

# Modeling and simulations of amorphous coatings

GWADW, 2018  
May 15, 2018  
Girdwood, Alaska

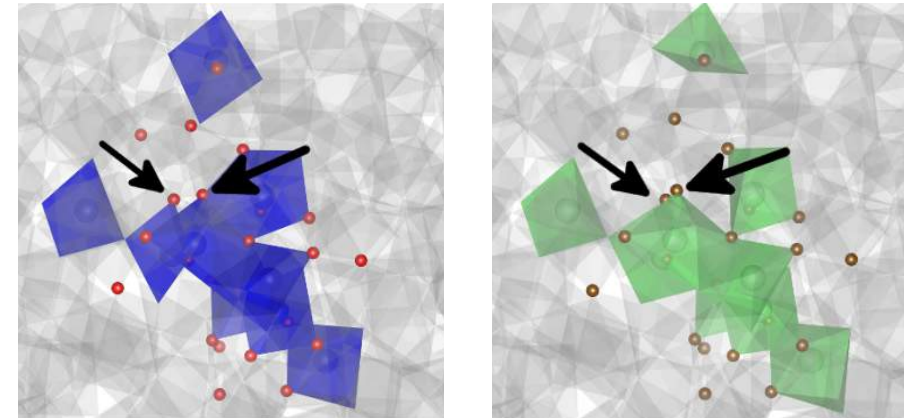
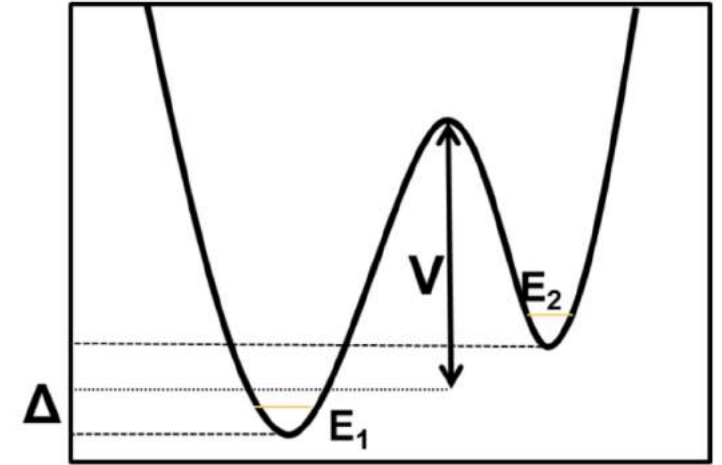
LIGO-G1801021

Kiran Prasai  
Stanford University  
prasai@stanford.edu



# Overview

- The optical coatings in the current LIGO mirrors use **amorphous** materials
- Reducing thermal noise comes down to **reducing two-level systems** that are intrinsic to amorphous coatings
- Some successes are coming from:
  - Choice of coating materials
  - Elevated temperature deposition: mainly in *a*-Si
  - Post-deposition annealing
  - Doping material/percentage
  - Nano-layering



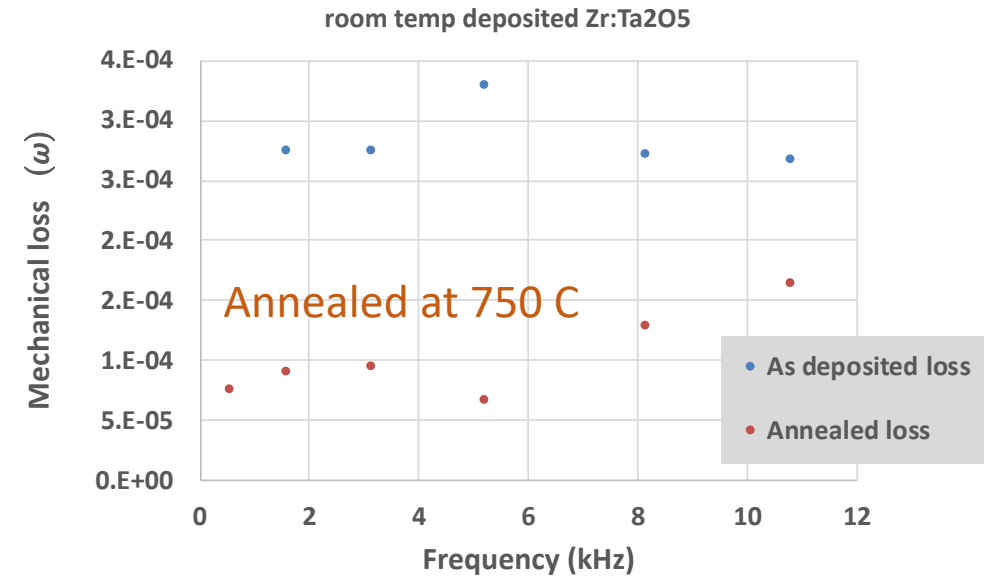
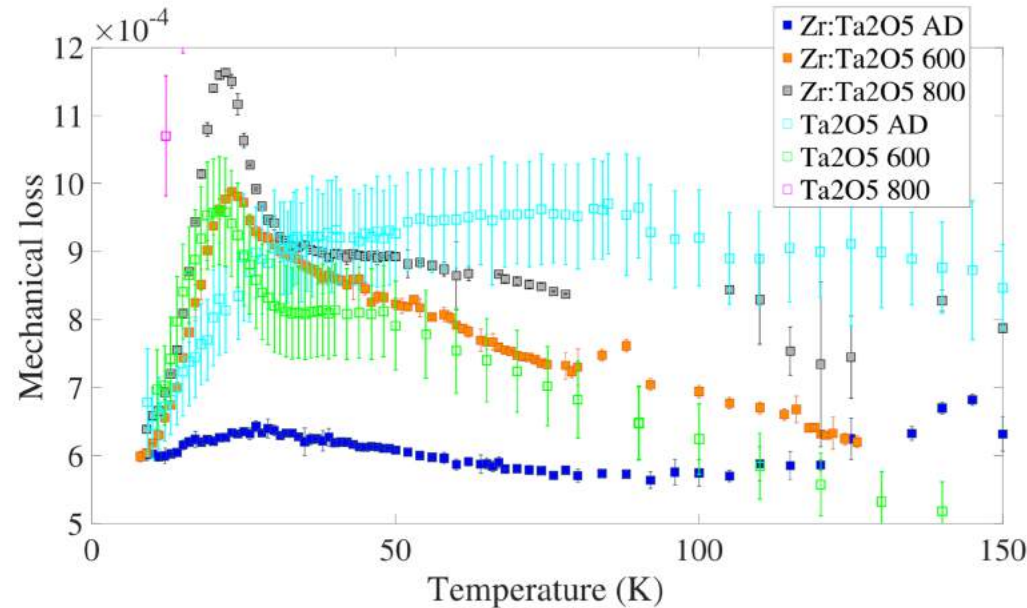
TLS in  $\alpha$ - $\text{Ta}_2\text{O}_5$   
Trinastic, PRB **93**, 014105 (2016)

# Plan of this talk

- Zirconia-doped-Tantala  
Insights from structural characterization
  
- Amorphous Si  
Vapor deposition simulations

# Zirconia-doped-Tantala

- Measured loss at room temperature decreases with annealing at higher temperatures



Source for both figures: G1800585-v3

- Doping with Zirconia suppresses crystallization:  
makes higher temperature (up to 900 C\*) annealing possible

\*According to G1800585-v3

# Pair Distribution Function (PDF)

- **Pair Distribution Function:**  
**Average position of atoms**

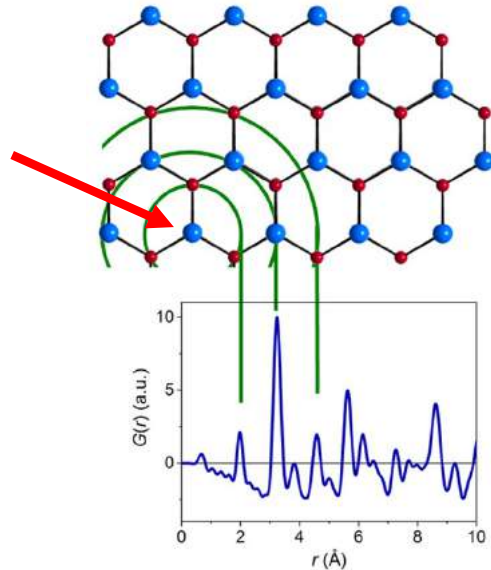
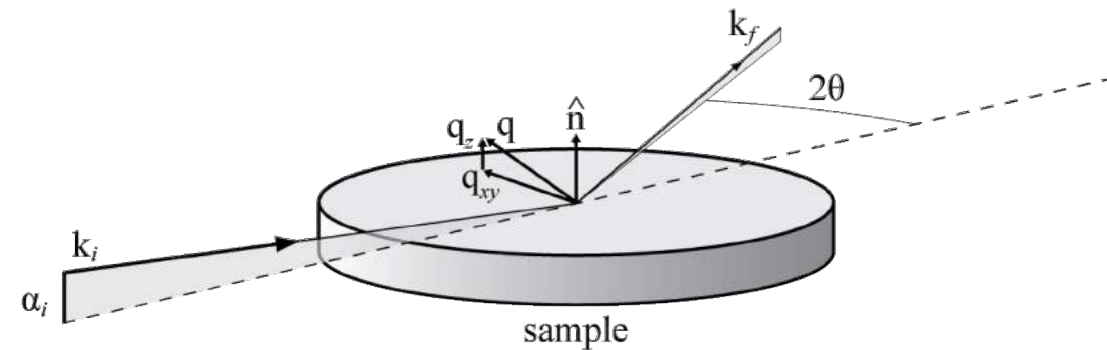


Figure: 2D Crystal for illustration

- **Connecting link** between experiments and modeling
- Experimentally measured as  
**Grazing Incidence Pair Distribution Function (GIPDF)**

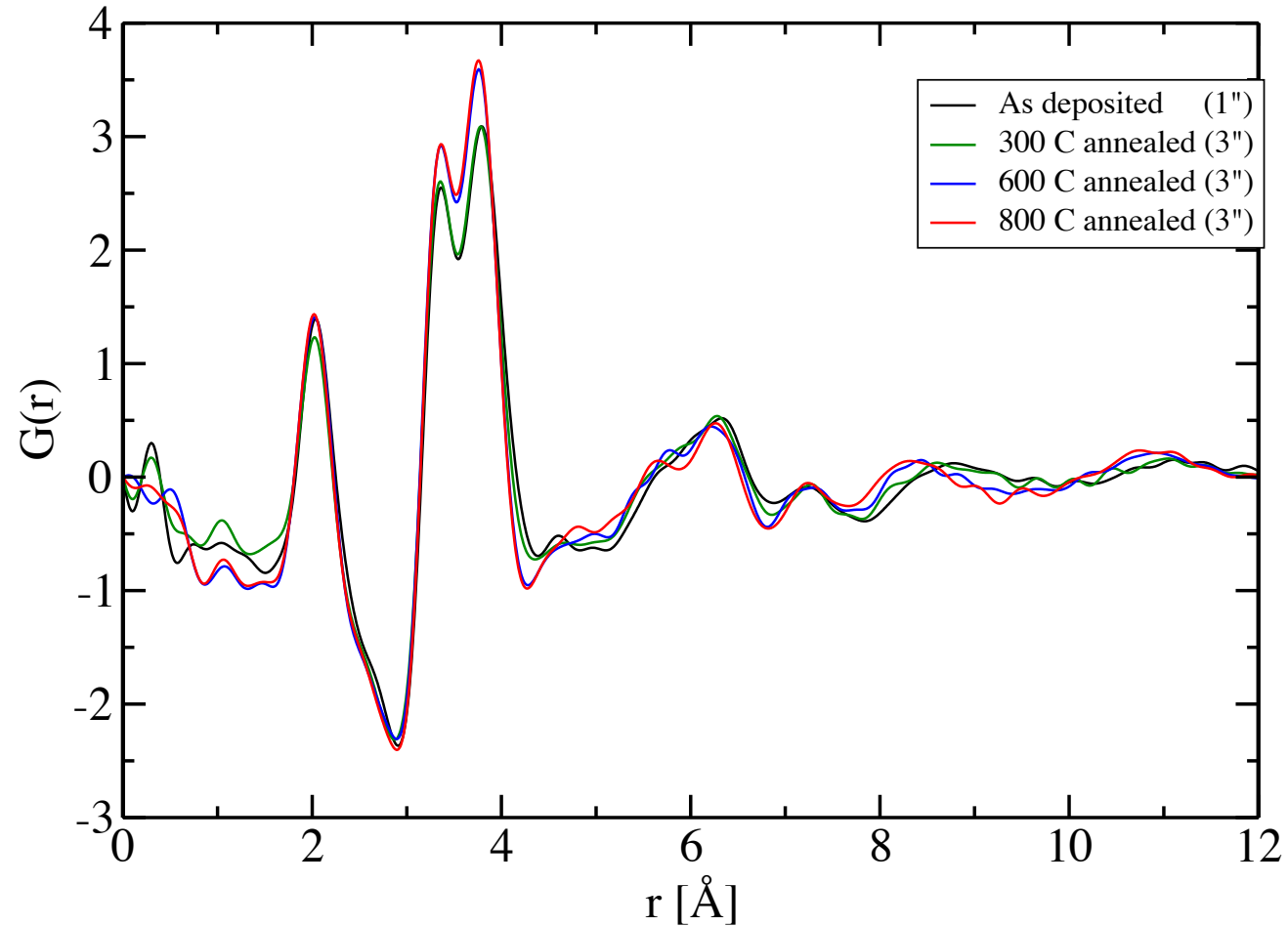


$$G(r) = \frac{1}{(2\pi)^3 \rho_0} \int_0^\infty 4\pi Q^2 F(Q) \frac{\sin Qr}{Qr} dQ$$

Figure source: [https://en.wikipedia.org/wiki/Grazing\\_incidence\\_diffraction](https://en.wikipedia.org/wiki/Grazing_incidence_diffraction)

Figure source: <http://www.mesostructures.uni-bayreuth.de/en/research/pair-distribution/index.html>

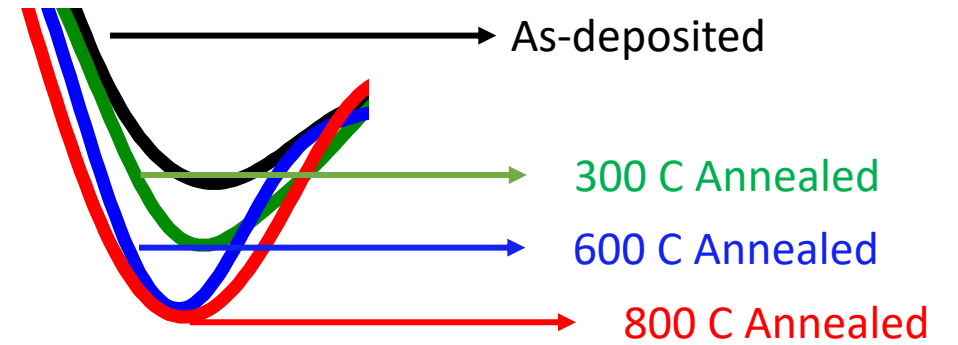
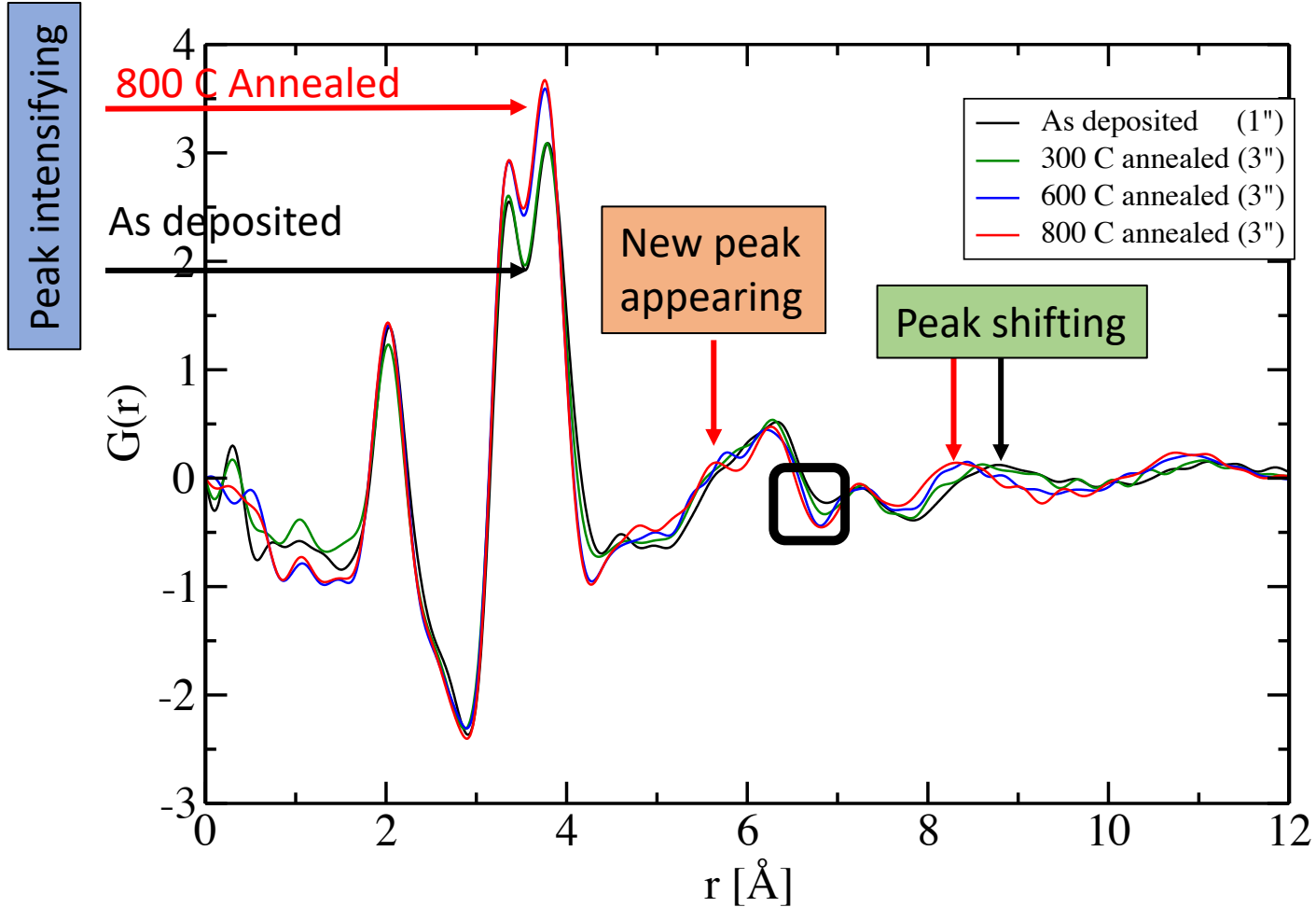
# Measured PDF of Zirconia-doped-Tantala



X-Ray GIPDF measurement on 35% Zirconia-doped-Tantala

SLAC National Accelerator Laboratory, October 2017

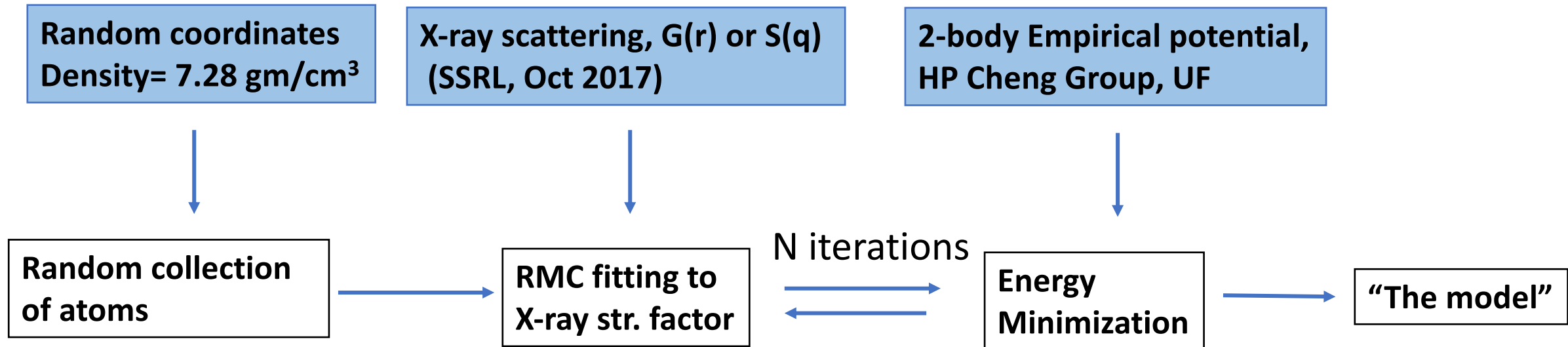
# Measured PDF of Zirconia-doped-Tantala



X-Ray GIPDF measurement on 35% Zirconia-doped-Tantala

SLAC National Accelerator Laboratory, October 2017

# Modeling of Zirconia-doped-Tantala

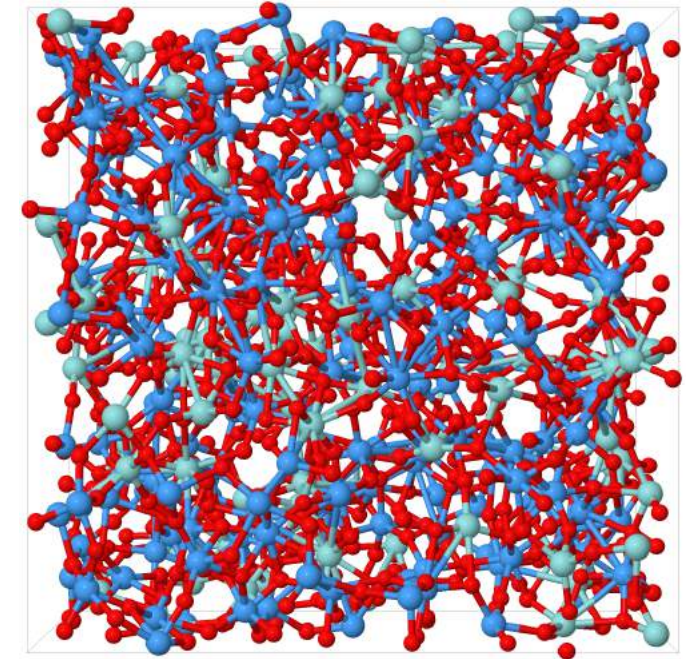
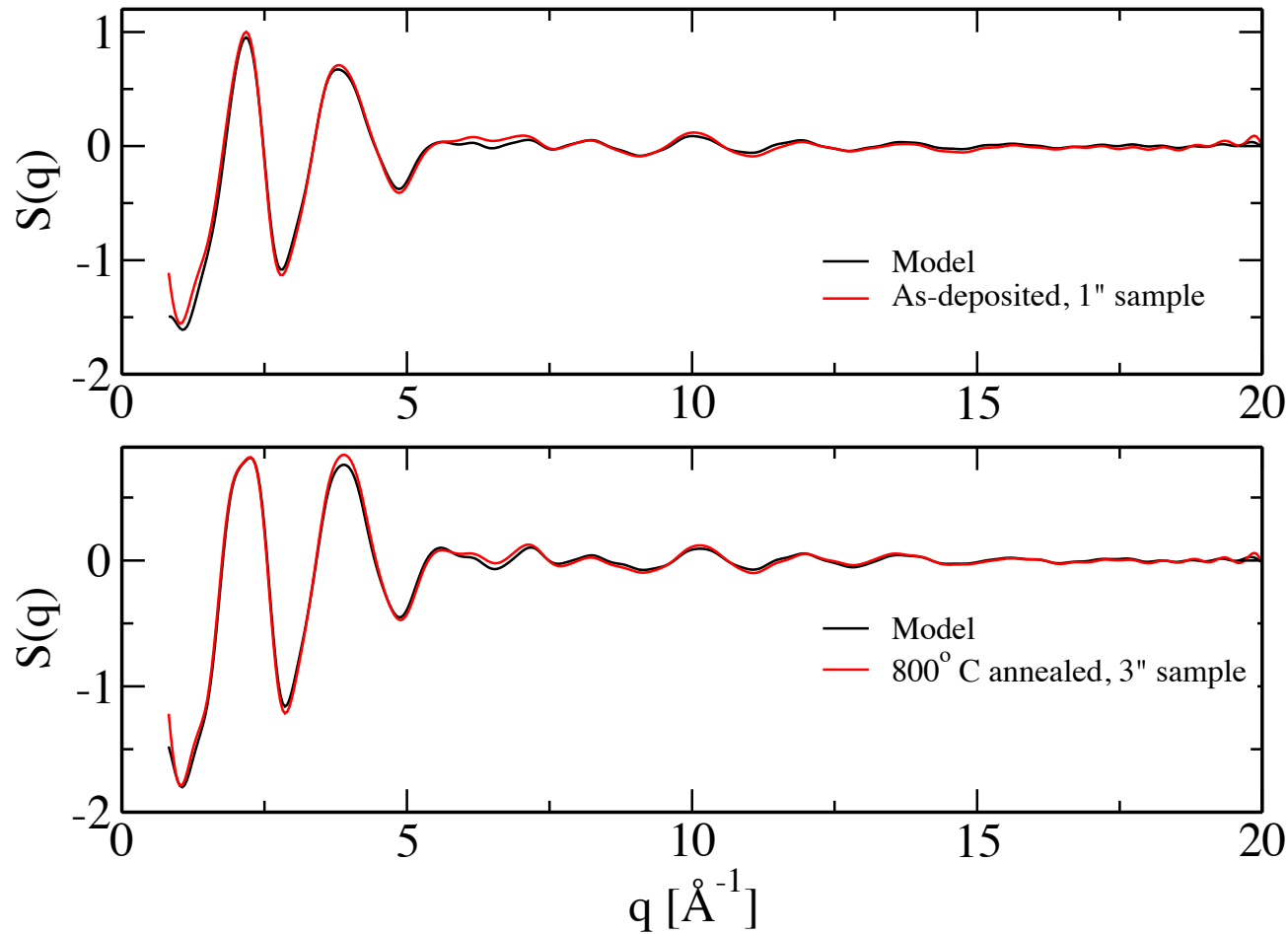


- 1064 atoms in all models,
- All results are averages over 100 models
- Density inferred from potential (Density measurements are underway!!)
- Fitting and minimization method:  
**FEAR**, Pandey, Biswas and Drabold, Scientific Reports **6:33731**, 2016



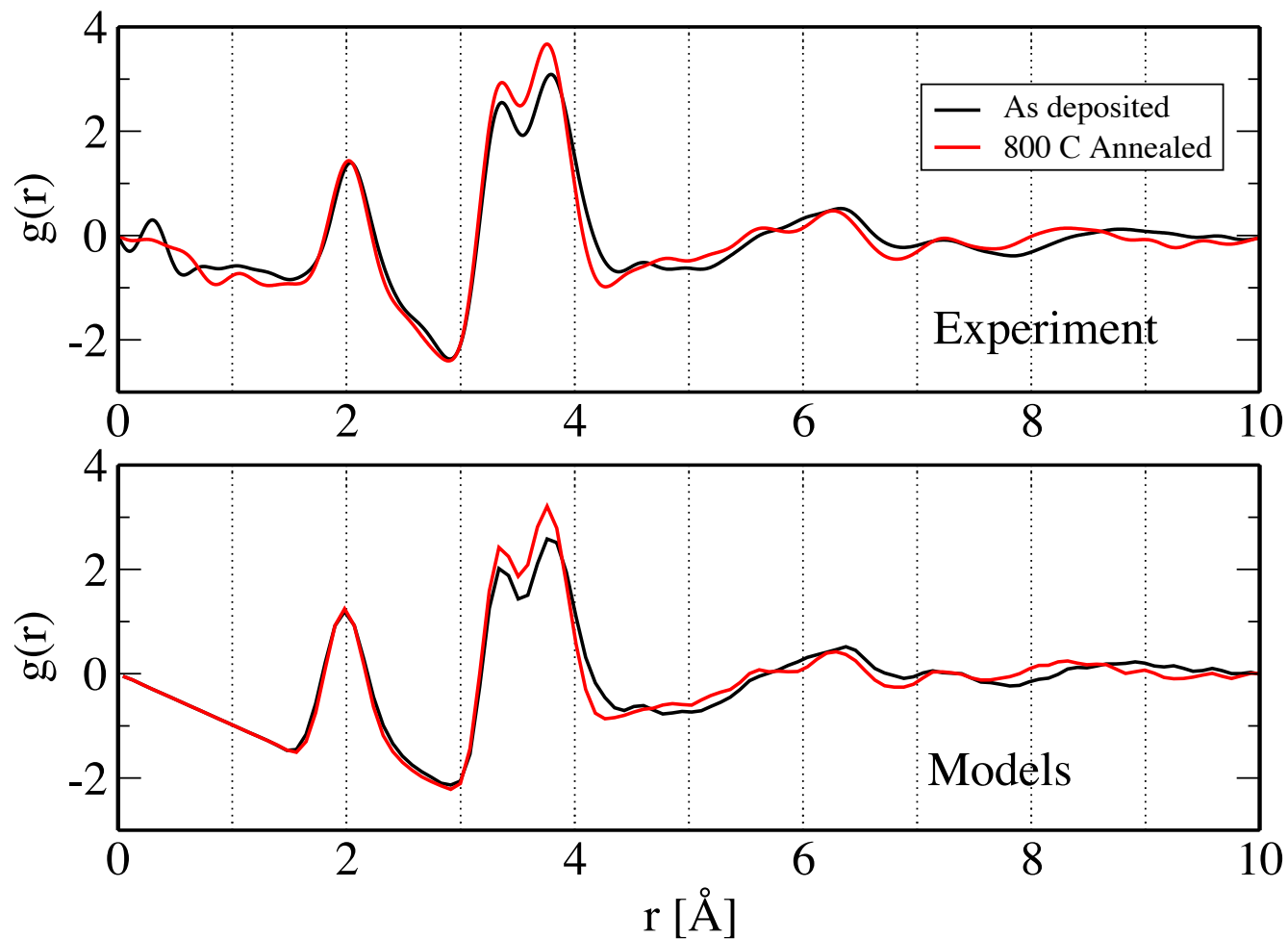
# Modeling of Zirconia-doped-Tantala

Atomic models fitted to x-ray structure factor  $S(q)$



Ball and Stick representation of final model

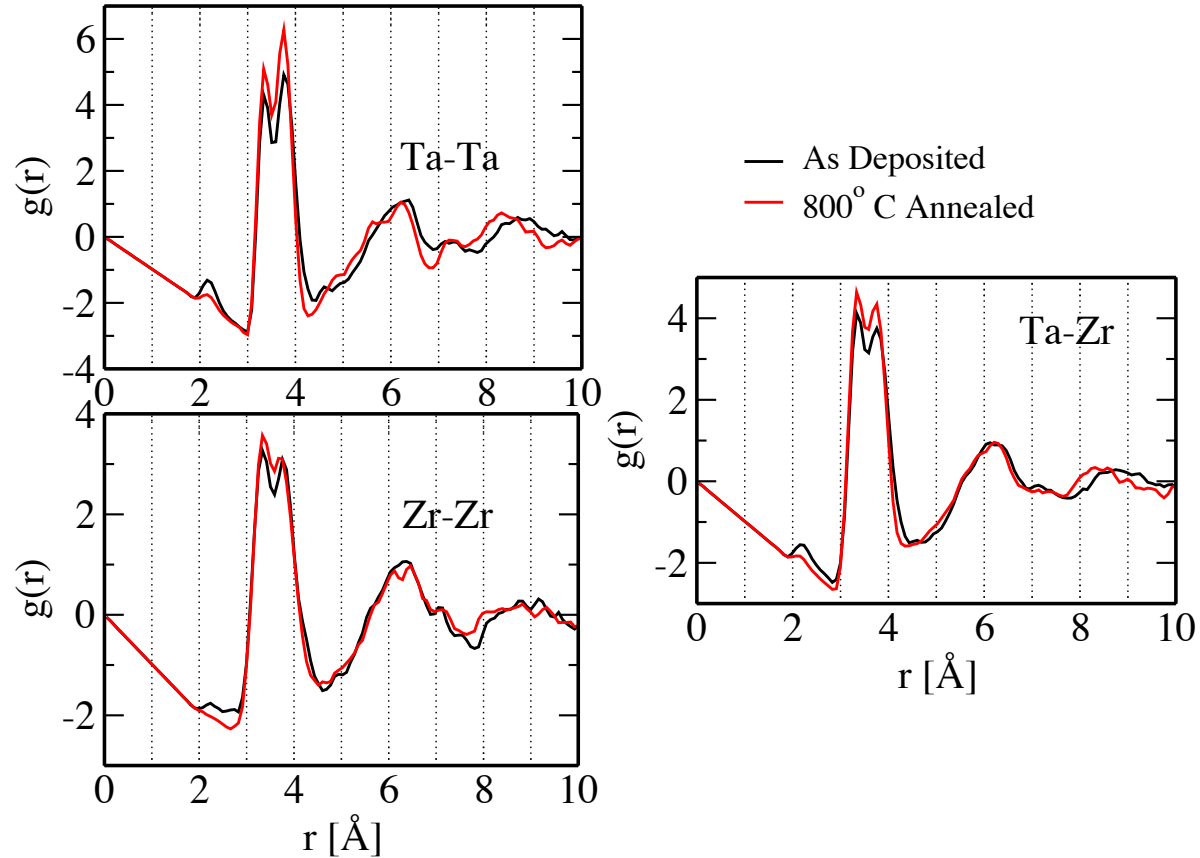
# Modeling of Zirconia-doped-Tantala



Models track the changes in experimental PDF very well

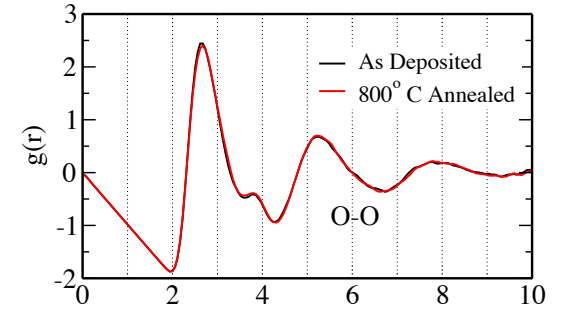
# Modeling of Zirconia-doped-Tantala

## Partial pair correlation functions

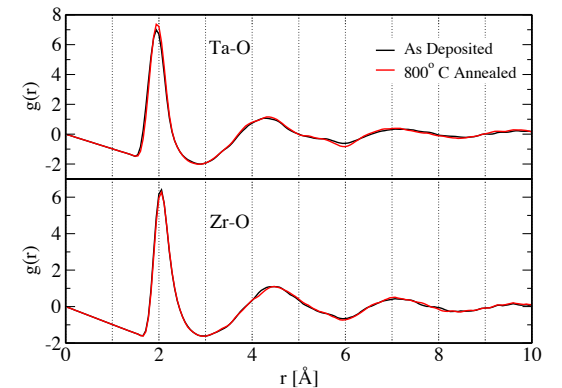


## Effect of annealing in Metal-Metal correlation

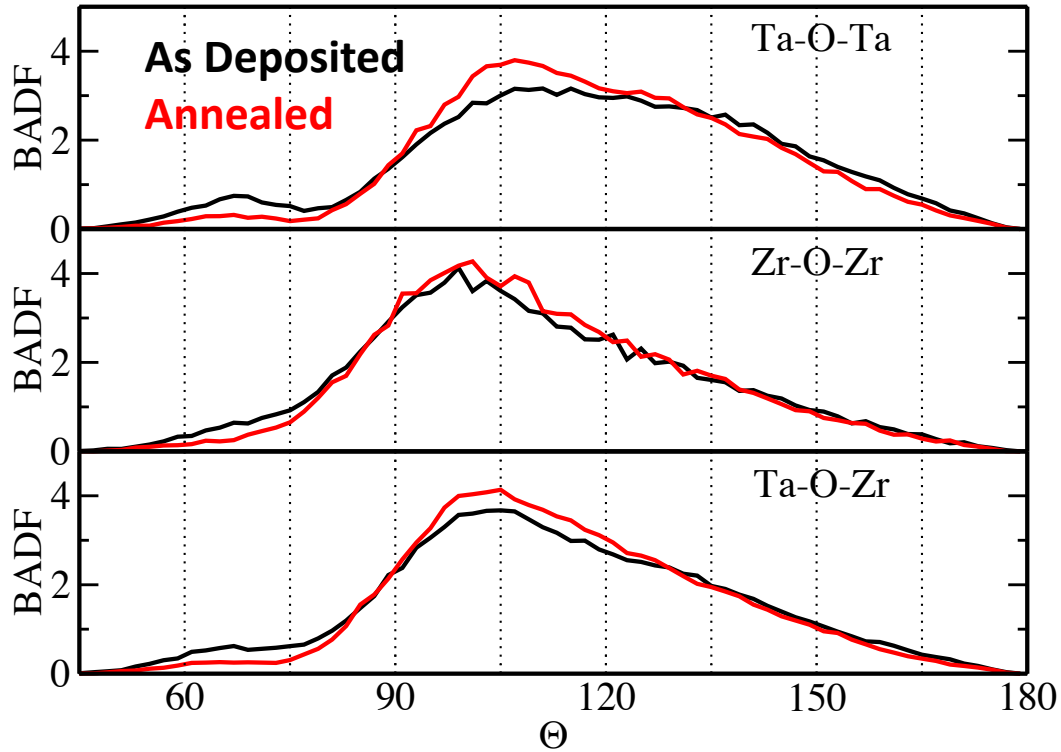
No major change in O-O correlation upon annealing.



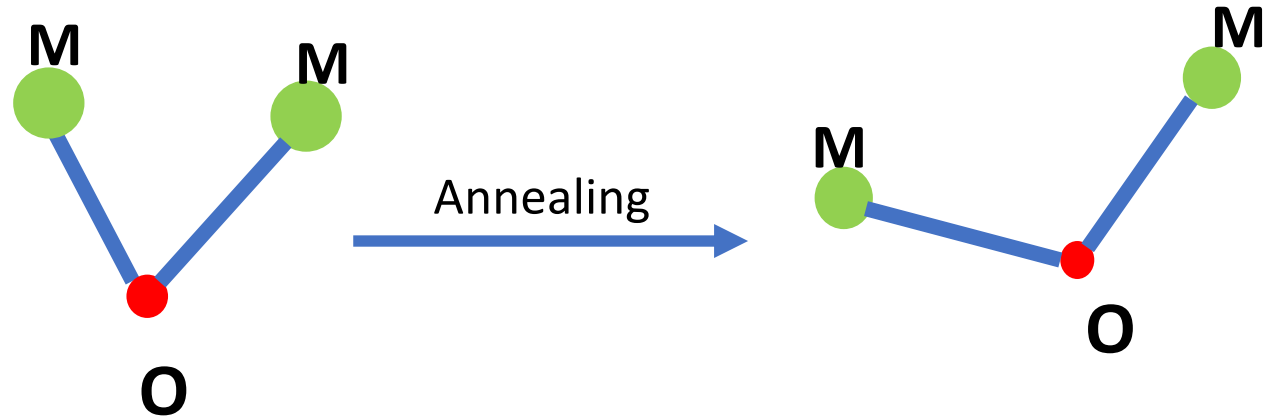
No major change in M-O correlation upon annealing.



# Modeling of Zirconia-doped-Tantala



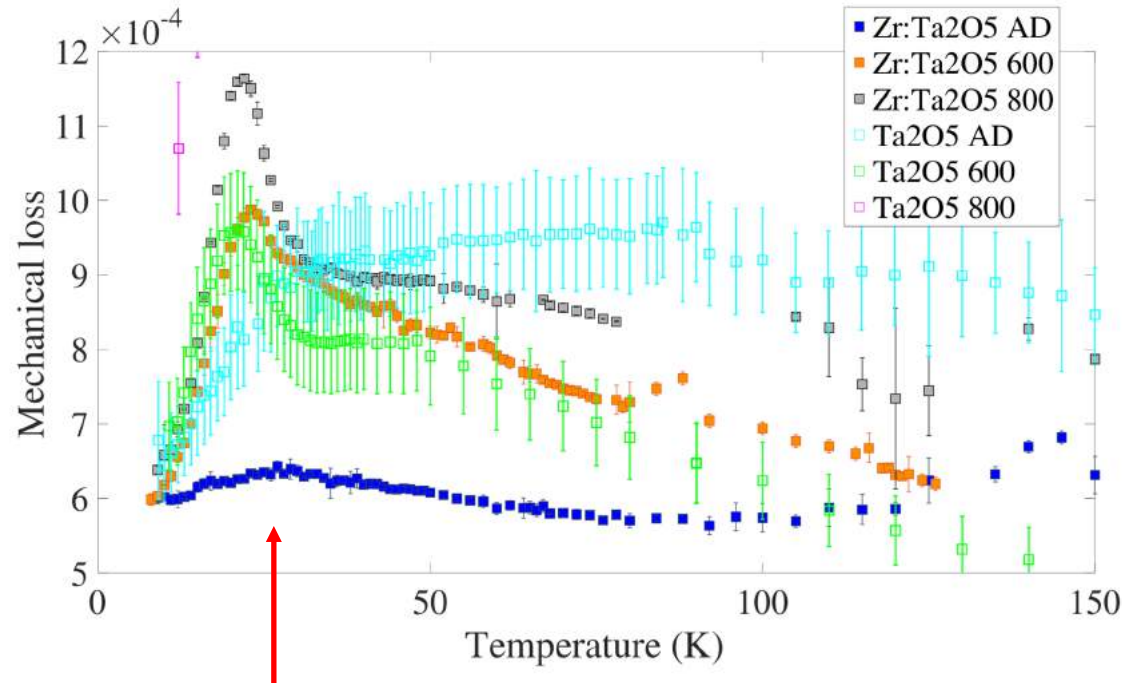
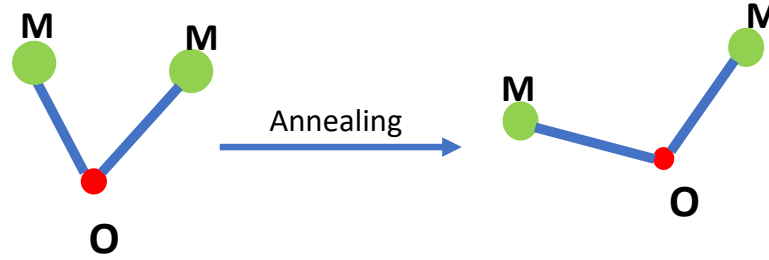
A simplified picture:



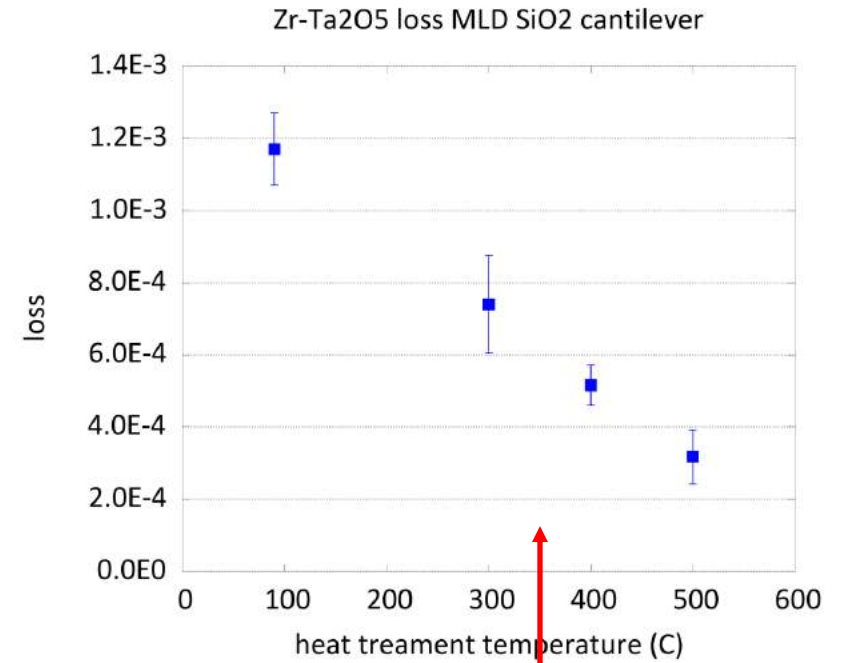
Bond angle distribution shows changes in M-O-M angles

# Modeling of Zirconia-doped-Tantala

**Loss mechanism hypothesis:**  
(Needs validation from two-level system analysis)



**Low barrier TLSs**  
**increase** upon annealing



**High barrier TLSs**  
**decrease** upon annealing

Source of both plots: G1800585-v3

# Modeling of Zirconia-doped-Tantala

## Next steps:

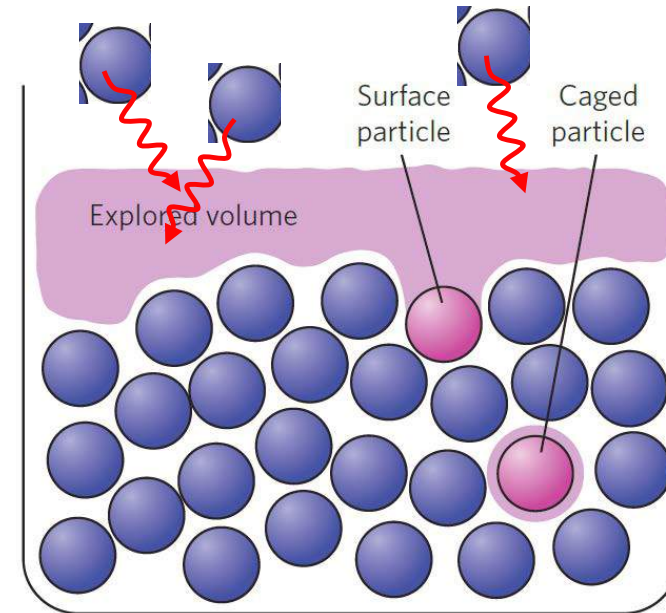
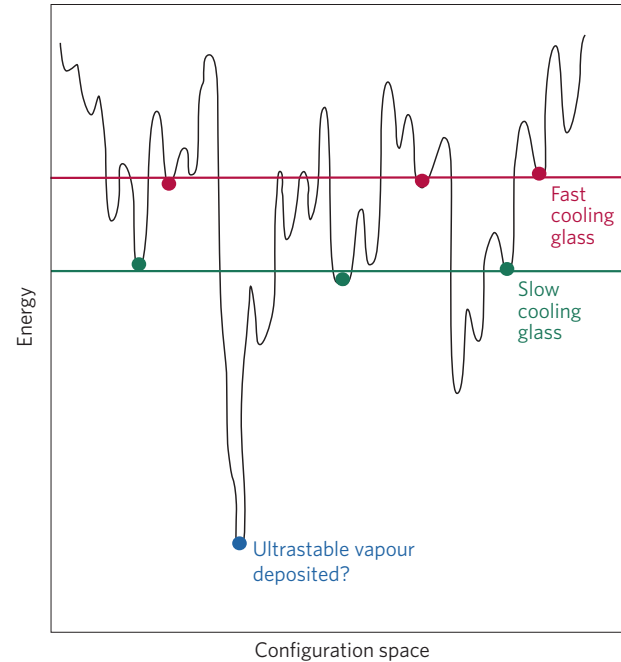
- Compute **two-level systems** and calculate **mechanical loss** (Team @ University of Florida is working on it!!)

See if the loss hypothesis holds.

- Search for dopants that can frustrate the two-level dynamics
- Continue study how  $\text{ZrO}_2$  doping inhibits crystallization in  $\text{Ta}_2\text{O}_5$ -  
**Initial results from caloric curve analysis consistent with observed frustration of crystallization by  $\text{ZrO}_2$  doping**

# Vapor deposition simulations

- Vapor deposition simulations mimic the coating deposition process



Figures from: Nature Mater. 12, 94 (2013)

- Aim: simulations can identify advantageous materials, dopants, substrate temperature, deposition rate



# Amorphous silicon

## Why choose a-Si for growth simulation?

- ➔ Ideal test case for vapor deposition simulation
  - Clear evidence of reduction in loss from experiments: E-beam deposited a-Si shows large drop in internal friction with high  $T_{\text{substrate}}$  deposition
  - Single atom type
  - Interatomic potentials for a-Si are more mature than those for oxides

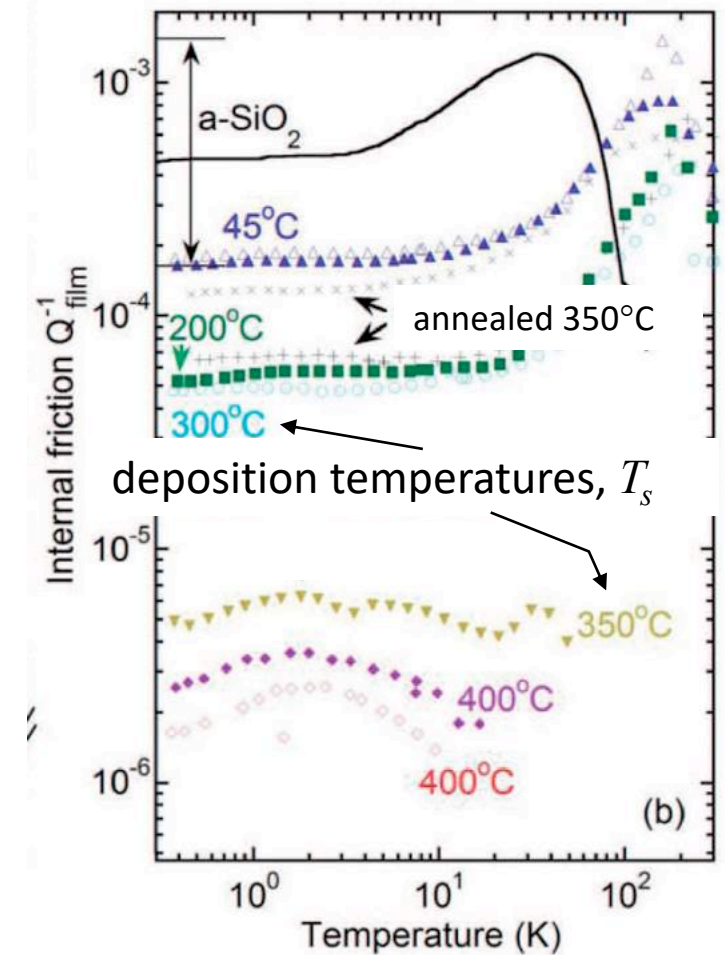
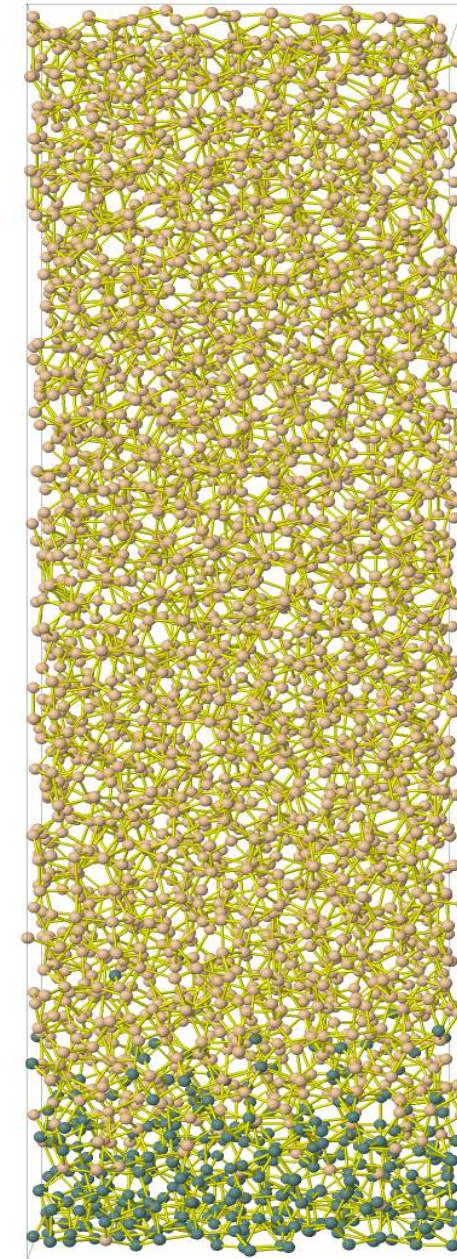
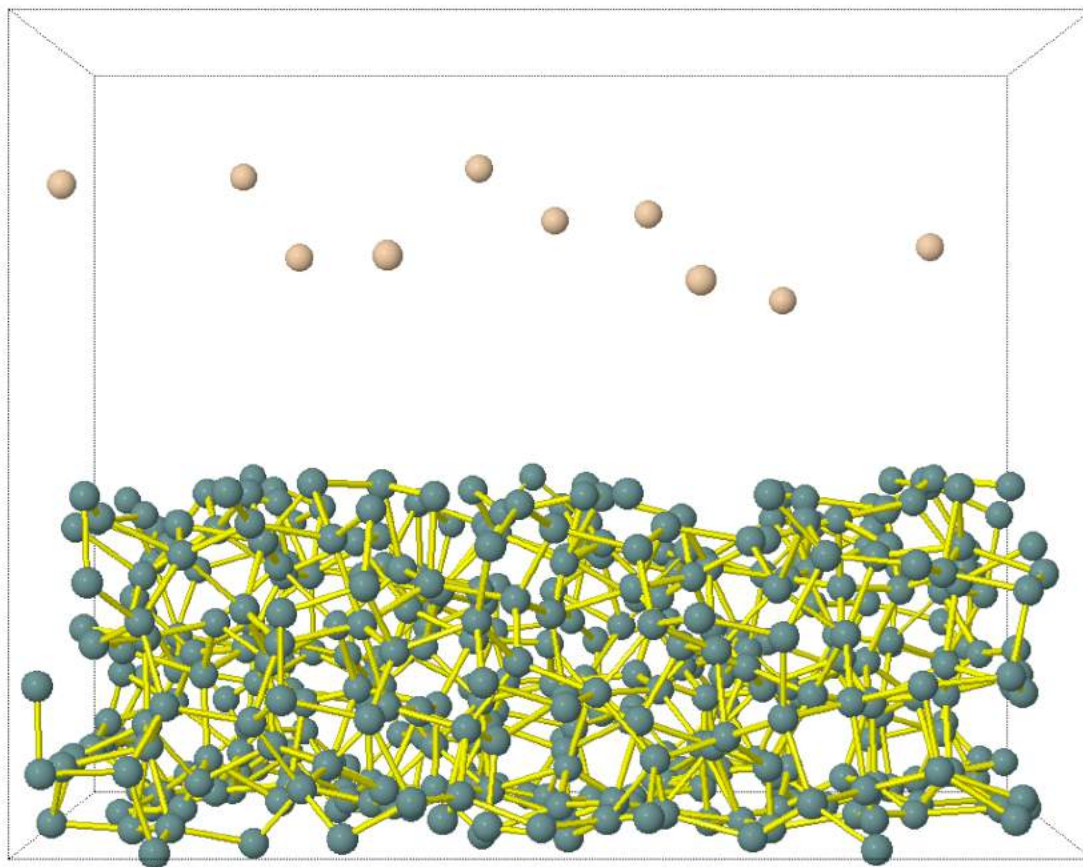


Figure reference:  
Liu et al, PRL **113**, 025503 (2014)

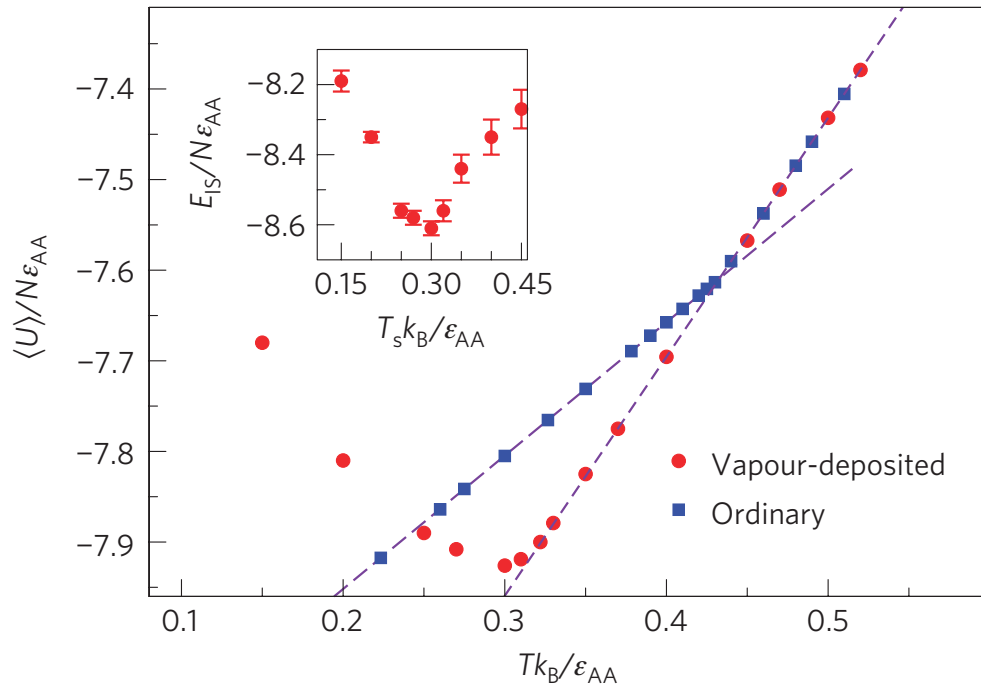


# Amorphous silicon growth simulations



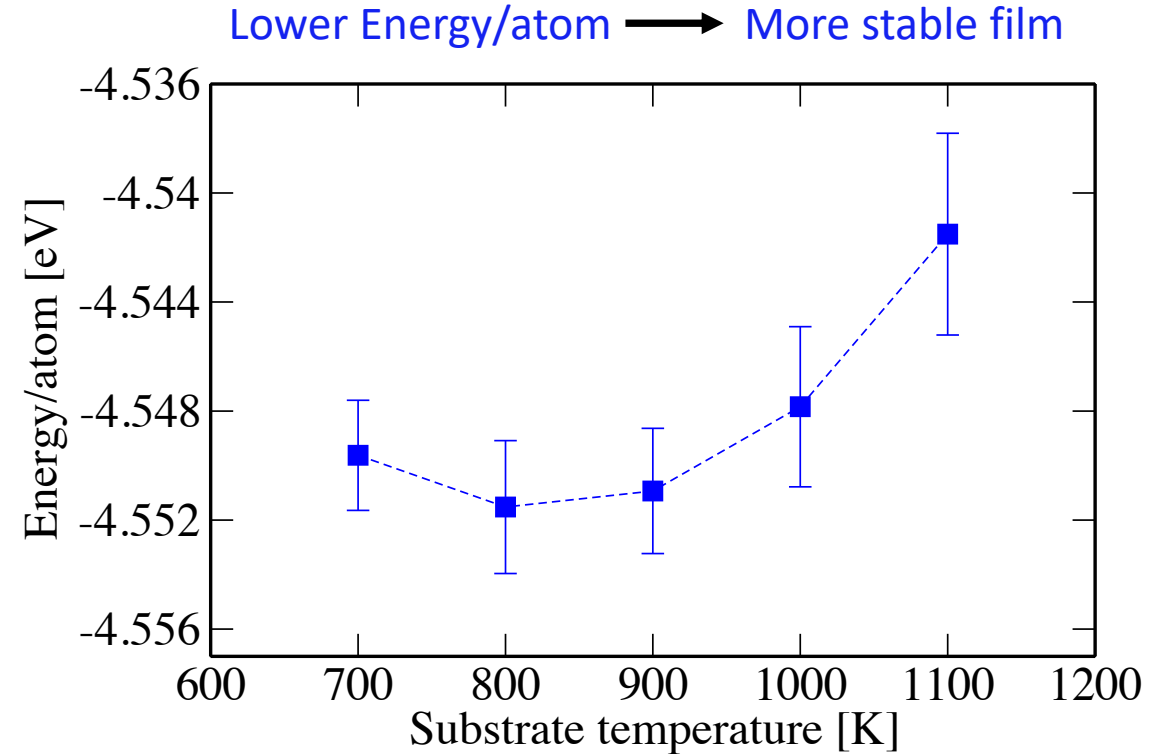
# Amorphous silicon growth simulations

Sweet spot for  $T_{\text{substrate}}$ : 85% of  $T_{\text{glass}}$ ?



Binary Lennard-Jones system

Source: Nature Materials **12.2** (2013)



Amorphous silicon

## Next steps: growth simulations

- Employ more accurate potential: Machine-learning based potentials are now available which are accurate as first principle calculations but scale  $\sim N$  in computational cost (*Bartók, Kermode, Bernstein and Csányi, arXiv:1805.01568*)
- Characterize models: voids, density profile, rings distribution, two-level systems and mechanical loss
- **Extend the simulations to oxides**  
*To model doping, substrate temperatures, mechanical loss and identify lower loss coatings*

# Summary

- X-ray scattering experiments have shown **clear trends of changes in short and medium range order** in the coatings with annealing.
- We have computer **models of coatings that capture the changes seen in samples** with annealing.
- Models indicate that **strained M-O-M bonds are being eliminated** because of annealing. We are awaiting further results from two-level system calculations
- Preliminary results from vapor deposition simulations of  $\alpha$ -Si show that **we can model the dependence of mechanical loss on substrate temperature**.
- More works are being done to **translate this knowledge into predicting the unknown:** better dopants, ideal substrate temperature *etc.*

# Center for Coatings Research

