



Refining the Search for Sub-threshold Lensed Gravitational Waves

LIGO SURF 2021

Storm Colloms

School of Physics and Astronomy, University of Edinburgh

Mentors: Alvin K. Y. Li,

Alan Weinstein

**LIGO Laboratory, California Institute of
Technology**

LIGO SURF 2021



Table of Contents

I. Background

Lensing?? Waveforms?? Sub-threshold??

II. Problem

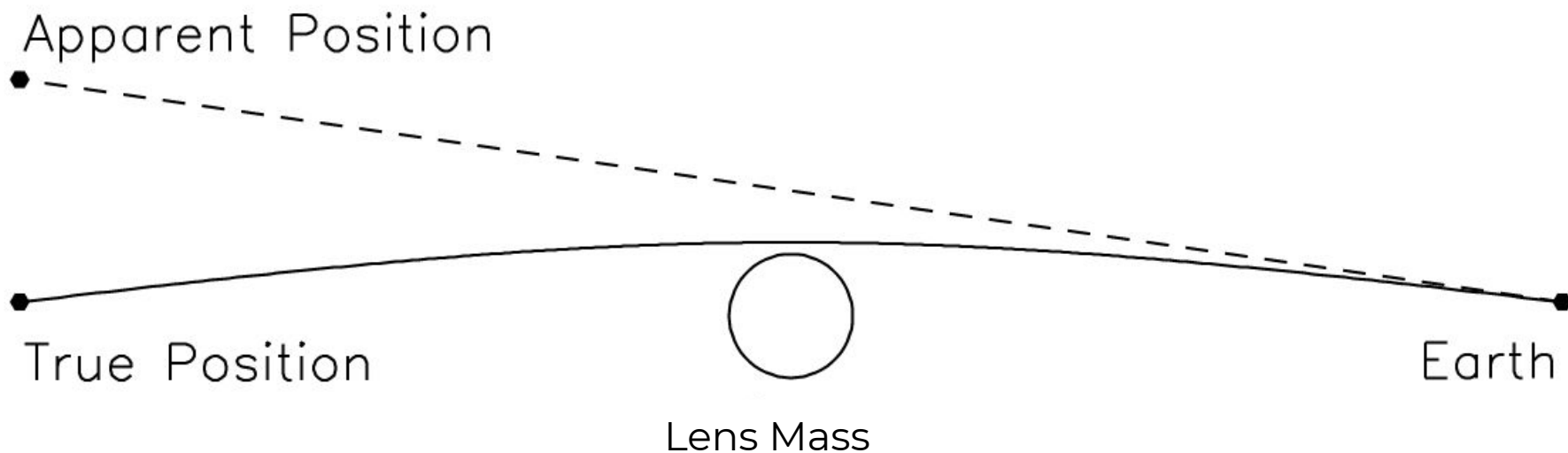
III. Solution

IV. What next

What is Gravitational Lensing?

Change in:

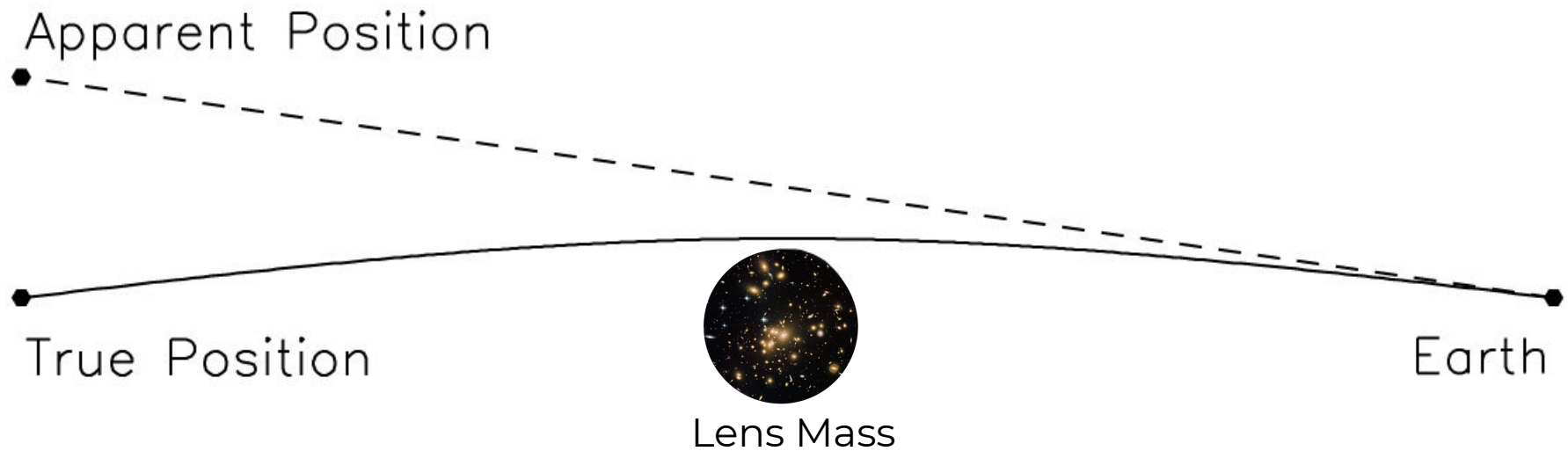
- apparent position



What is Gravitational Lensing?

Change in:

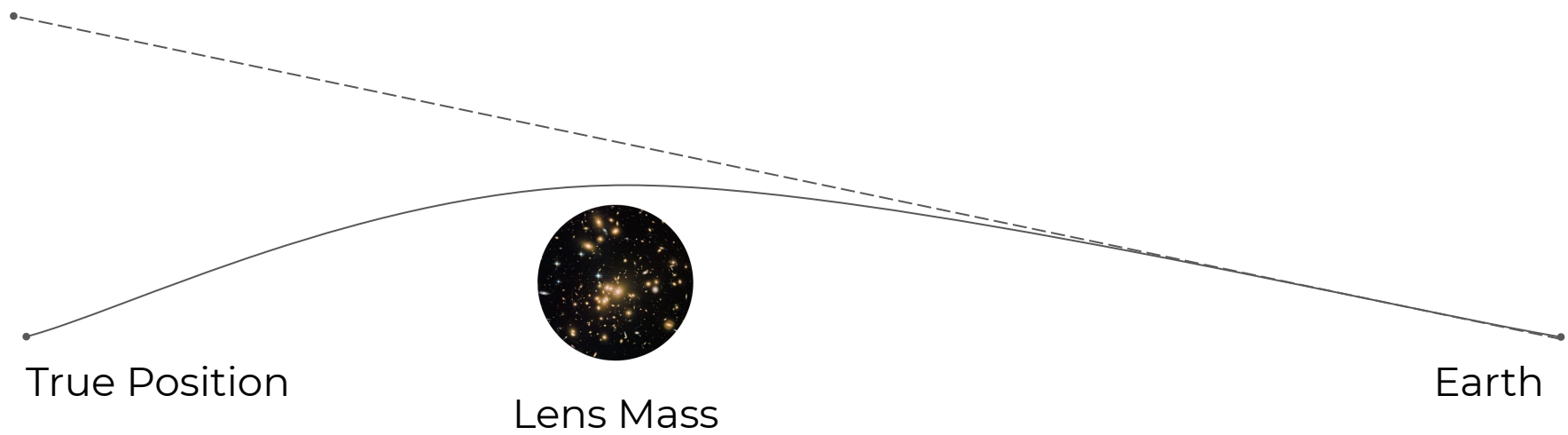
- apparent position



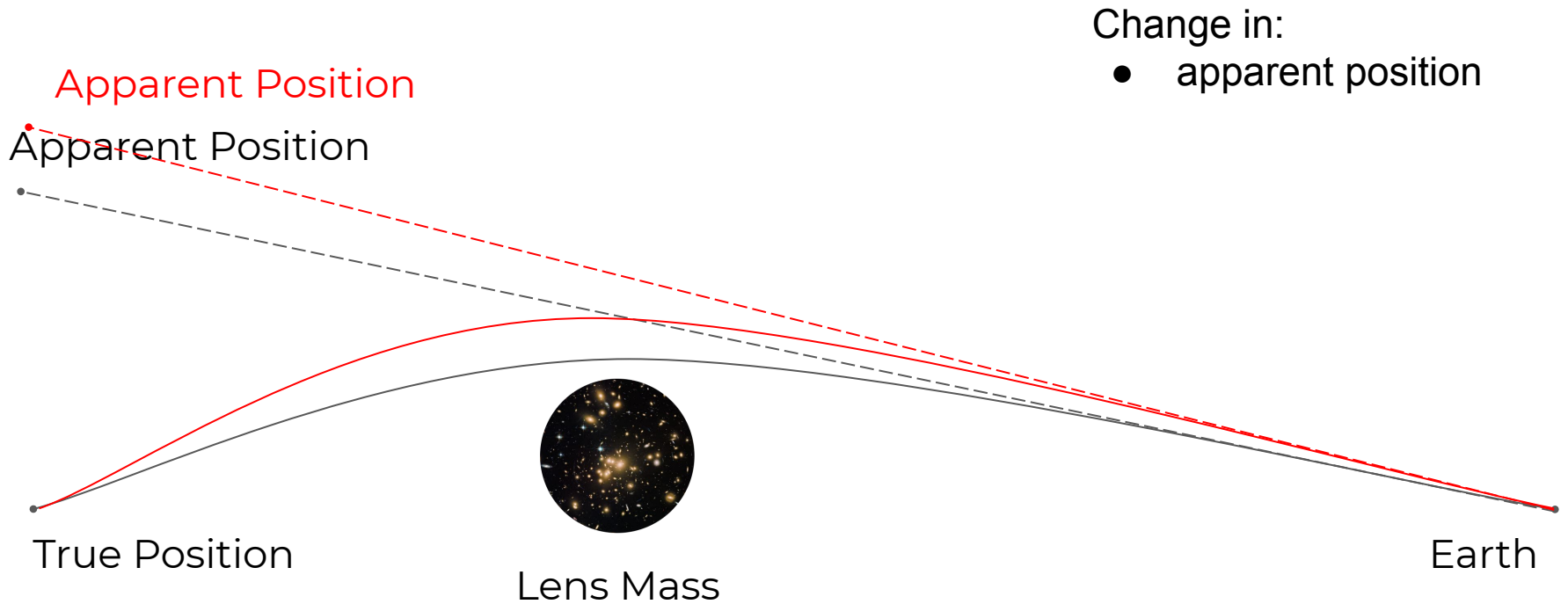
What is Gravitational Lensing?

- Change in:
- apparent position

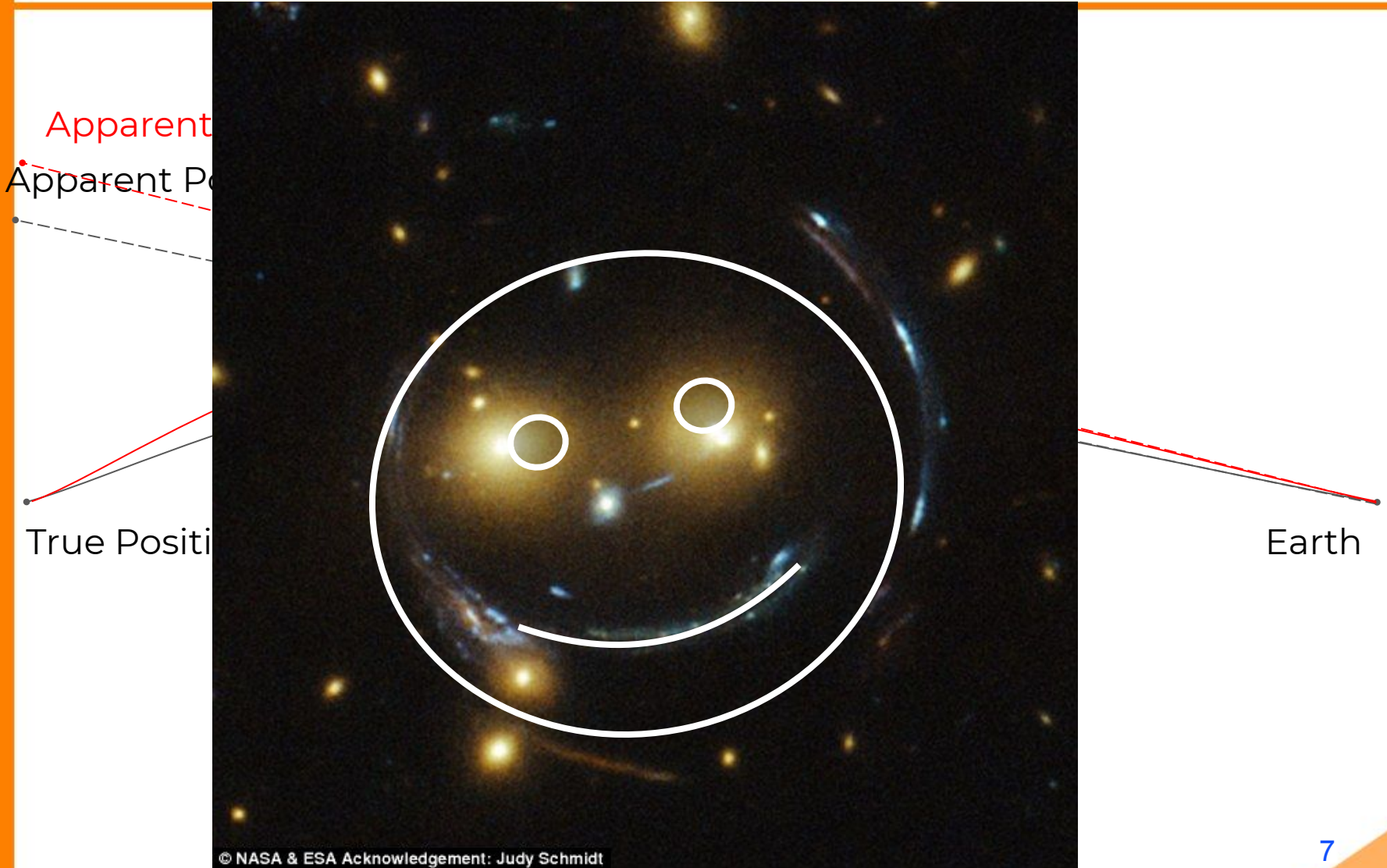
Apparent Position



What is Gravitational Lensing?



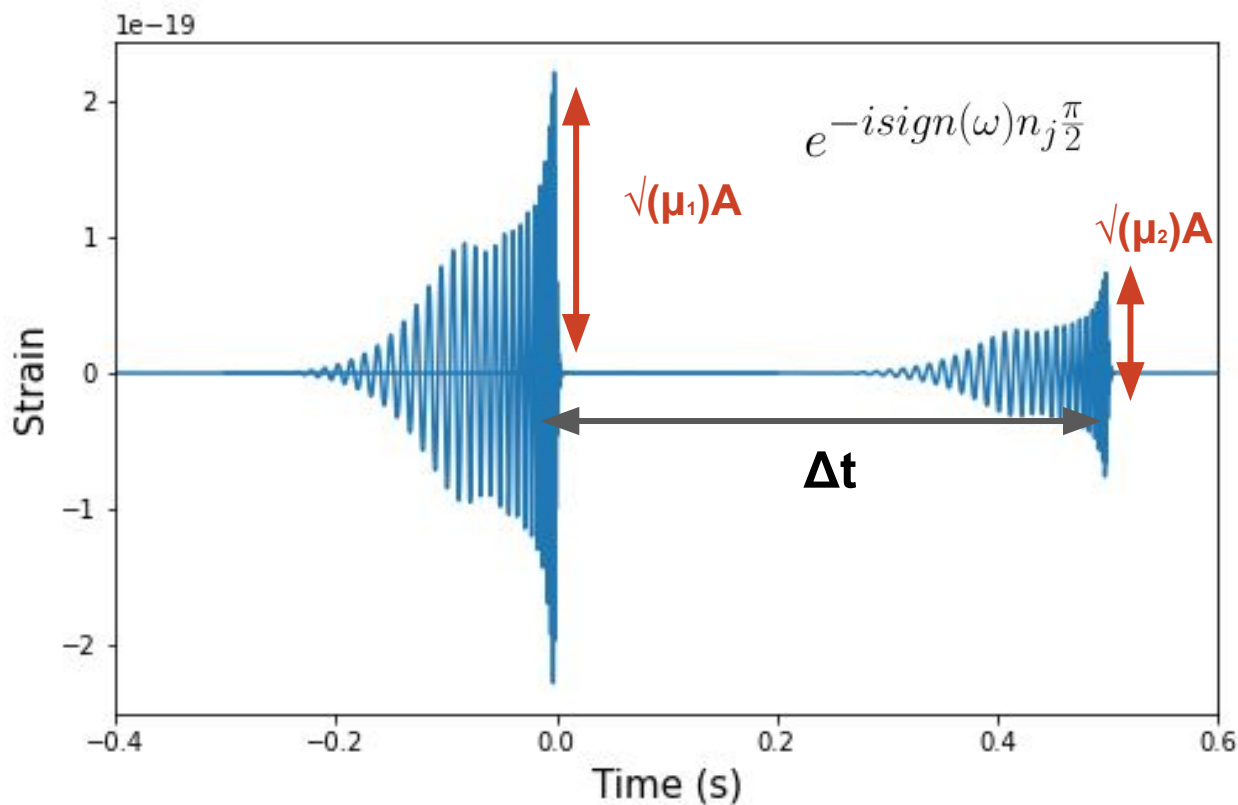
What is Gravitational Lensing?



What is Lensing Of GWs?

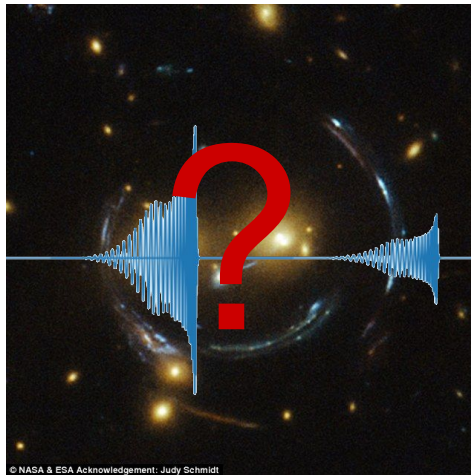
Change in:

- apparent position
- arrival time
- amplitude
- morse phase



Why look for Lensing of Gravitational Waves?

1. Not yet seen in Gravitational waves...



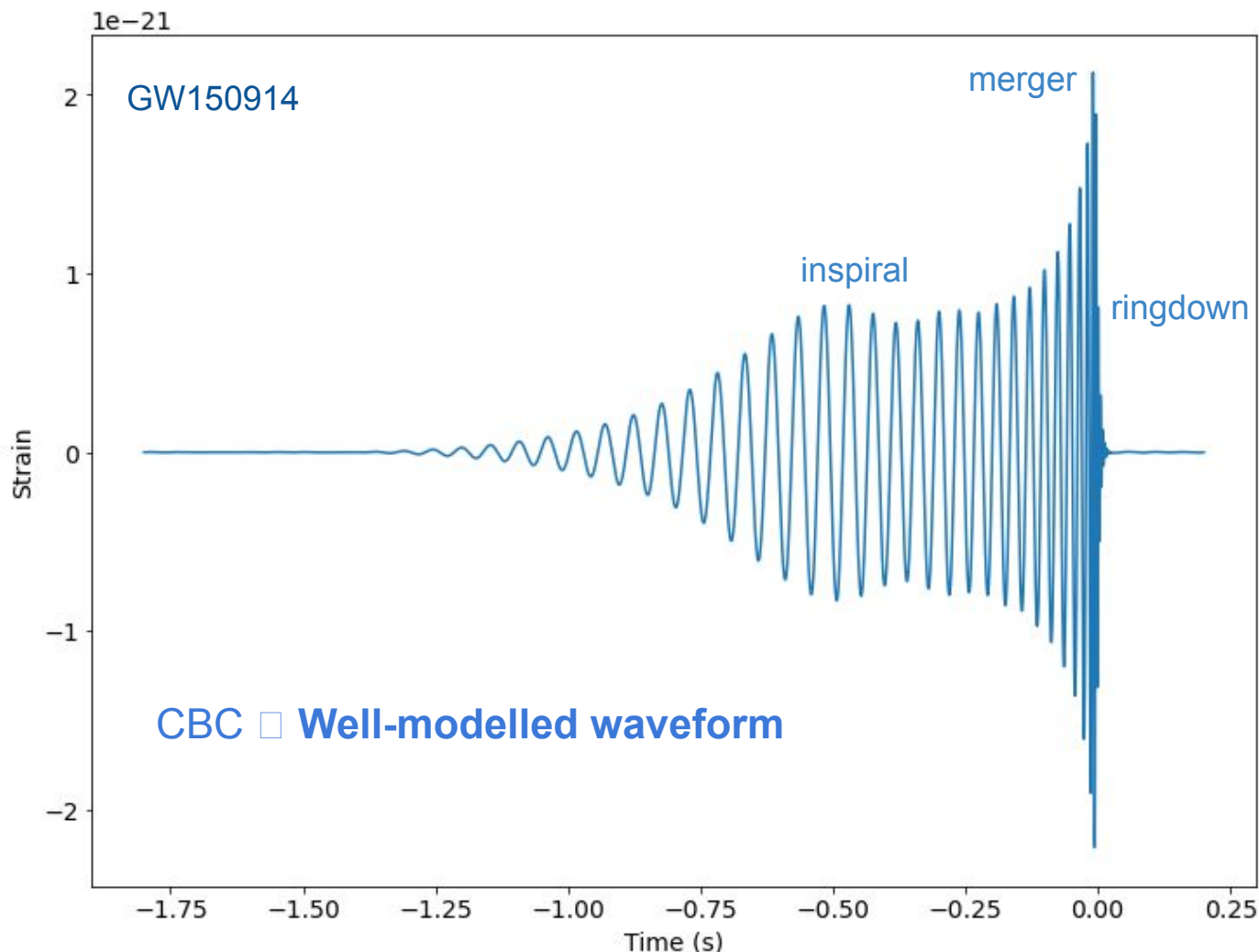
© NASA & ESA Acknowledgement: Judy Schmidt

2. Although everyone is looking...

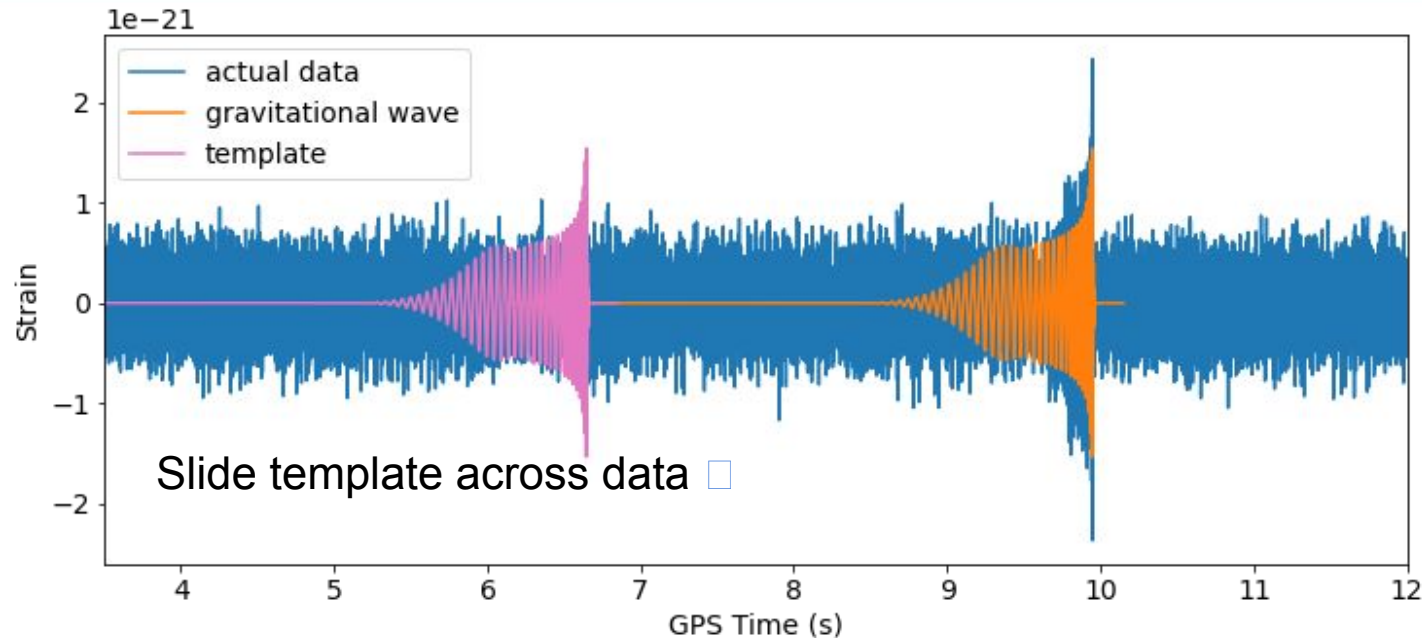
1. [arXiv:2106.12466](#) [pdf, other] [gr-qc](#) [astro-ph.HE](#) [astro-ph.IM](#)
Rapid Identification of Strongly Lensed Gravitational-Wave Events with Machine Learning
Authors: Srashti Goyal, Harikrishnan D., Shasvath J. Kapadia, Parameswaran Ajith
Abstract: A small fraction of the **gravitational...** [▽ More](#)
 Submitted 23 June, 2021; originally announced June 2021.
 Comments: 11 pages, 6 figures
2. [arXiv:2106.09630](#) [pdf, other] [gr-qc](#) [astro-ph.HE](#)
Lensing of Gravitational Waves as a Novel Probe of Graviton Mass
Authors: Ka-Wai Chung, Tjonnie Guang Feng Li
Abstract: The diffraction patterns of **lensed...** [▽ More](#)
 Submitted 17 June, 2021; originally announced June 2021.
 Comments: 6 pages, 4 figures
 Report number: KCL-PH-TH 2021/41, LIGO Document number of P2100192-v2
5. [arXiv:2106.06545](#) [pdf, other] [gr-qc](#) [astro-ph.CO](#)
Evidence for lensing of gravitational waves from LIGO-Virgo
Authors: Jose M. Diego, Tom Broadhurst, George Smoot
Abstract: Recently, the LIGO-Virgo Collaboration (LVC) concluded that there is no evidence for **lensed gravitational waves** (GW) in the first half of the run, claiming "We find the observation of **lensed** events to be unlikely, with the fractional... [▽ More](#)
 Submitted 11 June, 2021; originally announced June 2021.
 Comments: 7 pages with 2 figures
6. [arXiv:2106.06303](#) [pdf, other] [astro-ph.HE](#) [gr-qc](#)
Beyond the detector horizon: Forecasting gravitational-wave strong lensing
Authors: A. Renske A. C. Wierda, Ewoud Wempe, Otto A. Hannuksela, Léon V. E. Koopmans, Chris Van Den Broeck
Abstract: When **gravitational...** [▽ More](#)
 Submitted 22 June, 2021; v1 submitted 11 June, 2021; originally announced June 2021.
9. [arXiv:2106.00392](#) [pdf, other] [gr-qc](#) [astro-ph.CO](#) [astro-ph.GA](#) [astro-ph.HE](#)
Impact of astrophysical binary coalescence timescales on the rate of lensed gravitational wave events
Authors: Suvodip Mukherjee, Tom Broadhurst, Jose M. Diego, Joseph Silk, George F. Smoot
Abstract: The expected event rate of **lensed gravitational wave** sources scales with the merger rate at redshift $z \geq 1$, where the optical depth for **lensing** is high. It is commonly assumed that the merger rate of the astrophysical compact objects is... [▽ More](#)
 Submitted 1 June, 2021; originally announced June 2021.
 Comments: 10 pages, 6 figures
10. [arXiv:2105.14390](#) [pdf, other] [astro-ph.CO](#) [astro-ph.GA](#) [astro-ph.HE](#)
Please repeat: Strong lensing of gravitational waves as a probe of compact binary and galaxy populations
Authors: Fel Xu, Jose Maria Ezquiaga, Daniel E. Holz
Abstract: Strong **gravitational...** [▽ More](#)
 Submitted 29 May, 2021; originally announced May 2021.
 Comments: 26 pages, 13 figures
11. [arXiv:2105.07011](#) [pdf, other] [astro-ph.GA](#)
Event rate predictions of strongly lensed gravitational waves with detector networks and more realistic templates
Authors: Lilan Yang, Shichao Wu, Kai Liao, Xuheng Ding, Zhiqiang You, Zhoujian Cao, Marek Biesiada, Zong-Hong Zhu

3. Can constrain important values for cosmology and the structure of the local Universe...

What is a **Waveform**?

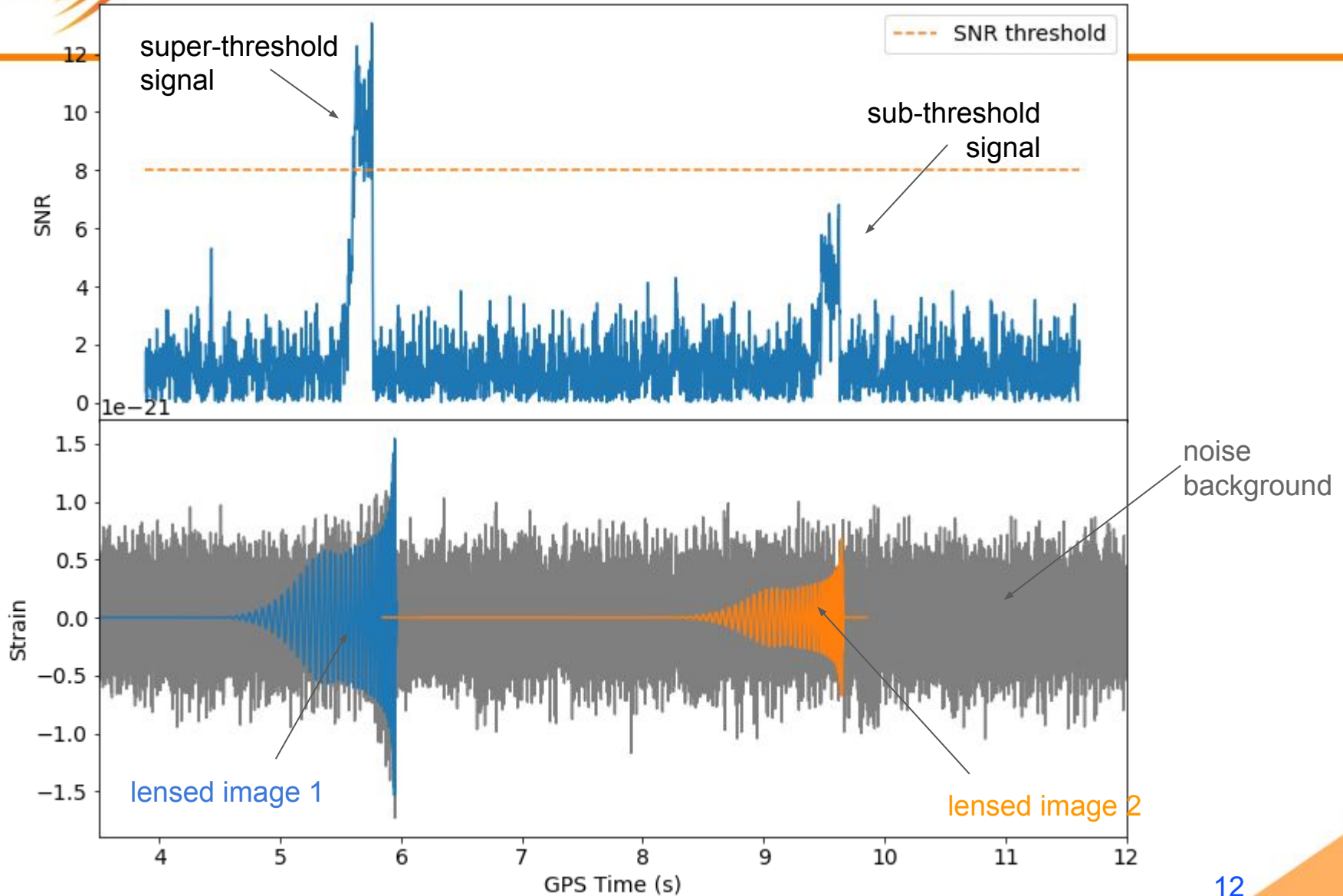


What is a Matched Filtering?

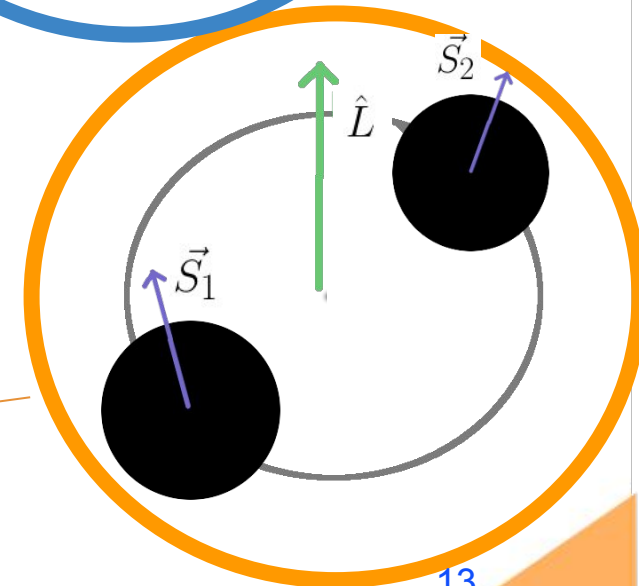
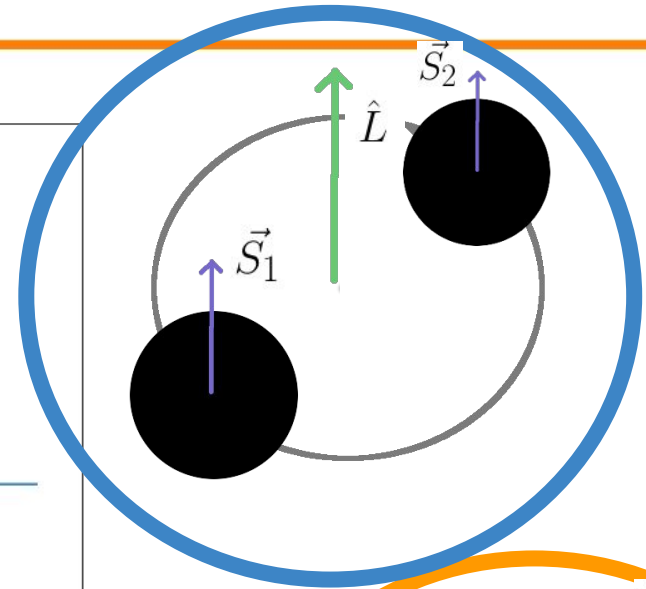
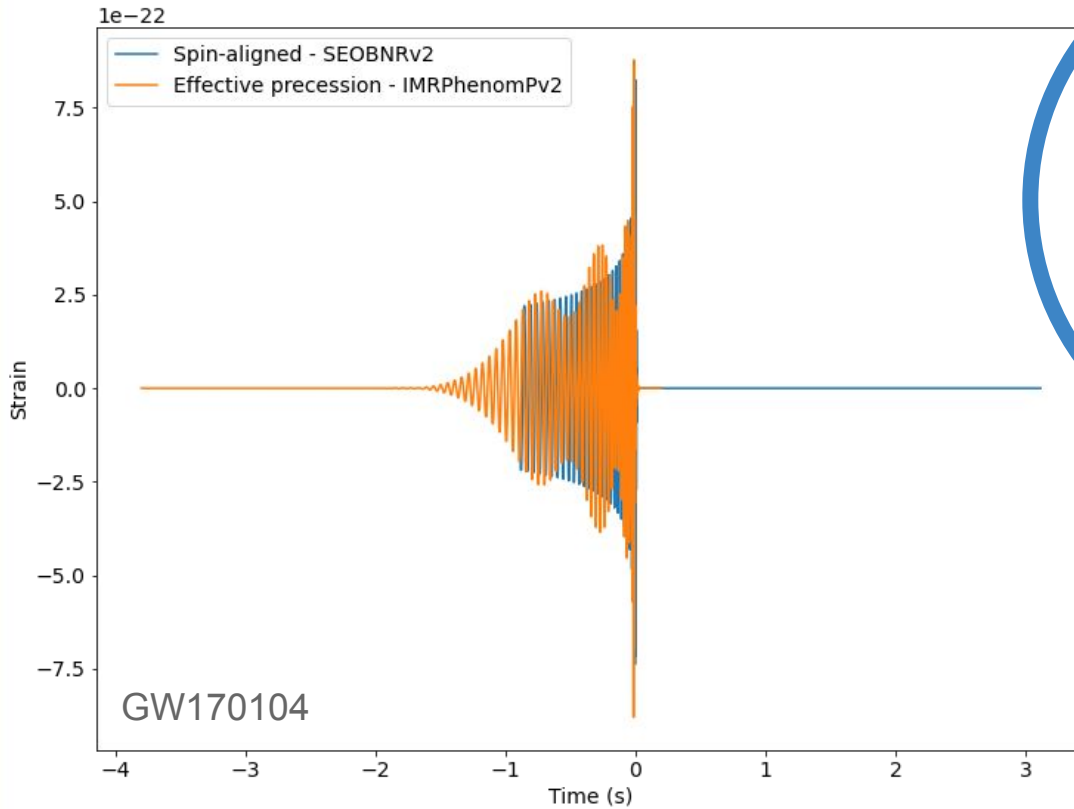


Measure the **correlation** between data and template to get **SNR**

What is Sub-threshold?



What is a waveform family?



amplitude and frequency modulation

What is a waveform family?

Spin Aligned, e.g. SEOBNRv2, IMRPhenomD

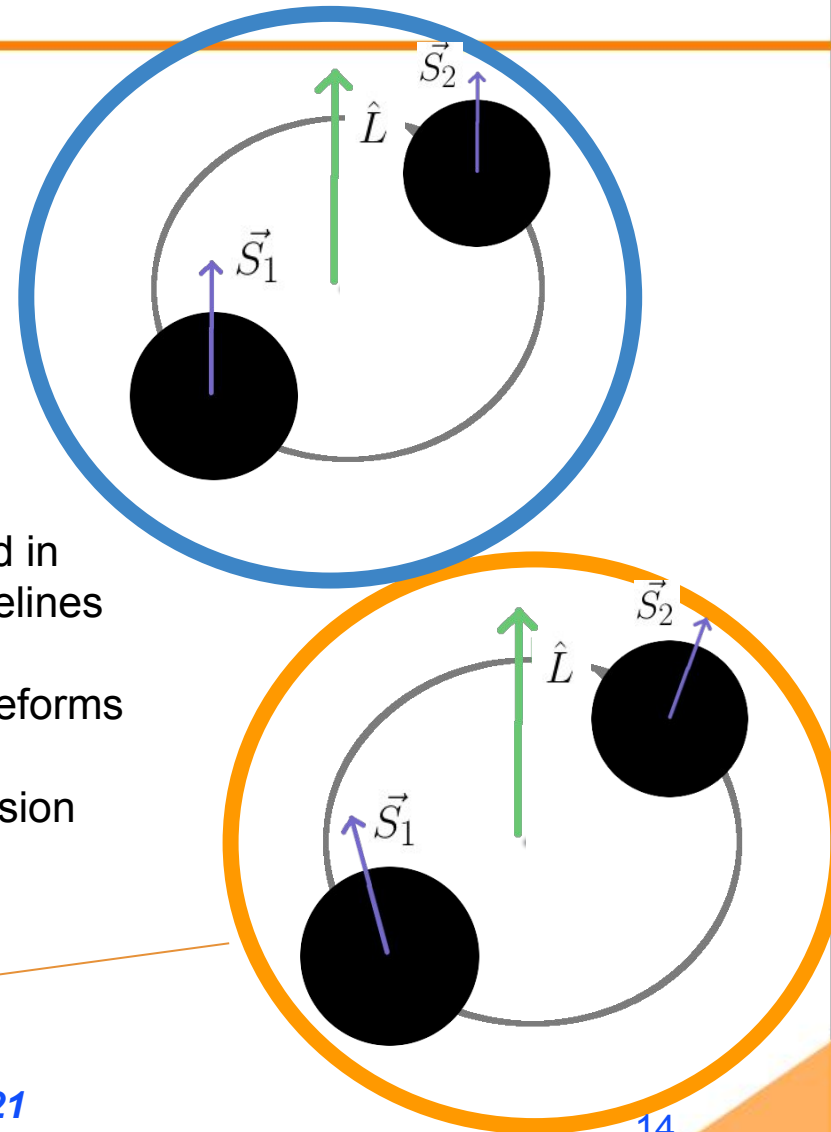
Can include Precession, e.g. IMRPhenomPv2

□ Different waveform families used in different sub-threshold lensing pipelines

GstLAL pipeline: spin-aligned waveforms

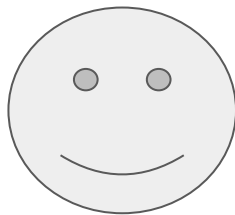
PyCBC pipeline: considers precession

amplitude and frequency modulation

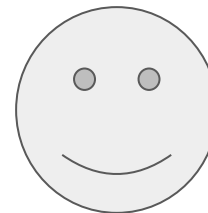


What is the motivation?

"You might lose potential candidates due to the waveform families you are using in the pipeline!"



"You should consider the differences between waveform families!"





What is reality?

- All **O1, O2, and O3a super-threshold events** have been **recovered** from sub-threshold lensing searches with both **spin-aligned** and **precessing** waveforms
 - Evidence that the waveform family does not alter the chances of detecting a **super-threshold** gravitational wave



What am I doing?

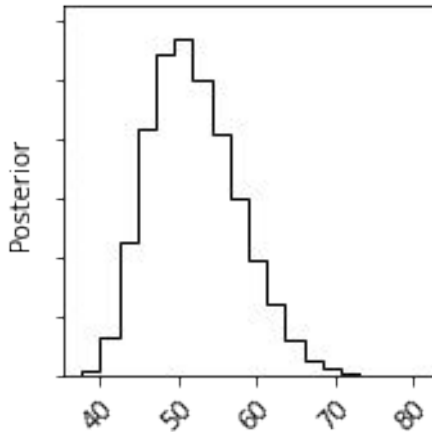
- How to find out if waveform family does not alter the search pipeline for finding **sub-threshold signals**?

- What I'm working on:**

Finding the **match** between O1 and O2 events plotted with **spin-aligned** and **non-spin aligned** waveform families

Waveform Matching - Method

1. Load in essential parameter **posterior samples** found with both spin aligned and non-spin aligned waveform families from previous analyses, find sample with the **maximum log likelihood**



Primary Mass (M_{\odot})

Intrinsic parameters:

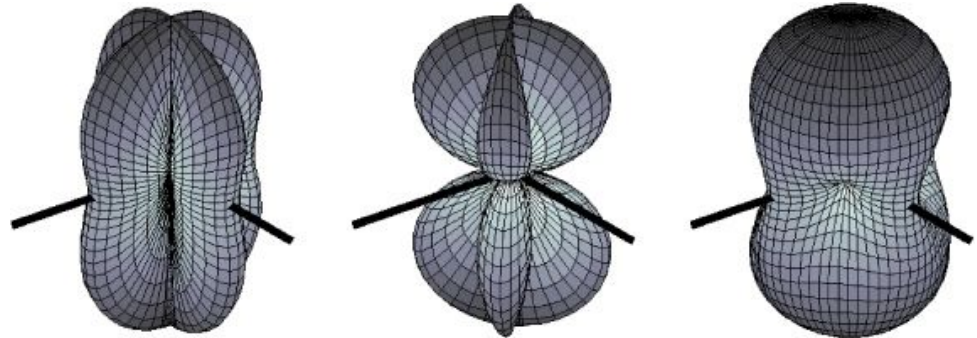
masses (m_1, m_2),
spins (\vec{S}_1, \vec{S}_2),

Extrinsic parameters:

time (t_c), reference phase (φ_c),
sky position (α, δ), distance (d_L),
orbital orientation (θ_{Jn}, ψ),

Waveform Matching - Method

2. Include Antenna Pattern function: how the strain appears in the detector



$$F_+(\zeta, \Phi, \Psi) = \frac{1}{2}(1 + \cos^2 \zeta) \cos 2\Phi \cos 2\Psi - \cos \zeta \sin 2\Phi \sin 2\Psi$$

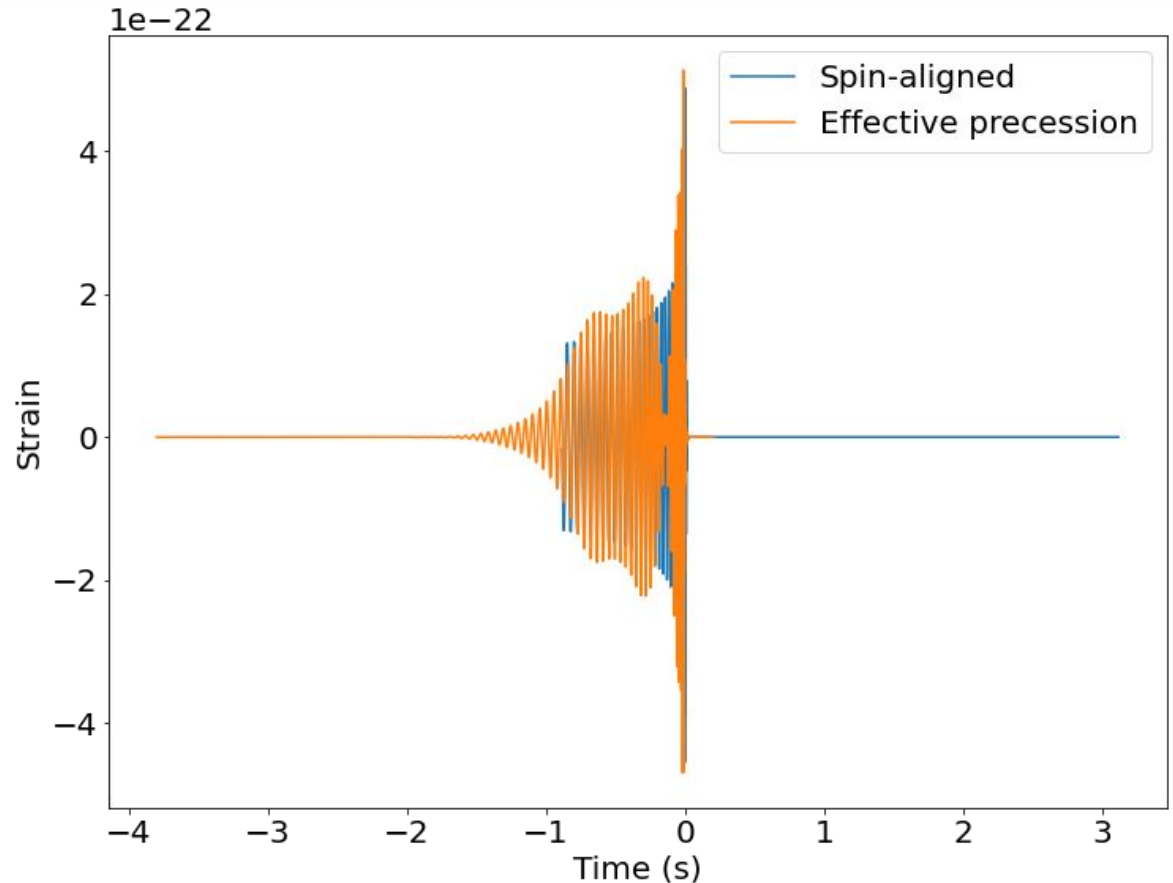
$$F_\times(\zeta, \Phi, \Psi) = \frac{1}{2}(1 + \cos^2 \zeta) \cos 2\Phi \sin 2\Psi + \cos \zeta \sin 2\Phi \cos 2\Psi$$

antenna pattern function depends on sky location, polarisation angle

$$\text{total strain} = F_+(\zeta, \Phi, \Psi)h_+(t) + F_\times(\zeta, \Phi, \Psi)h_\times(t)$$

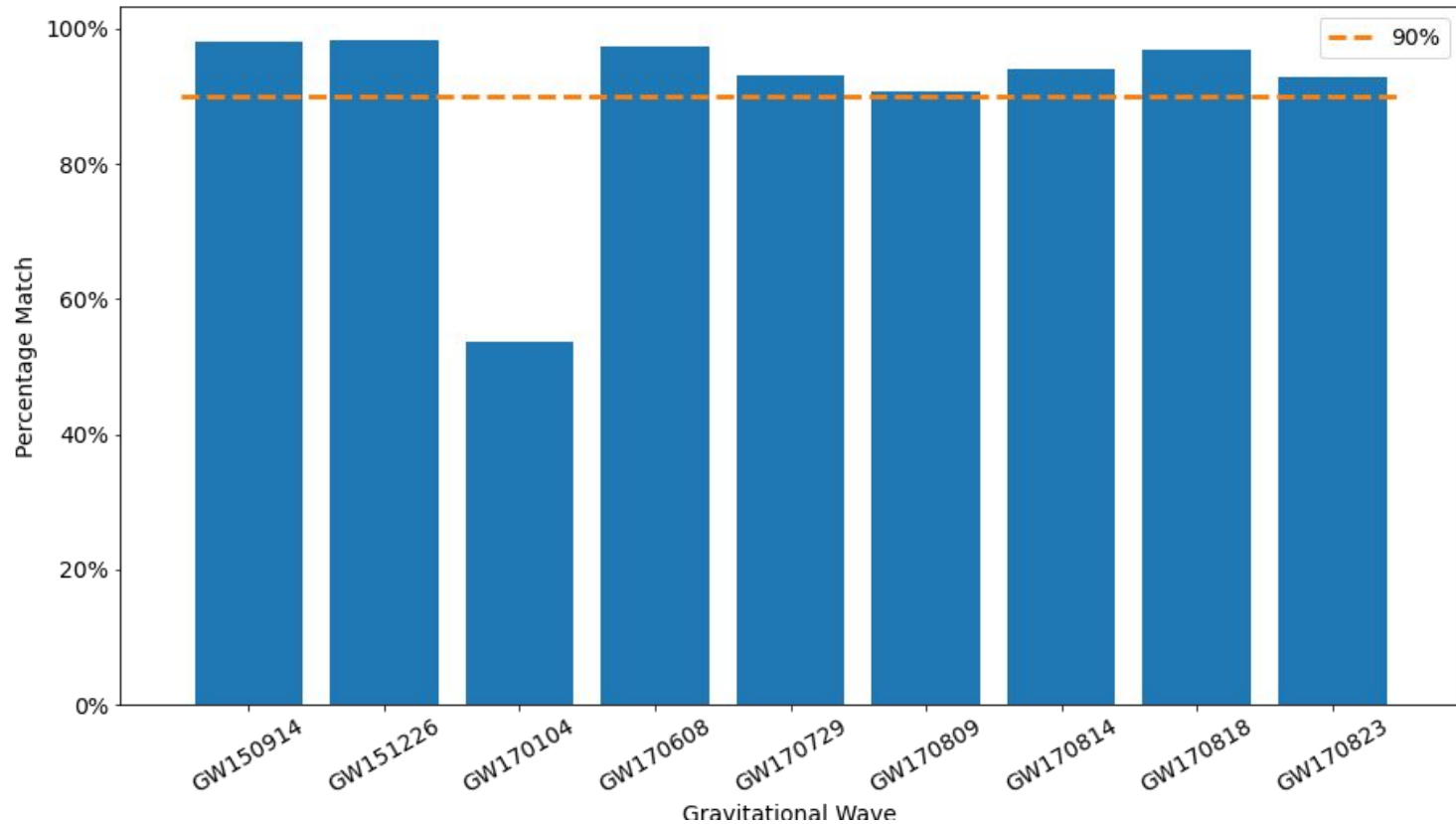
Waveform Matching - Method

3. Find the **match** between the strain for **spin-aligned** and **precessing** waveforms in each of the Hanford and Livingston detectors



GW170104 in Hanford Detector

Waveform Matching - Results



All above 90% match! Well, apart from GW170104..... evidence for precession?

Waveform Matching - Conclusion

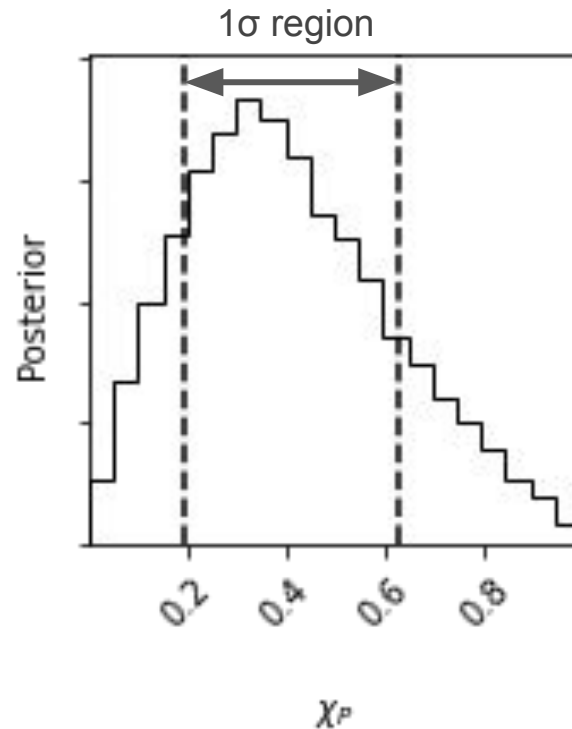
- If GW170104 is really precessing > SNR loss for aligned spin waveform



**Might lose
sub-threshold
signals**

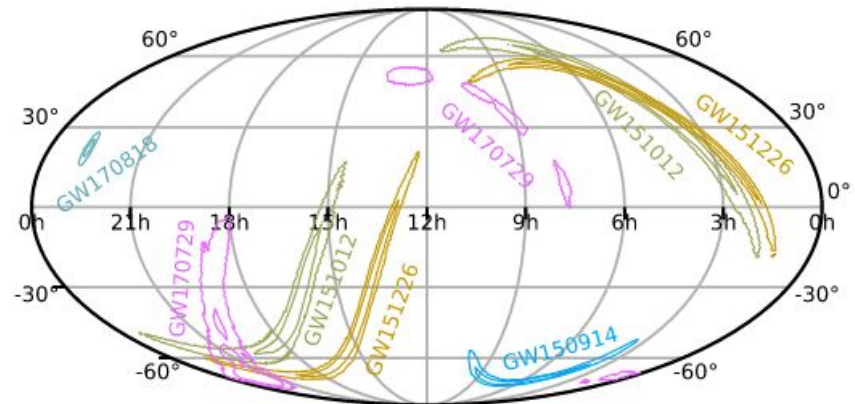
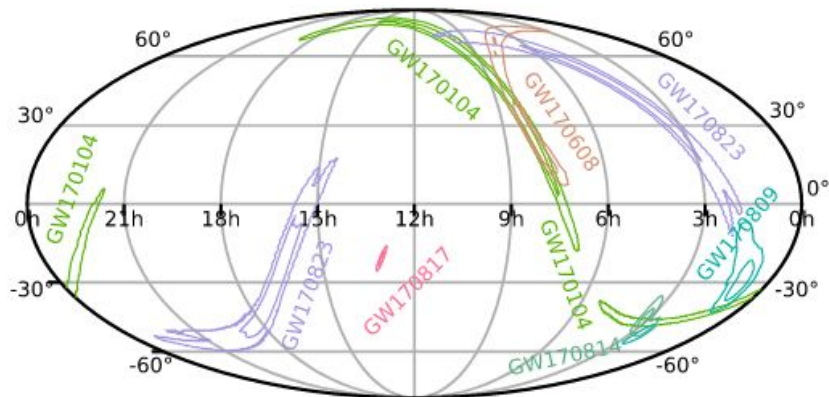
- If there is large uncertainty in precession (very likely) then either waveform should be suitable, not necessarily SNR loss

Waveform Matching - Conclusion



Effective precession spin parameter Posterior
Distribution of GW170104

Next Steps - Fundamentals

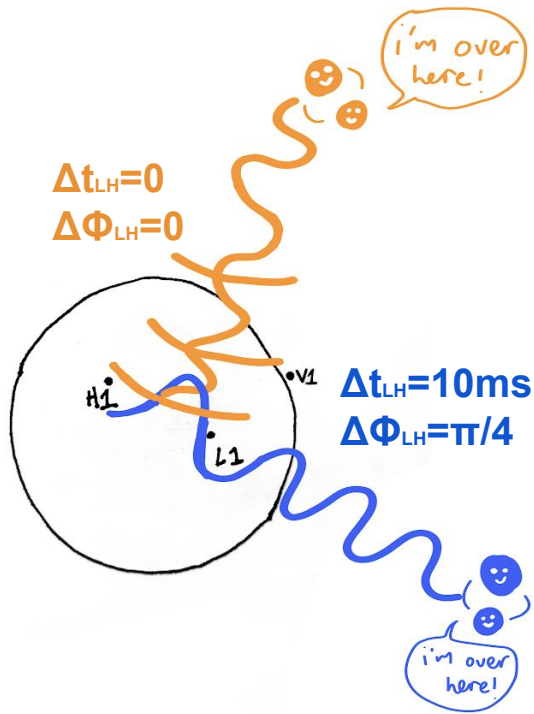


- Lensed images will come from approximately the same sky area
- Can rank lensed candidates higher based on their sky locations

Next Steps - Ranking

$$\mathcal{L} = \frac{\text{Probability that the data is a true signal}}{\text{Probability that the data is noise}}$$

Log Likelihood Ratio - Ranking Statistic

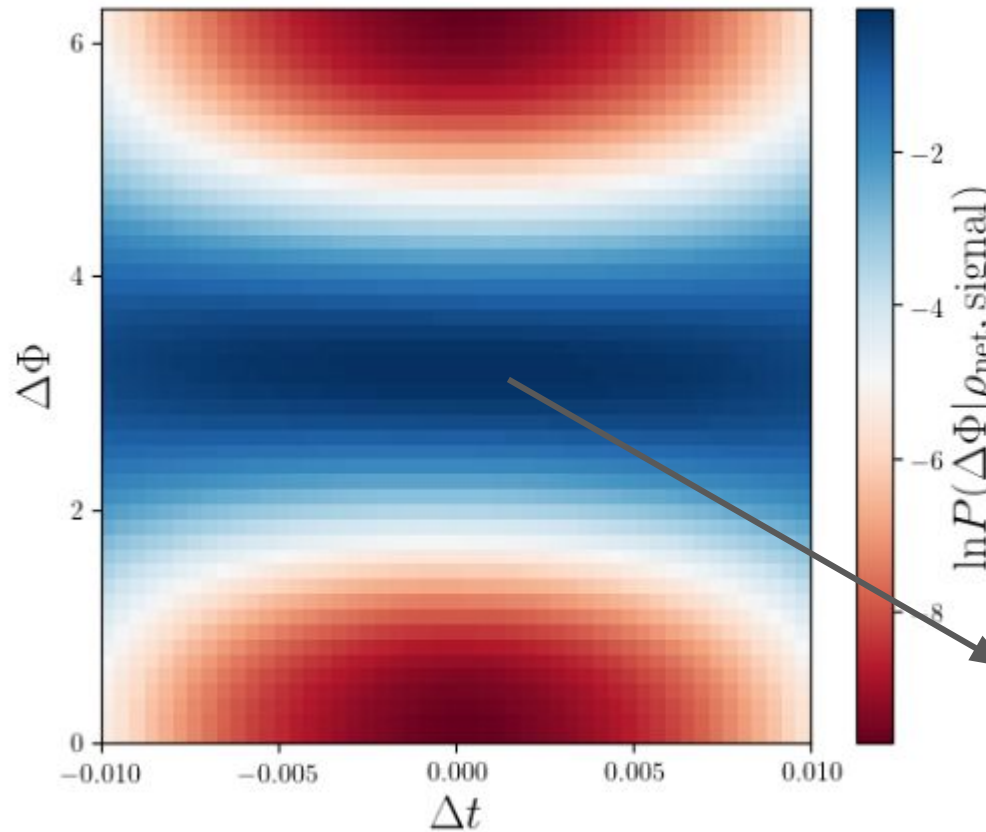


Both depend on Δt and $\Delta \Phi$:
the difference in arrival time and arrival phase
between 2 detectors [1]

□ Δt and $\Delta \Phi$ both depend on the sky location of
the source!

Next Steps - Ranking

2D Probability distribution for $\Delta\Phi$ and Δt considering signals across the whole sky:



Ranking of higher probability blue areas is boosted in pipeline

But what if we constrain the sky location.....?



Next Steps - Objectives

- Figure out how the **PDF of $\Delta\Phi$ and Δt changes** when considering a **smaller sky location**
- Implement this new constraint on $\Delta\Phi$ and Δt into the search pipeline to **target the search based on the sky location** of the super-threshold event
- Thus **boost ranking of lensed counterparts with similar sky location** to the target



References

[1] S. Sachdev, S. Caudill, H. Fong et. al. “The gstlal search analysis methods for compact binary mergers in advanced ligo’s second and advanced virgo’s first observing runs,” (2019), arXiv:1901.08580

Questions?

Extra Slide - GW170608 in Hanford

