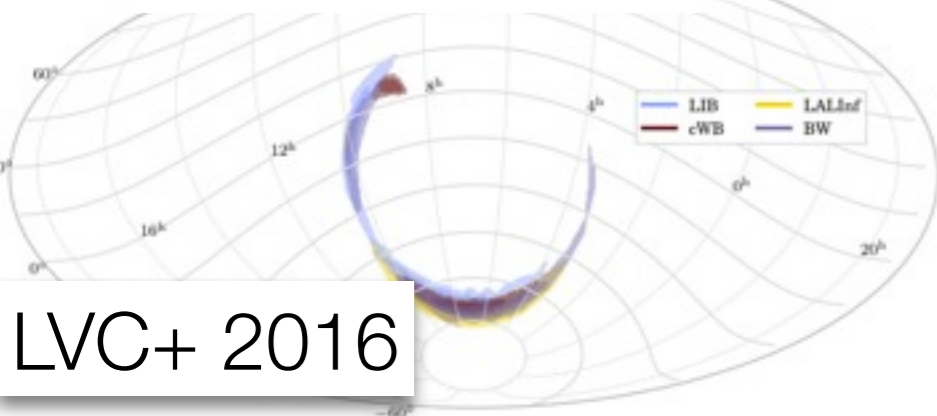
- Some very fast schemes to produce posterior distributions on the sky → **astronomers point telescopes**

- Fold in a few more parameters, **may not account for other masses or spin configurations**

- Are we dealing with a “**EM-bright**” source? Is it **inclined towards us**? Redshift?



LVC+ 2016



LVC+ 2016

Gravitational Waves: From Detection to Follow-Up

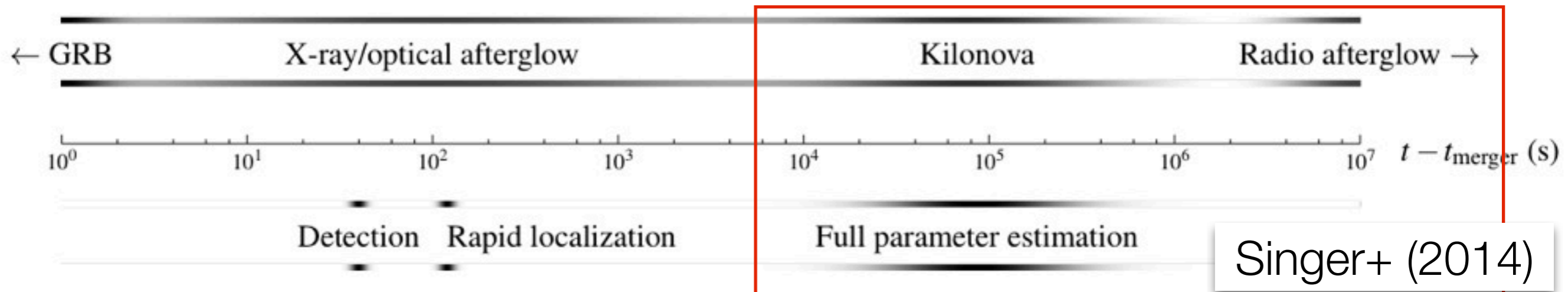
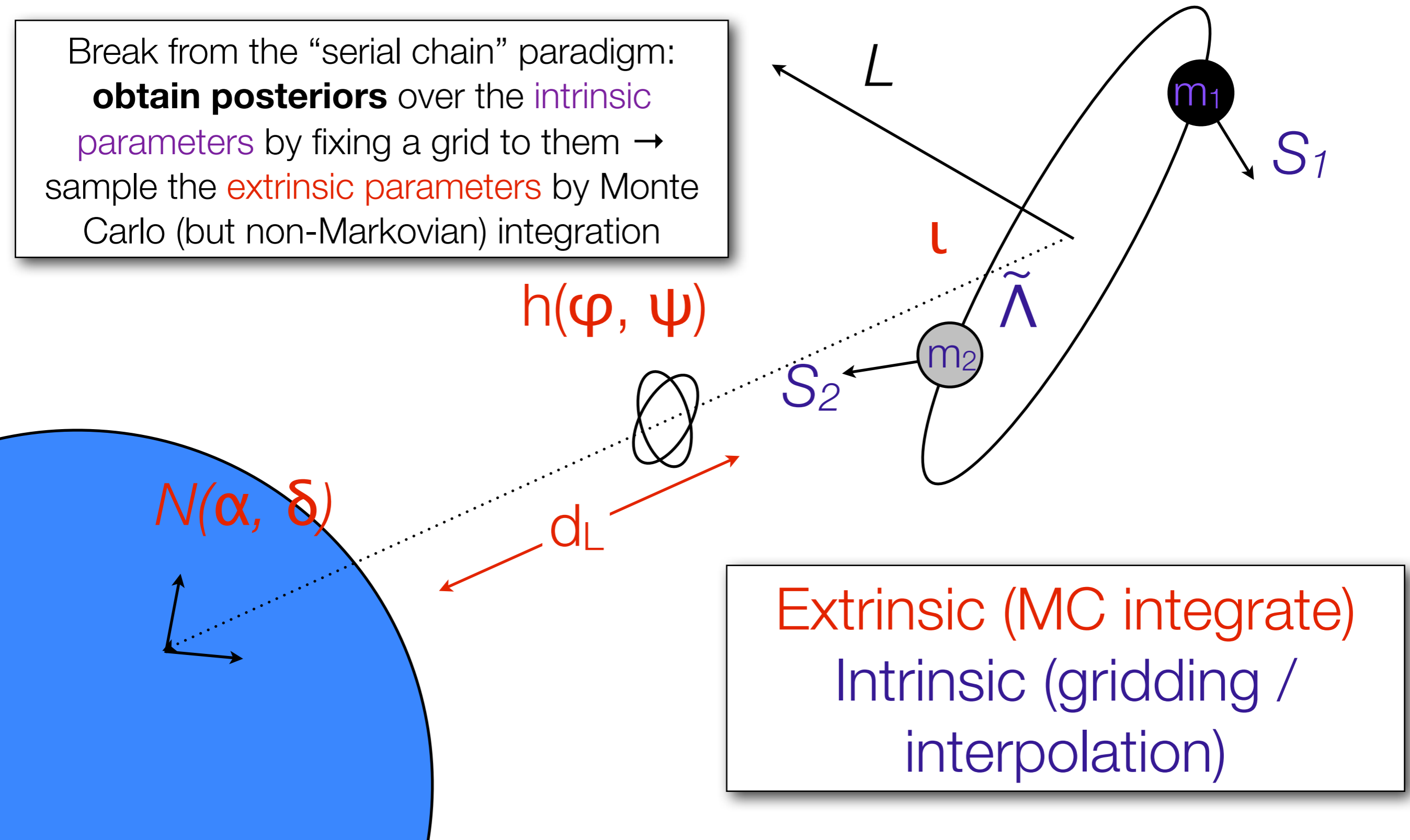


Figure 2. Rough timeline of compact binary merger electromagnetic emissions in relation to the timescale of the Advanced LIGO/Virgo analysis described in this paper. The time axis measures seconds after the merger.

- GW sky position posteriors are **wide**, need a highly coordinated effort for best observing strategy → fast and confirmed localization **can boost detection confidence** in NSBH or BNS GW candidate and **better populate light curves**
- **Full parameter estimation in O(days)**: but we may have already **lost the optical afterglow (GRB)** ... also will have **technical challenges** with half hour long **BNS in 2018**
- ***Need to do basic parameter estimation (masses/distance/inclination) in O(min) to better facilitate optical follow up***

System Parameterization

Break from the “serial chain” paradigm:
obtain posteriors over the **intrinsic parameters** by fixing a grid to them →
 sample the **extrinsic parameters** by Monte Carlo (but non-Markovian) integration



Extrinsic (MC integrate)
 Intrinsic (gridding /
 interpolation)

Rapid PE: Ingredients

- At fixed **intrinsic parameters**, the likelihood has a novel formulation which only requires **one** waveform generation (\mathbf{h}), and **one** set of precomputed inner products over a **spherical harmonic mode decomposition** (l,m) of the **measured** (ρ) and **optimal** ($\bar{\rho}$) signal to noise ratio \rightarrow reconstruct the likelihood at arbitrary **extrinsic parameters** with a few multiplications and adds

$$\tilde{s}(f) = \tilde{h}(f) + \tilde{n}(f)$$

$$\ln \mathcal{L} \propto \rho - \frac{1}{2} \bar{\rho}^2$$

$$\ln \mathcal{L}(\lambda^0, \theta) = \frac{d_{\text{ref}}}{d} \Re \sum_k \sum_{l,m} F_k Y_{lm}^* \rho_{k,lm}(\lambda^0) - \frac{d_{\text{ref}}^2}{4d^2} \sum_k \sum_{lm, l'm'} |F_k| Y_{lm}^* Y_{l'm'} \bar{\rho}_{k,lm,l'm'}(\lambda^0) + \Re (F_k^2 Y_{lm} Y_{l'm'} \bar{\rho}^*(\lambda^0))$$

$$F_k \sim \{\alpha, \delta\}$$

$$Y_{lm} \sim \{\iota, \psi, \phi\}$$

Precomputed

$$\rho_{k,lm} = (h_{k,lm} | s)$$

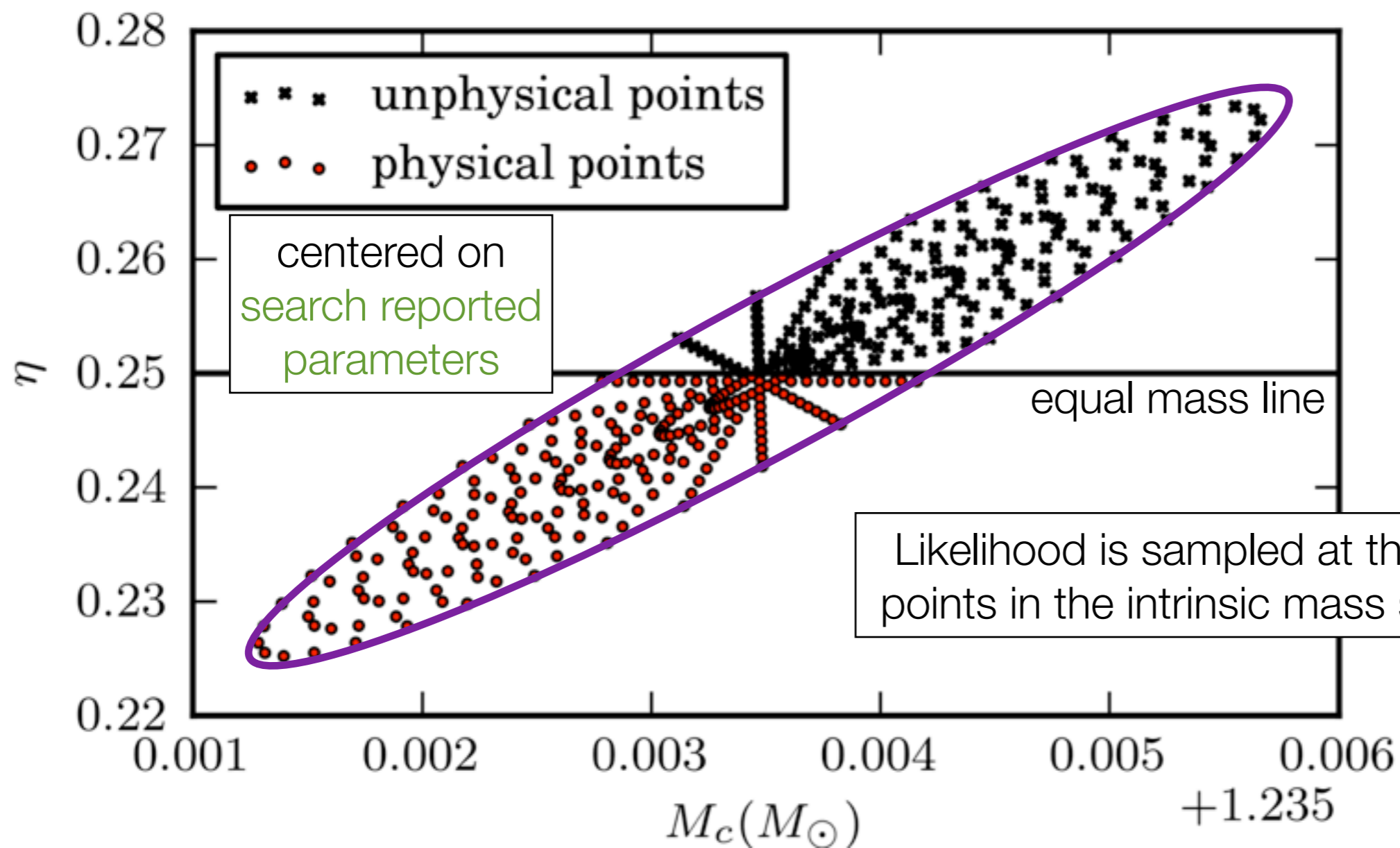
$$\bar{\rho}_{k,lm,l'm'} = (h_{k,lm} | h_{k,l'm'})$$

$$\bar{\rho}_{k,lm,l'm'}^* = (h_{k,lm}^* | h_{k,l'm'})$$

...over k instruments...

Intrinsic Parameter Placement (Fisher-matrix)

- Low latency searches provide intrinsic parameter measurement (possibly biased or incomplete!) → we use this to guide a strategic placement of the intrinsic grid

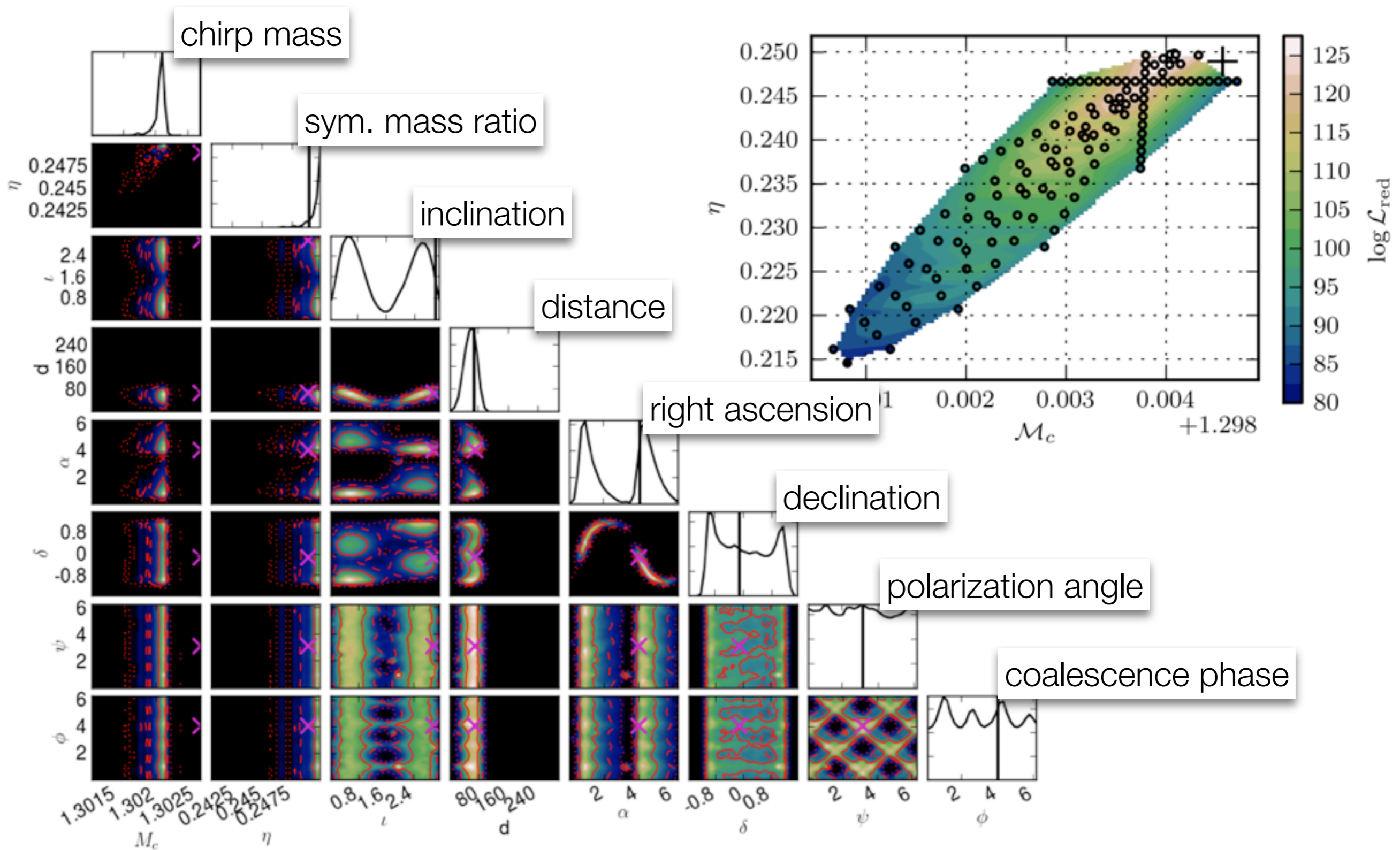


Fit to **parameter ambiguity** contours

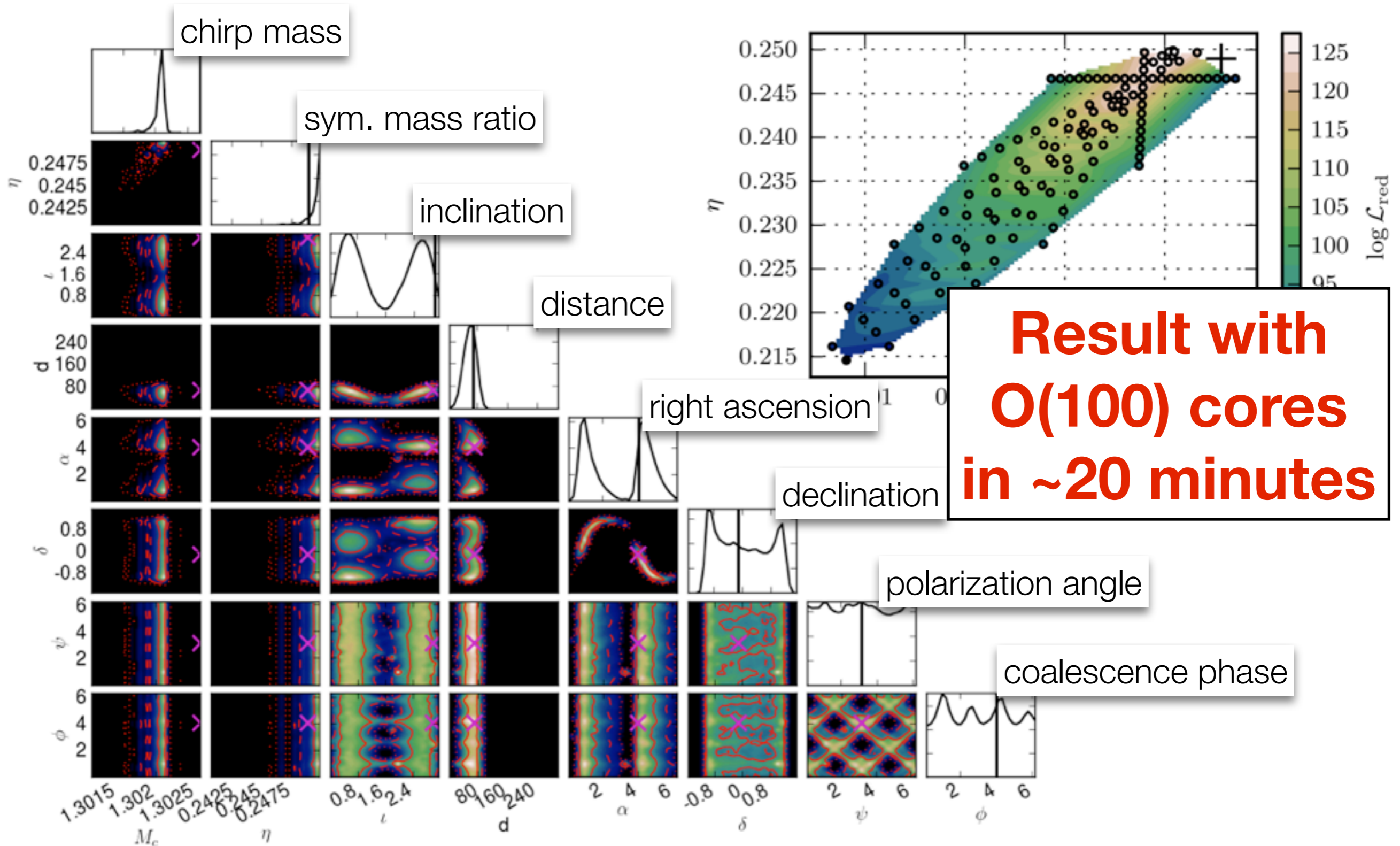
Used as a surrogate to the shape of the likelihood surface in the intrinsic parameters

+1.235

Parameter Estimation Results: Synthetic BNS Signal in O1



Parameter Estimation Results: Synthetic BNS Signal in O1



Improving Placement / Using Search Information

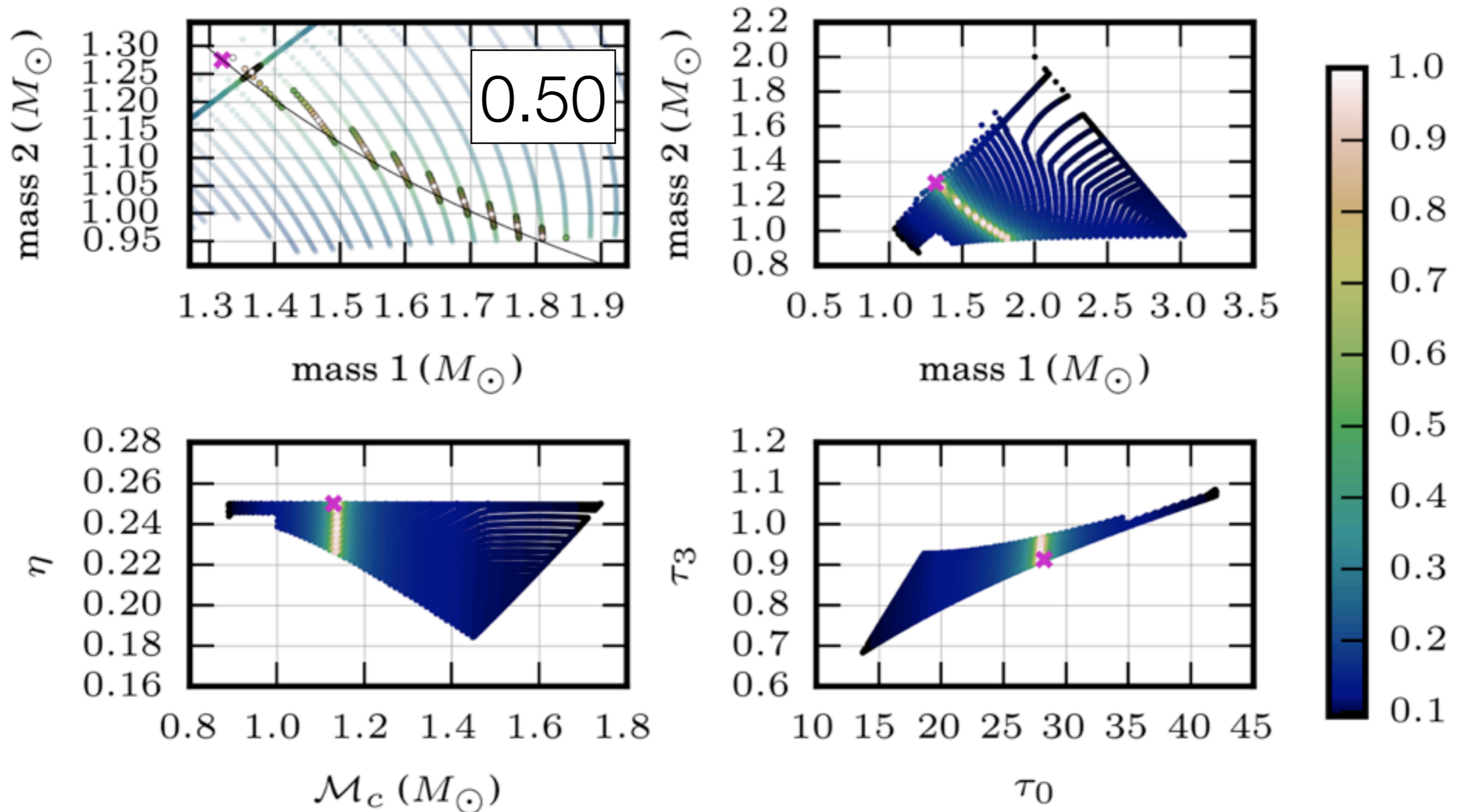
- Initial point selection motivated by Fisher matrix which has limited applicability (inappropriate at low SNR, multimodality in the likelihood function, no clear gridding procedure)
- Template banks of waveforms have ~3% mismatch — very densely oversampled for detection in the intrinsic basis

$$\mathcal{O}_{12} = \frac{(h_1|h_2)}{\sqrt{(h_1|h_1)(h_2|h_2)}} \sim 0.97$$

- Solution: Use point estimate of mass information from the search and check the search template bank for “relevant templates”

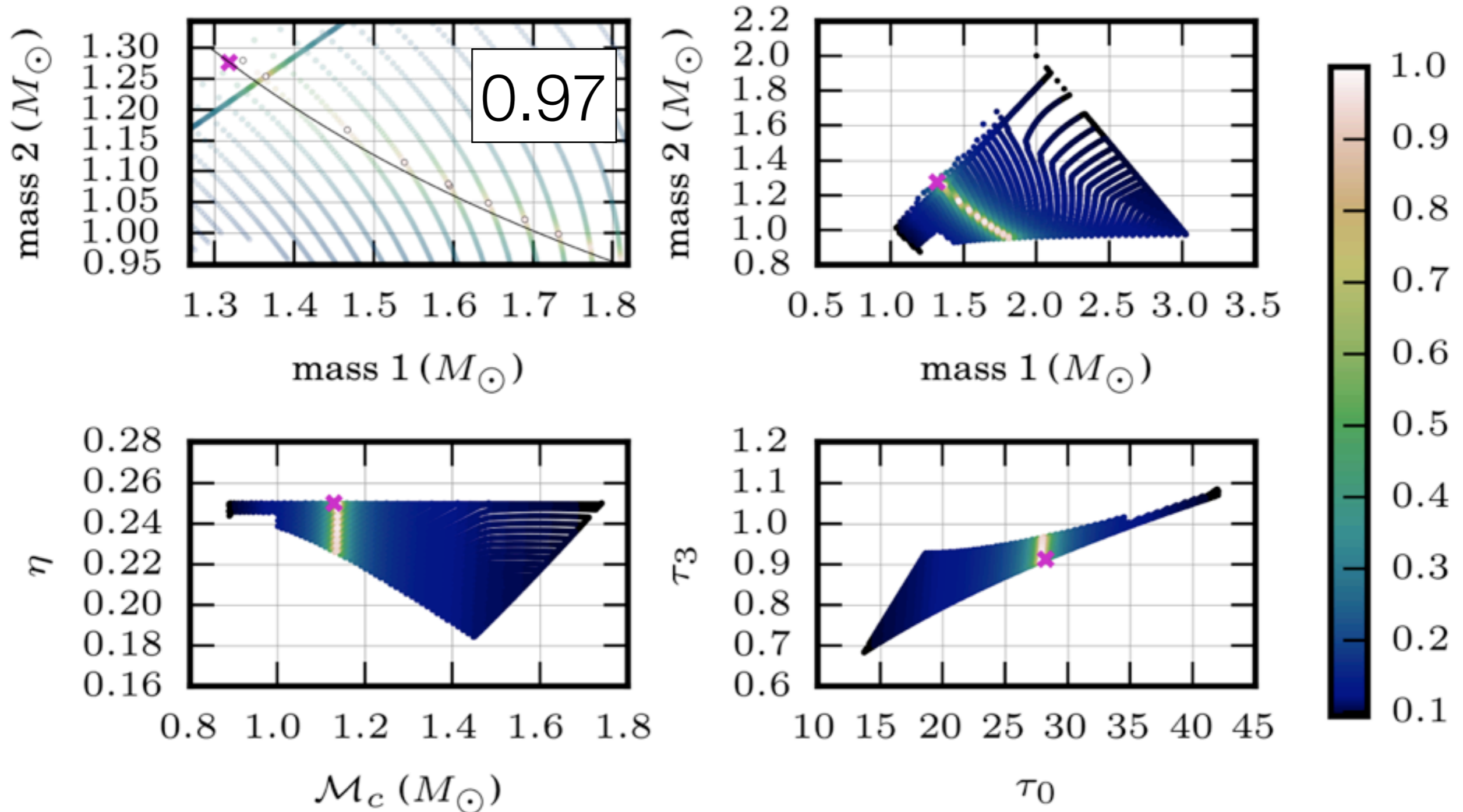
Improving Placement / Using Search Information

Overlap with template bank for (1.32, 1.28)

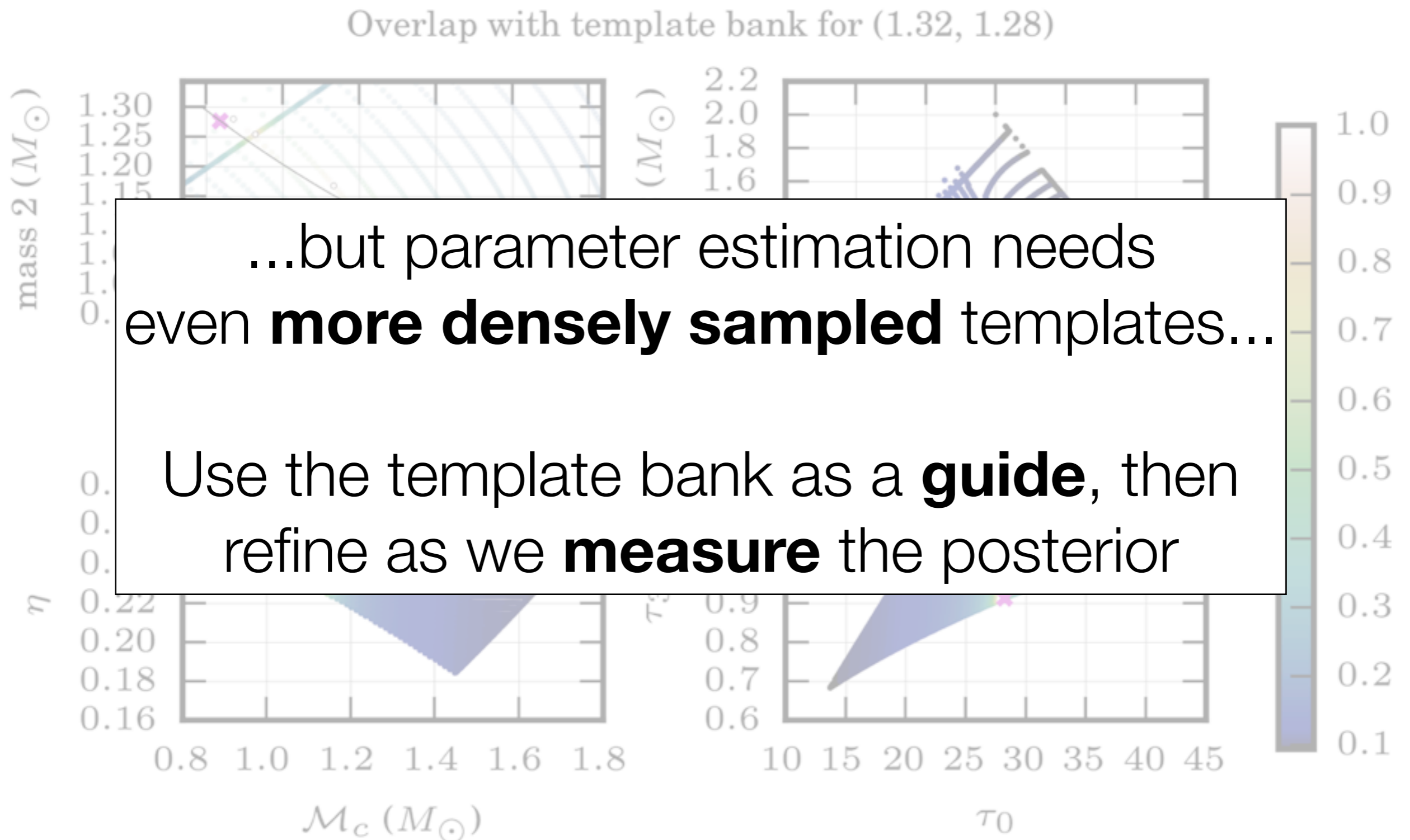


Improving Placement / Using Search Information

Overlap with template bank for (1.32, 1.28)

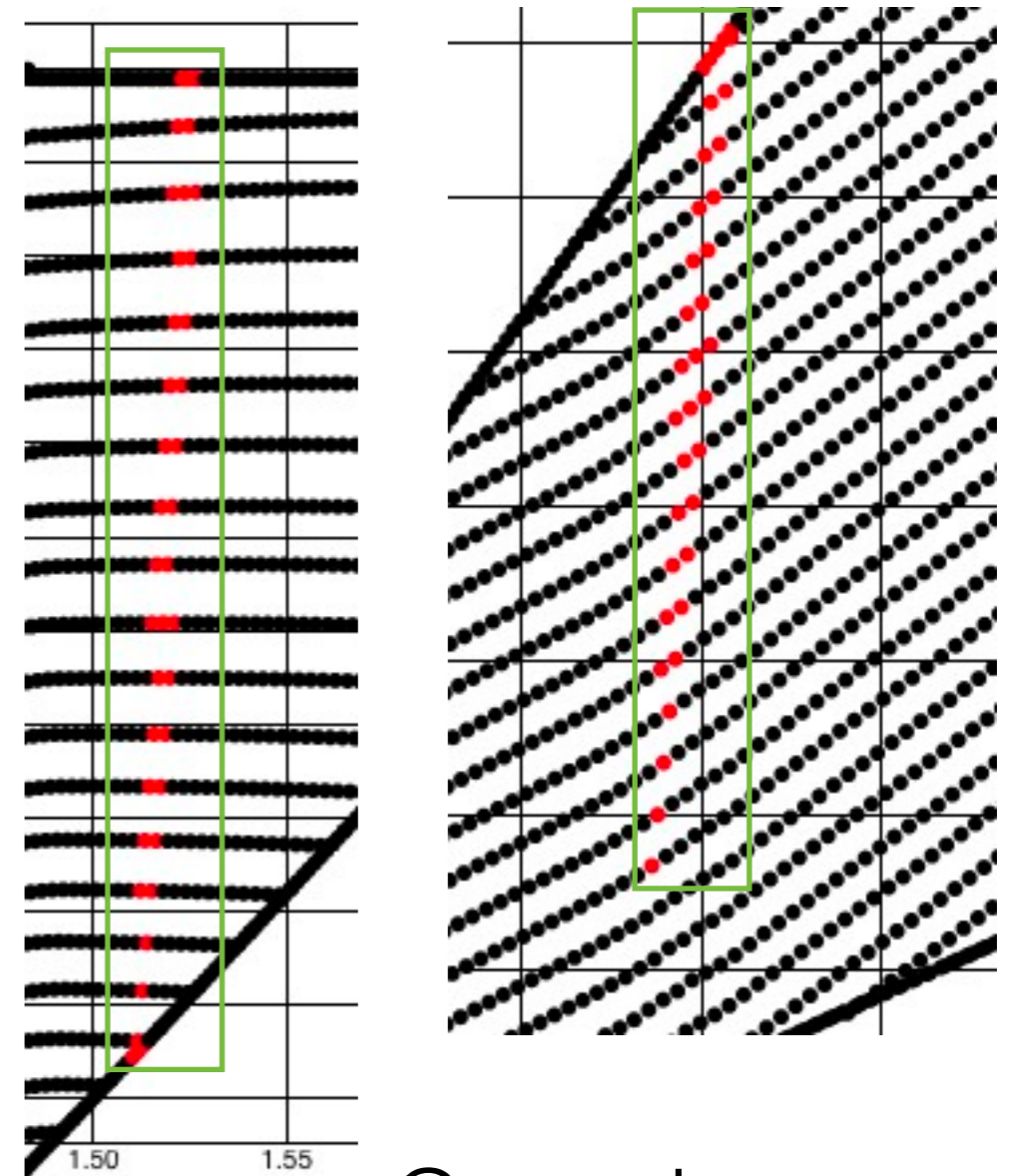
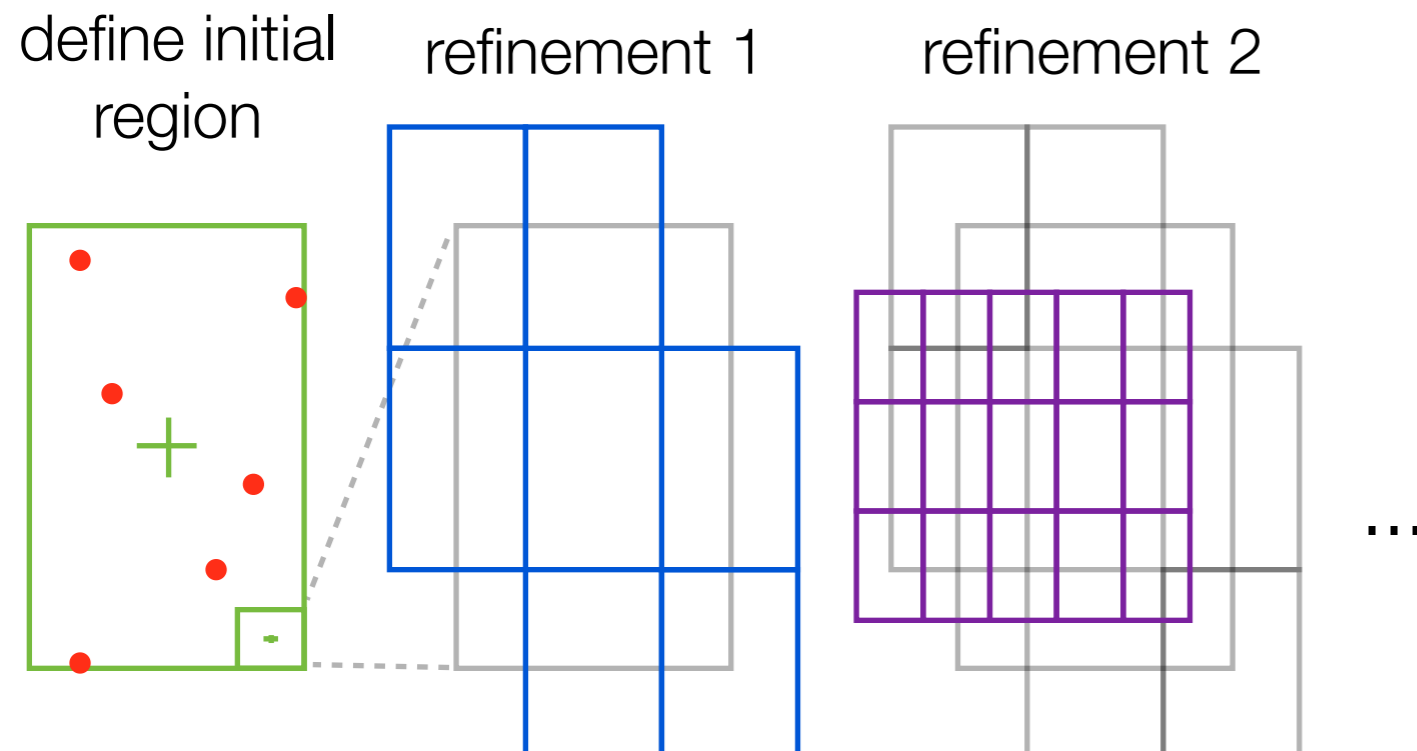


Improving Placement / Using Search Information



Region Identification and Grid Construction

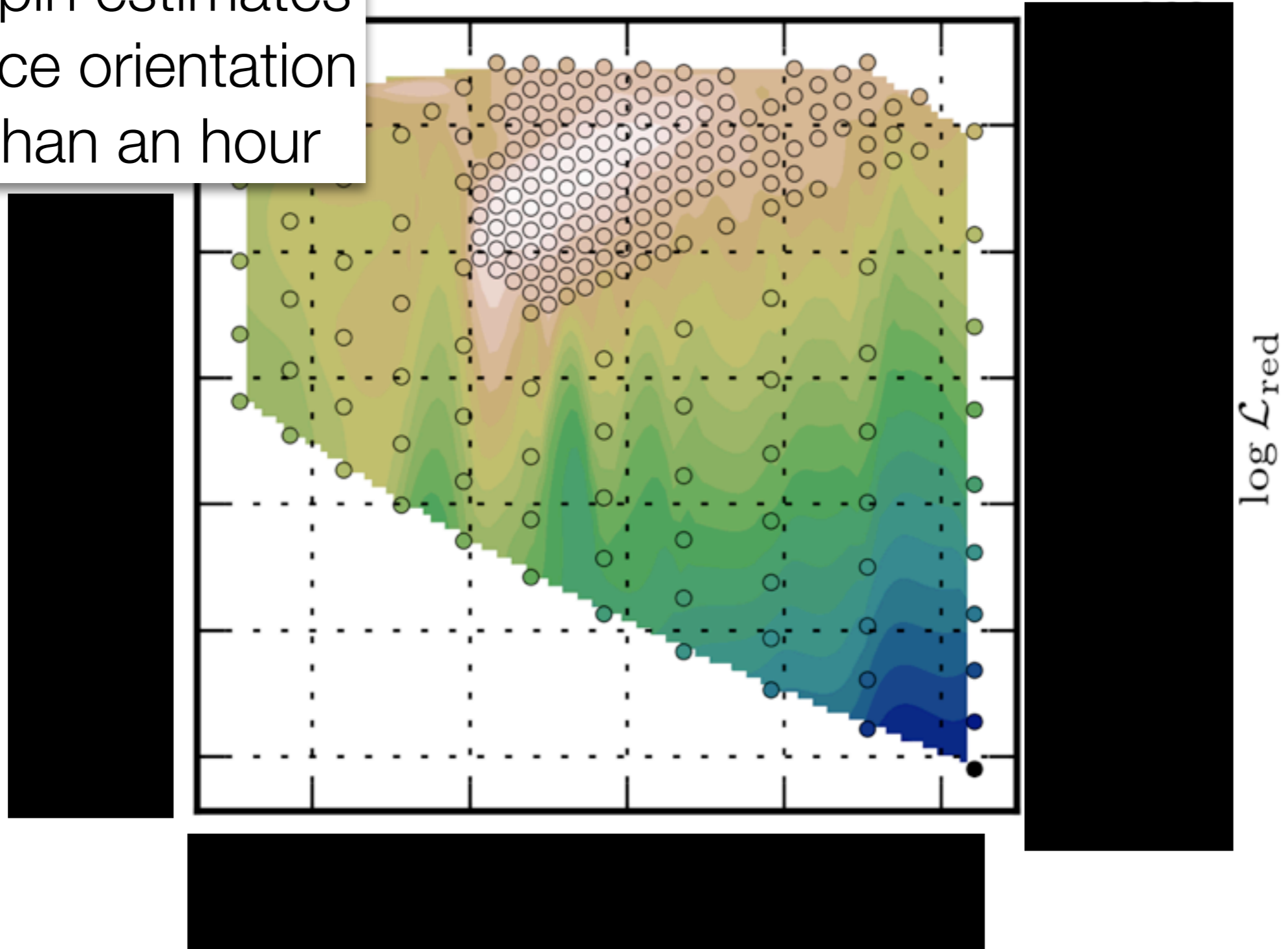
- The same points in M_c / η (left) and τ_0 / τ_3 (right) space — Euclidean “closeness” and overlap “closeness” much more local and apparent here
- Use these to define cells upon which to adapt — Cell can be arbitrarily refined, or not evaluated at all depending on initial overlap or evaluated L_{red} at the point



Green box
approximates cell
“region”

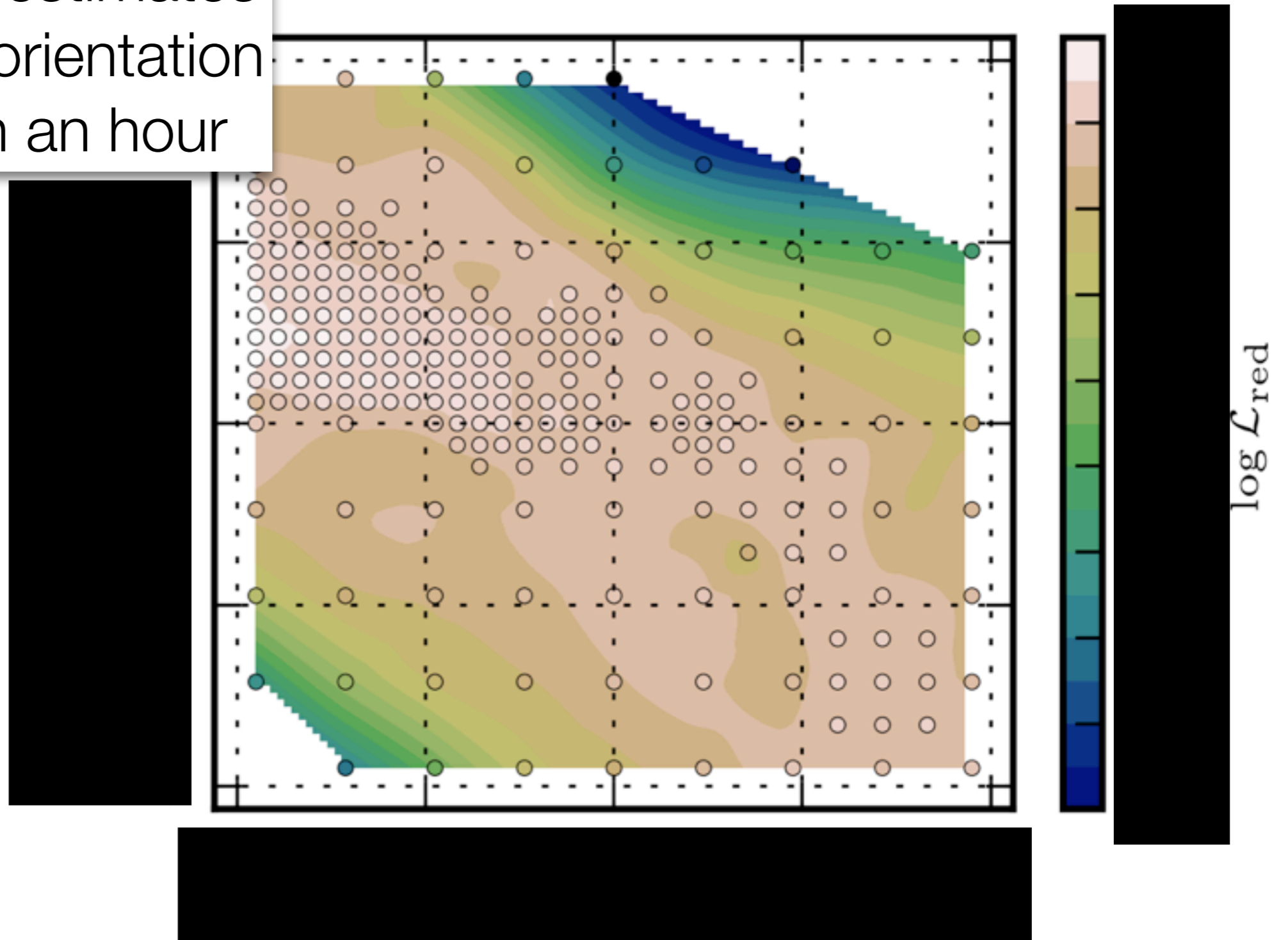
GW150914

mass / spin estimates
and source orientation
in less than an hour



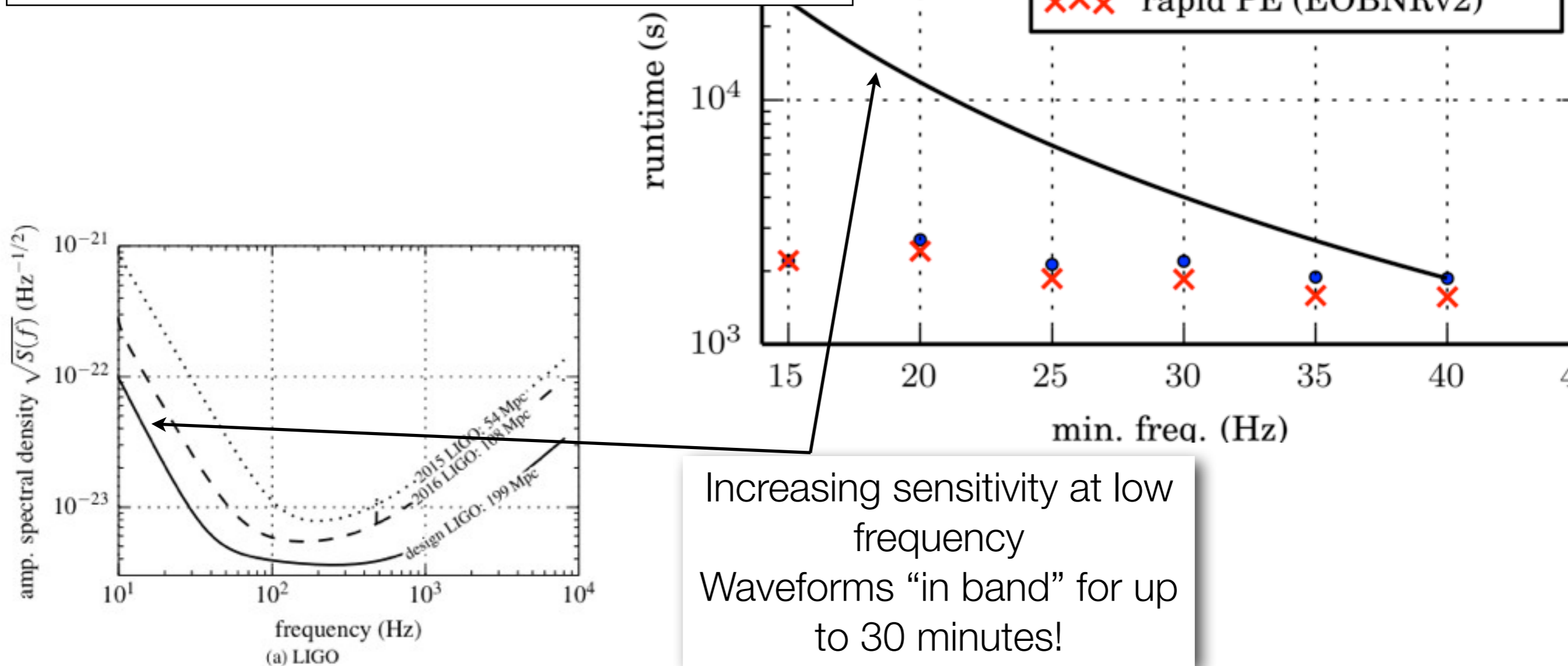
GW150914

mass / spin estimates
and source orientation
in less than an hour



Scaling to Design Sensitivity Advanced LIGO

We can use any waveform in full design sensitivity advanced LIGO... *right now*

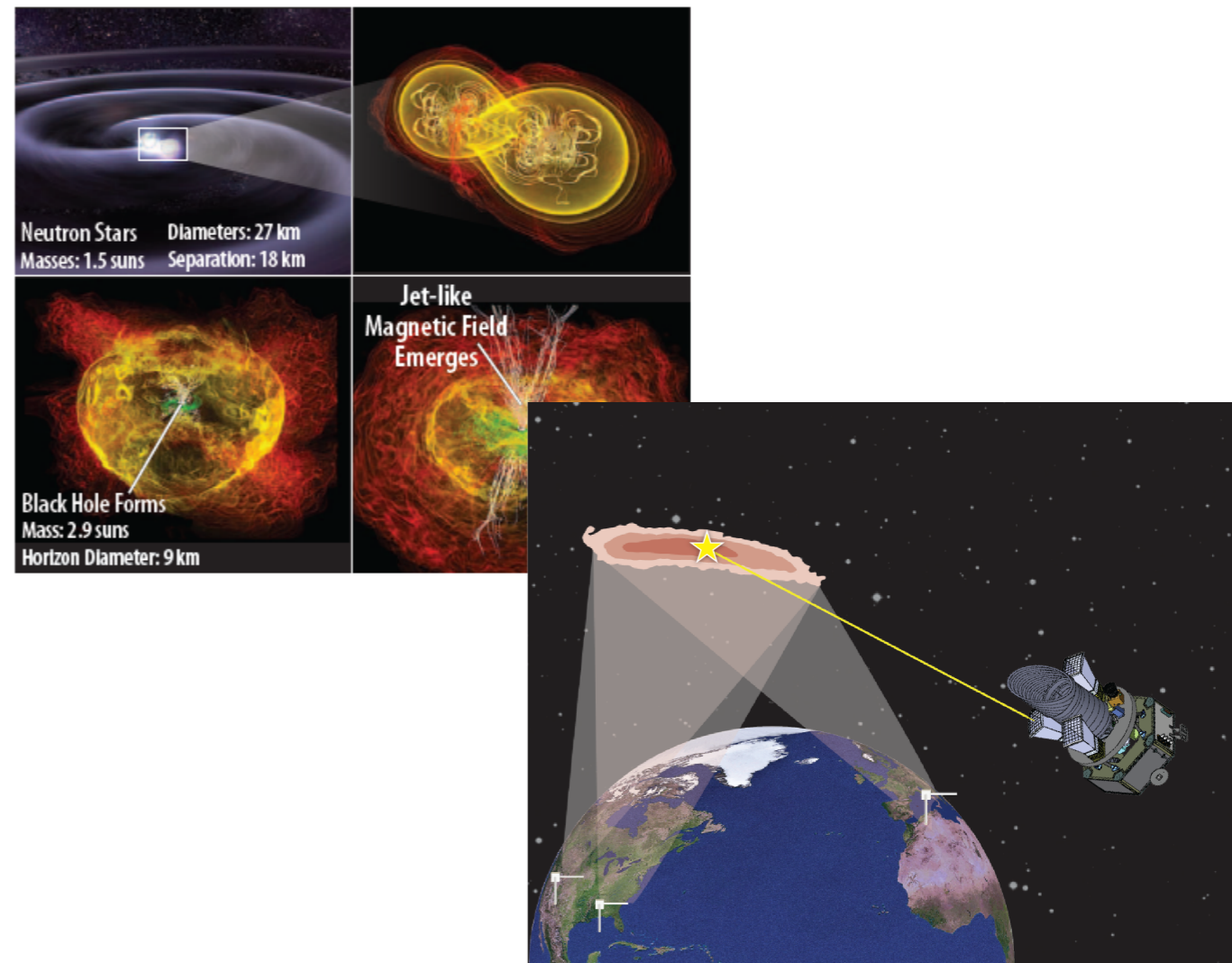


The Upshot

- Minimal parameter estimation (expanding into aligned spin) in **under an hour**
- Gearing up to be running in **near real time response** to LIGO-Virgo triggers in 2nd Observation Run
- **Extensible** and ready for observations **throughout the lifetime** of advanced interferometric instruments (up through 2018+)
- Extensions to **precessing spin** and **use of NR waveforms** has been done ([arxiv: 1606.01262](https://arxiv.org/abs/1606.01262))
- ***Bring on the NSBH and BNS!***

Explorer for Transient Astrophysics (ETA)

- EM Followup of Gravitational Wave Detections (launch ~2023)
 - Wide-Field Imager (WFI) search for X-ray afterglows (and possibly prompt emission!)
 - IR Telescope search for kilonovae IR emission
 - Gamma-ray Transient Monitor (GTM)
- Early Universe Studies with High Redshift GRBs
 - IRT followup of GTM/ WFI detection
- X-ray Transient Sky
 - Tidal Disruption Events
 - SN Shock Breakouts



Several per year NS-NS and/or NS-BH

Increase range, confidence of LIGO detections

Precise localization of source (redshift)

Energetics of source

Relative speed of graviton and photon (10^{-17})

Extrapolating the Shape of the Likelihood

