



Refining the Search for Sub-threshold Lensed Gravitational Waves

LIGO SURF 2021

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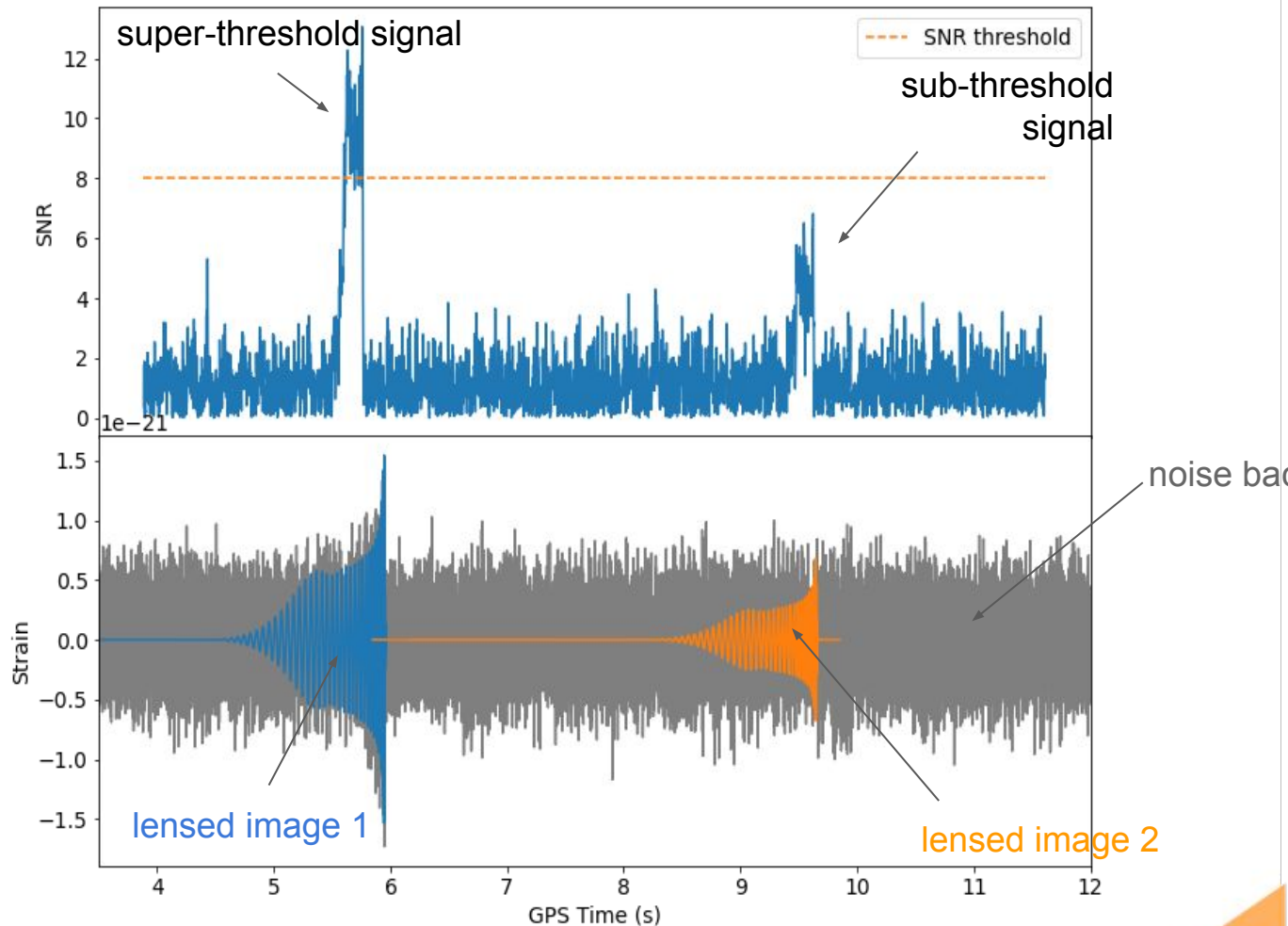


Key Points

- I. Where were we? Lensing, Sky location, Ranking
- II. Aims: Boosting ranking of lensed images
- III. Solution + Results so far
- IV. What next

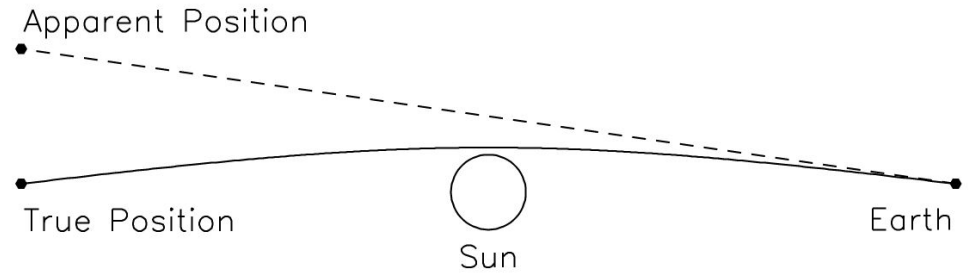
Refresher: Finding sub-threshold Gravitationally Lensed GWs

STRONG LENSING!

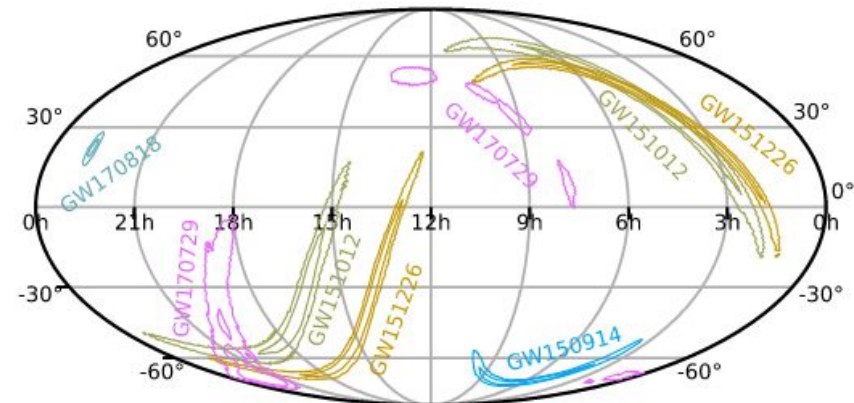
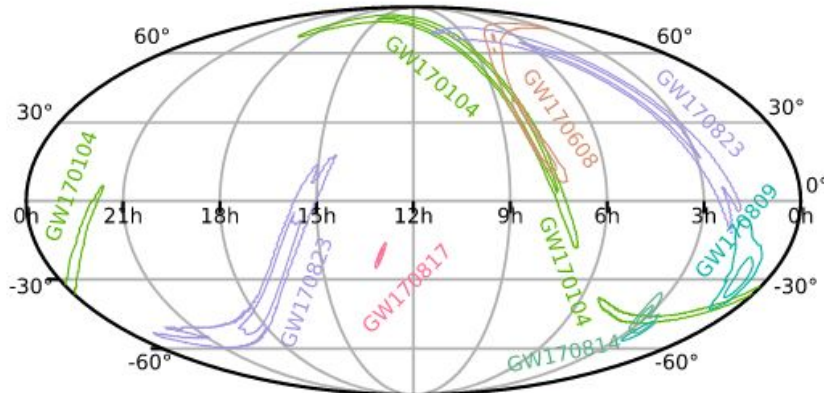


Refresher: Sky Localisation of GWs >> Lensed Image Separation

**STRONG
LENSING!**



SKYMAPS!





Refresher: Ranking Candidates in GstLAL Pipeline

STRONG
LENSING!

SKYMAPS!

RANKING!

$$\mathcal{L} = \frac{P(\{D_1, D_2\} \{d_1, d_2\}, \rho_1, \rho_2, \xi_1^2, \xi_2^2, \Delta\phi, \Delta t | \text{signal})}{P(\{D_1, D_2\} \{d_1, d_2\}, \rho_1, \rho_2, \xi_1^2, \xi_2^2, \Delta\phi, \Delta t | \text{noise})}$$

Refresher: Tying it all together...

STRONG
LENSING!

SKYMAPS!

RANKING!



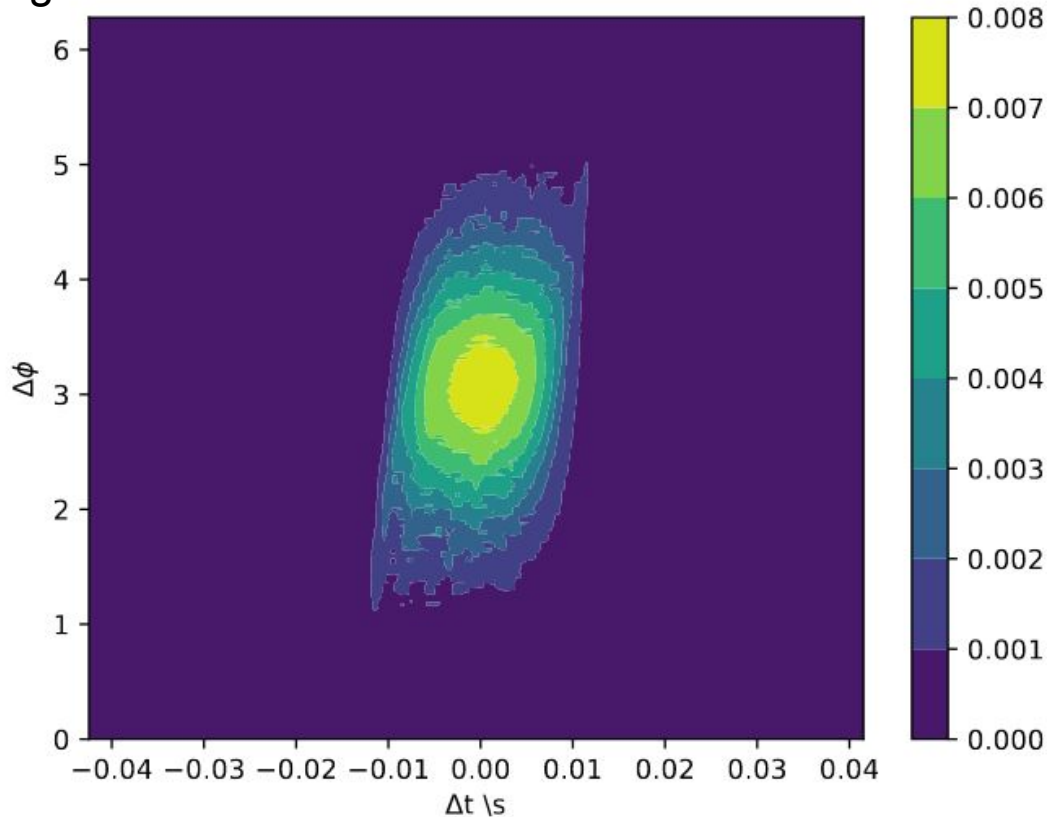
Credit: Duncan Brown

WOO!

$$\mathcal{L} = \frac{P(\{D_1, D_2\} \{d_1, d_2\}, \rho_1, \rho_2, \xi_1^2, \xi_2^2, \Delta\phi, \Delta t | \text{signal})}{P(\{D_1, D_2\} \{d_1, d_2\}, \rho_1, \rho_2, \xi_1^2, \xi_2^2, \Delta\phi, \Delta t | \text{noise})}$$

Aims: Looking for $\Delta\Phi$ Δt PDF

2D Probability distribution for $\Delta\Phi$ and Δt considering signals **across the whole sky** for Hanford and Livingston:



But what if we constrain the sky location.....?



Aims: Looking for $\Delta\Phi$ Δt PDF

Working on....

- Figuring out how the **PDF of $\Delta\Phi$ and Δt changes** when considering a **smaller sky location**

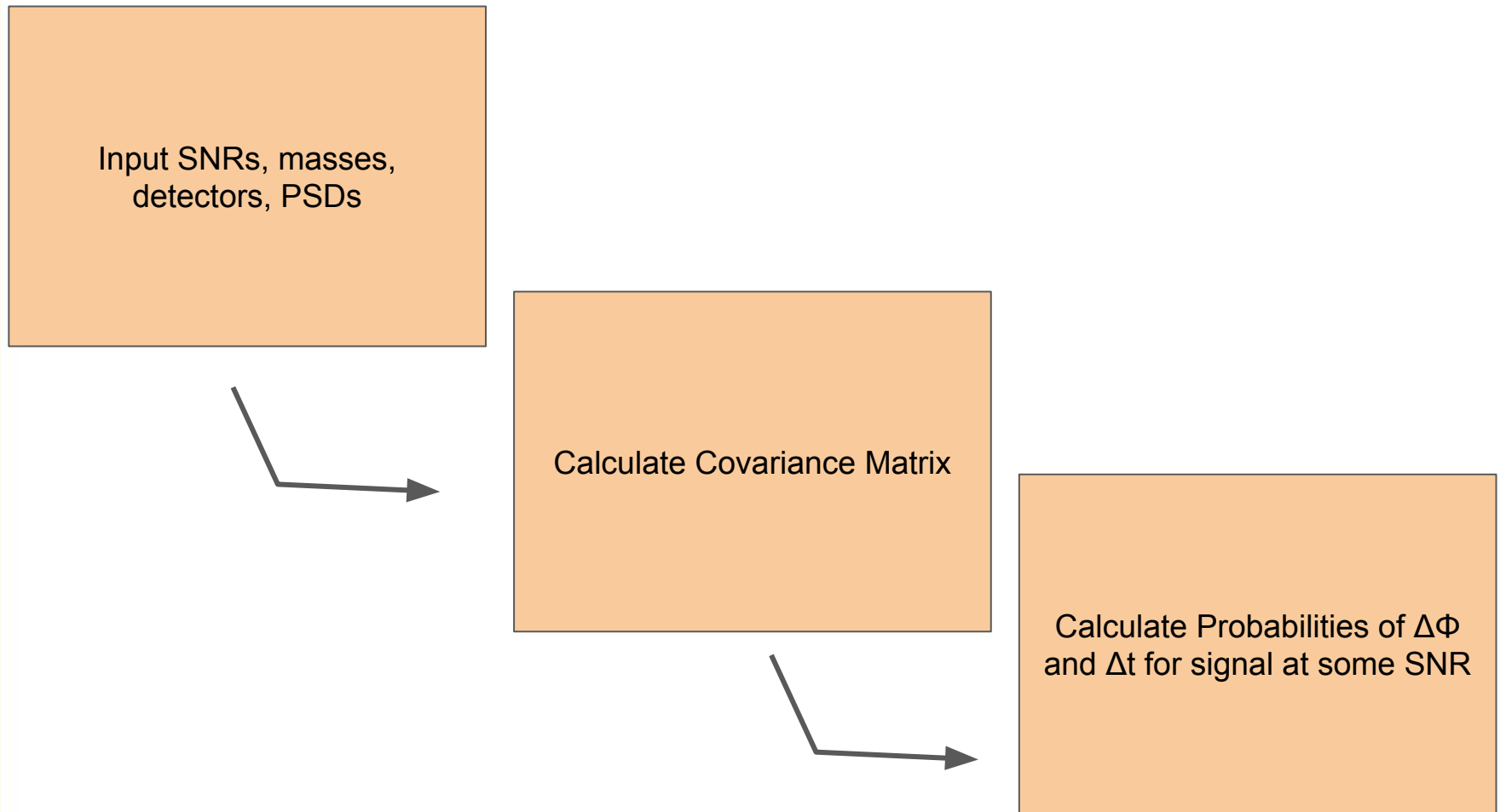
To eventually implement....

- Implement this new constraint on $\Delta\Phi$ and Δt into the search pipeline to **target the search based on the sky location** of the super-threshold event
- Thus **boost ranking of lensed counterparts with similar sky location** to the target

How??????????

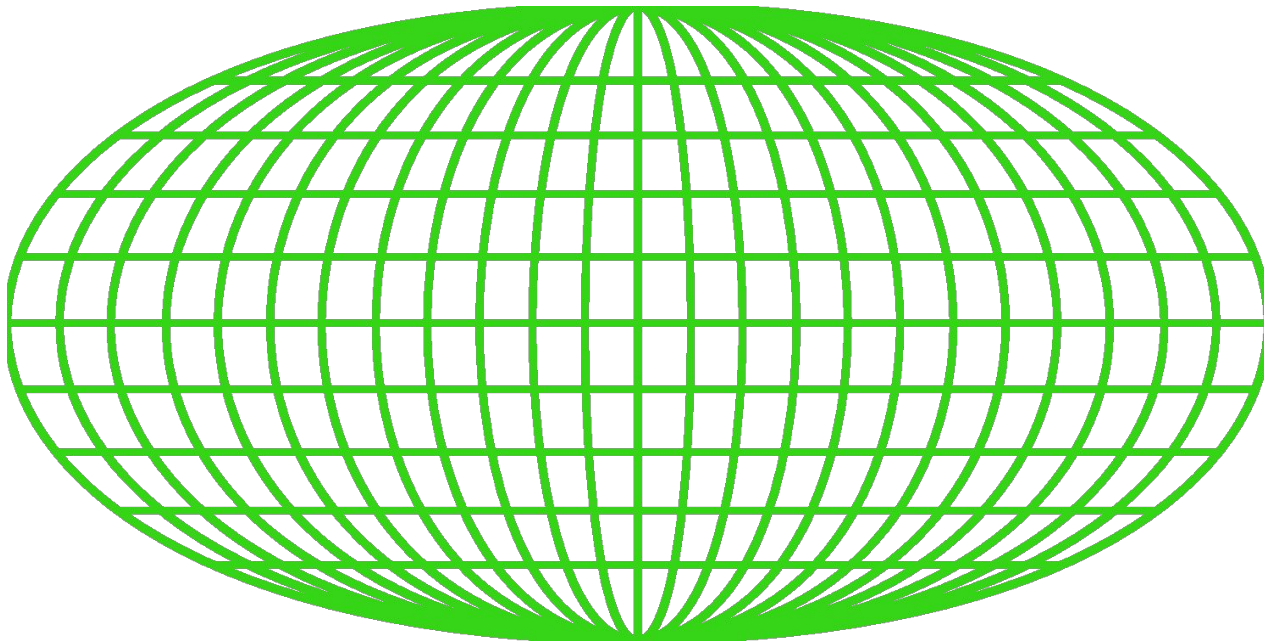


Inside the GstLAL Pipeline:



Inside the Probability Calculation:

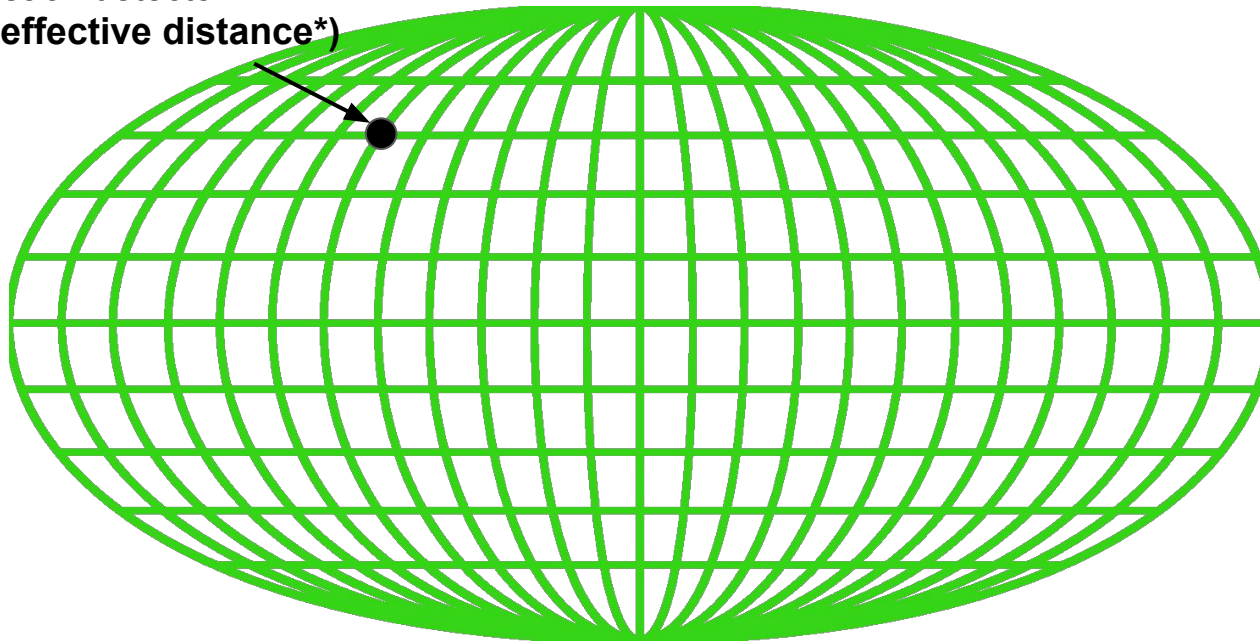
- GstLAL finds the PDF of $\Delta\Phi$ and Δt with a tiling function: tiles **the whole sky** with even probability of event from each direction



Inside the Probability Calculation:

- GstLAL finds the PDF of $\Delta\Phi$ and Δt with a tiling function: tiles **the whole sky** with even probability of event from each direction

Calculates for each detector:
(time, phase, effective distance*)



*equivalent to SNR

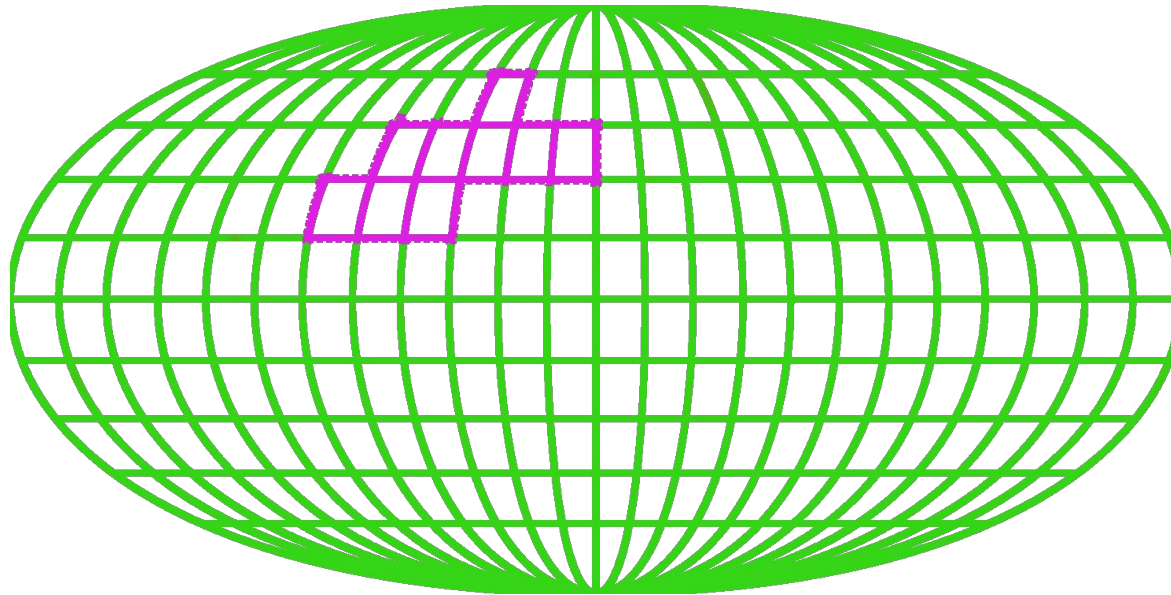


Inside the Probability Calculation:

- Obtain Δt , $\Delta\Phi$, ΔD_{eff} between **each of the detectors** for **each point**
- **Use this to calculate the PDF** using the covariance matrix, with lots more maths [Chad Hanna, 2019]
<https://arxiv.org/pdf/1901.02227.pdf>

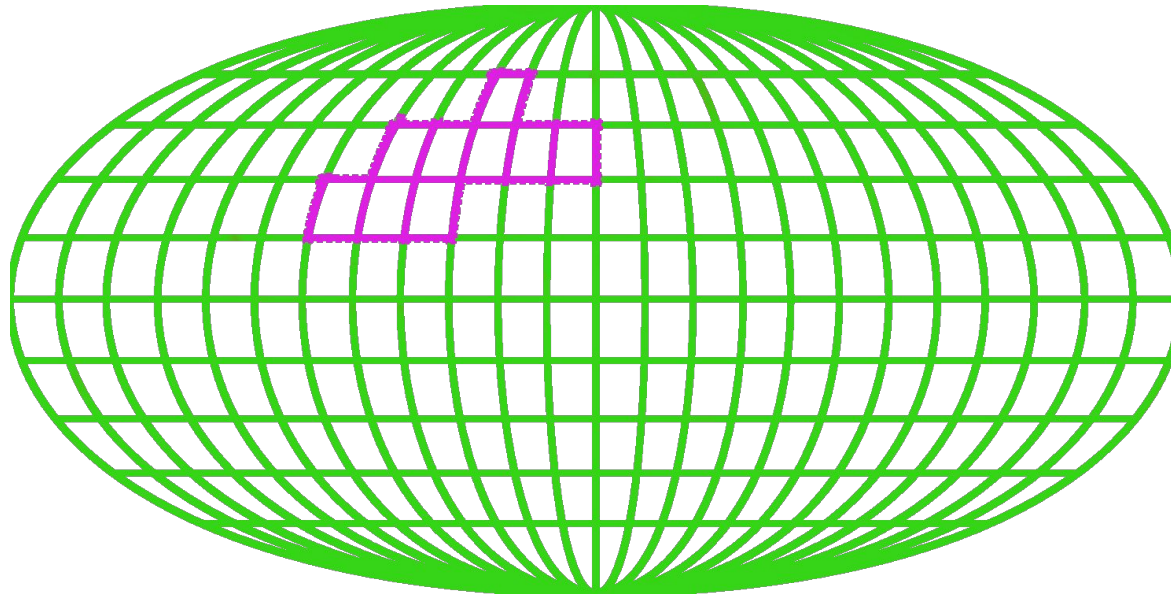
Inside the New Improved Probability Calculation:

- We modify GstLAL to find the PDF of $\Delta\Phi$ and Δt with a tiling function: tiles the **90% credible region** of a real target event with even probability



Inside the New Improved Probability Calculation:

- We modify GstLAL to find the PDF of $\Delta\Phi$ and Δt with a tiling function: tiles the **90% credible region** of a real target event with even probability
- PDF then found as before.....

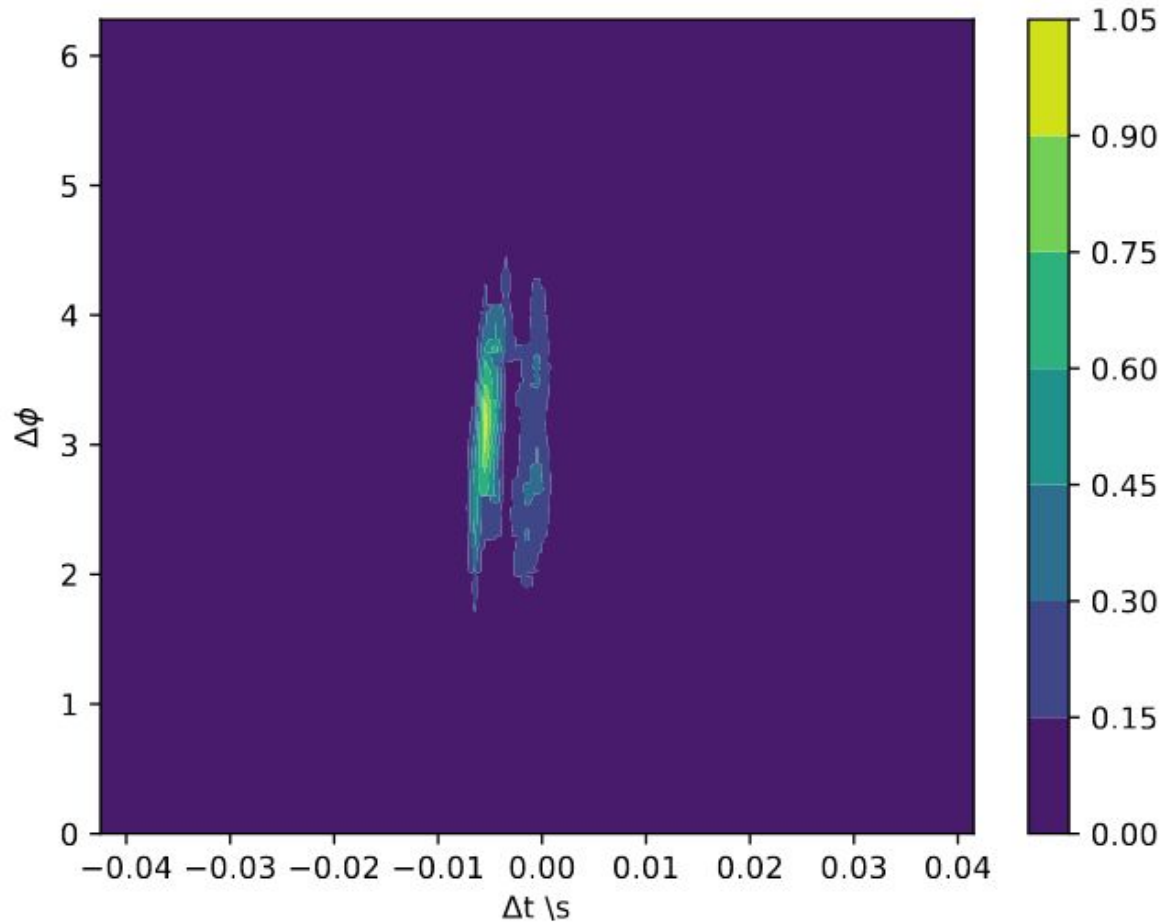


Momentary Pause while we get lost in GstLAL bugs



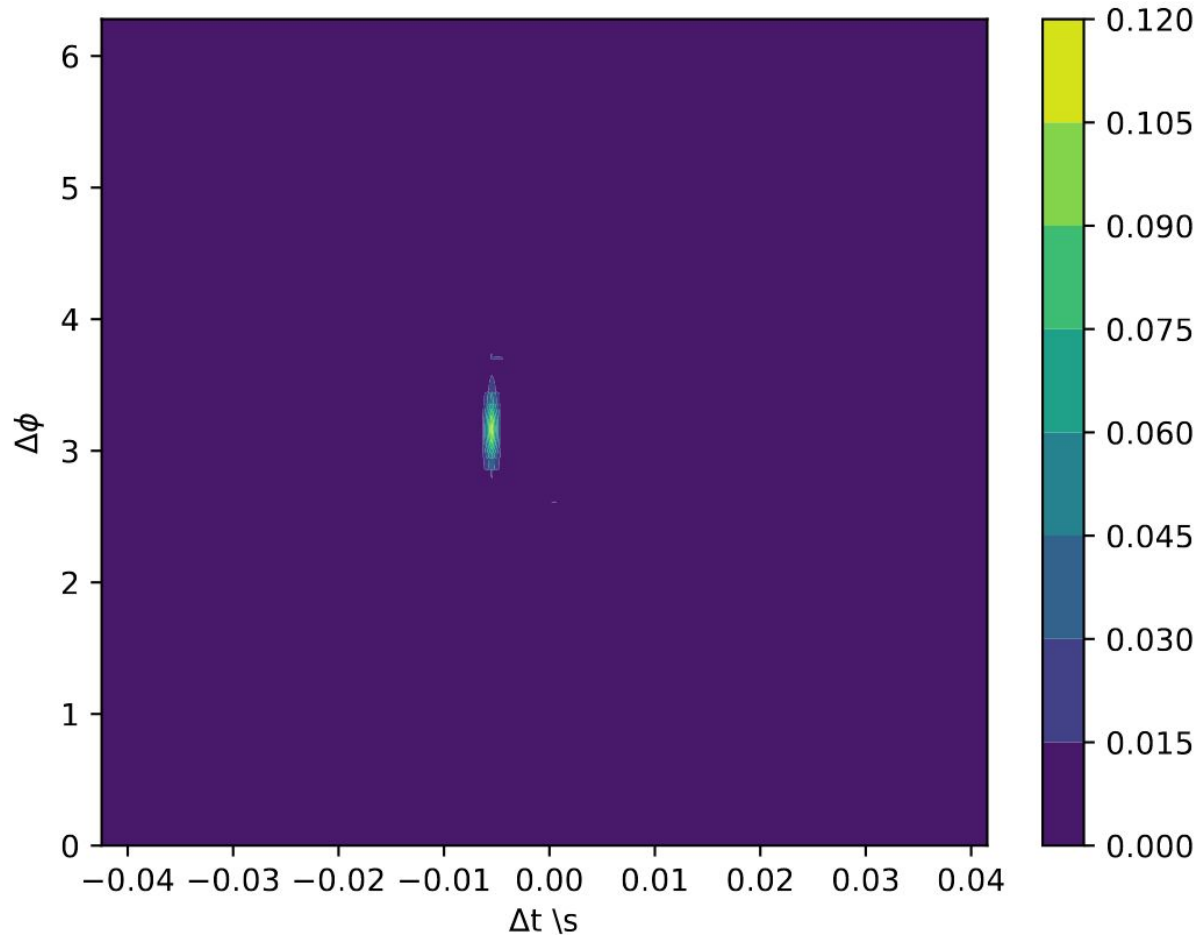
Results.... !

$\Delta\phi$ and Δt PDF for S190408an, with detector H1 and L1, SNRs = 4



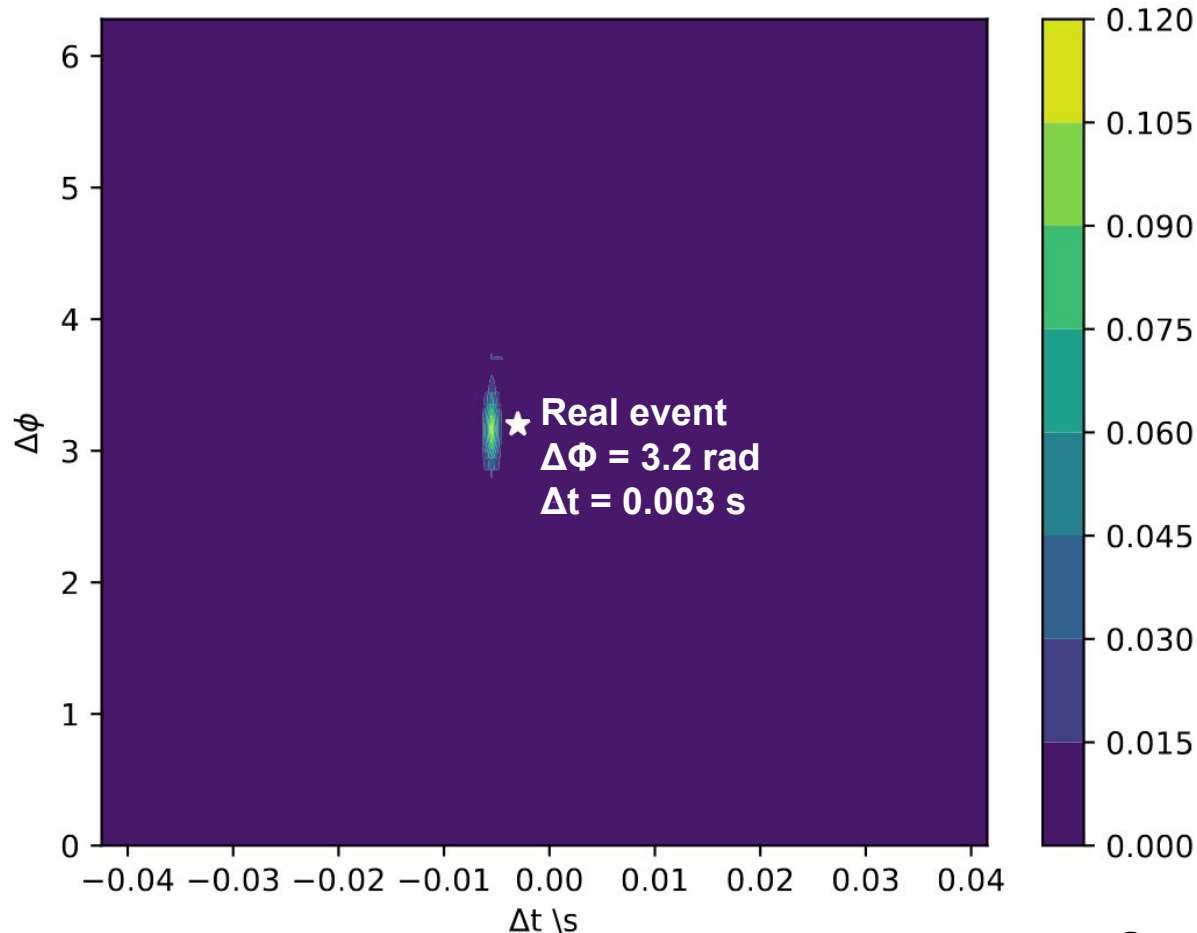
Results... With Real SNRs!

$\Delta\phi$ and Δt PDF for S190408an for H1L1 with detector SNRs equal to event values



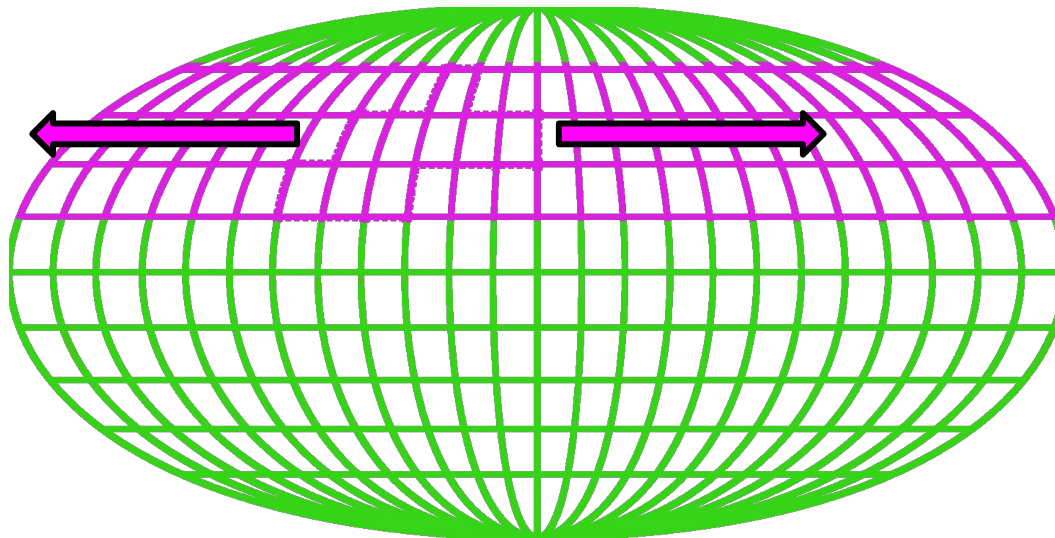
Results... With Real SNRs!

$\Delta\Phi$ and Δt PDF for S190408an for H1L1 with detector SNRs equal to event values



What about Rotation of the Earth?

- Lensed images separated by minutes up to weeks or months
 - Earth will have rotated between images
- Need to account for different detector response functions
- Image will effectively come from any RA within target's DEC range





What next?

- Implement the skymap rotation into GstLAL to **tile 90% band of the sky**
- Run modified search pipeline and **compare to previous candidates** with known target event overlap between sky localisations and **see if events are boosted appropriately**



Summary

- Aiming to **boost rankings of lensed images with similar sky localisations**

Done:

- Changed tiling method to only account for **90% credible interval** of a target event

To do:

- Need to further modify this to **account for the rotation of the Earth**, and tile a band around the sky
- Test in sub-threshold search pipeline against previously found candidates to **see if likelihood boosting works as expected**