



Recovering Higher Order Modes in the Ringdown of BBH Coalescences

DCC #LIGO-T2200250

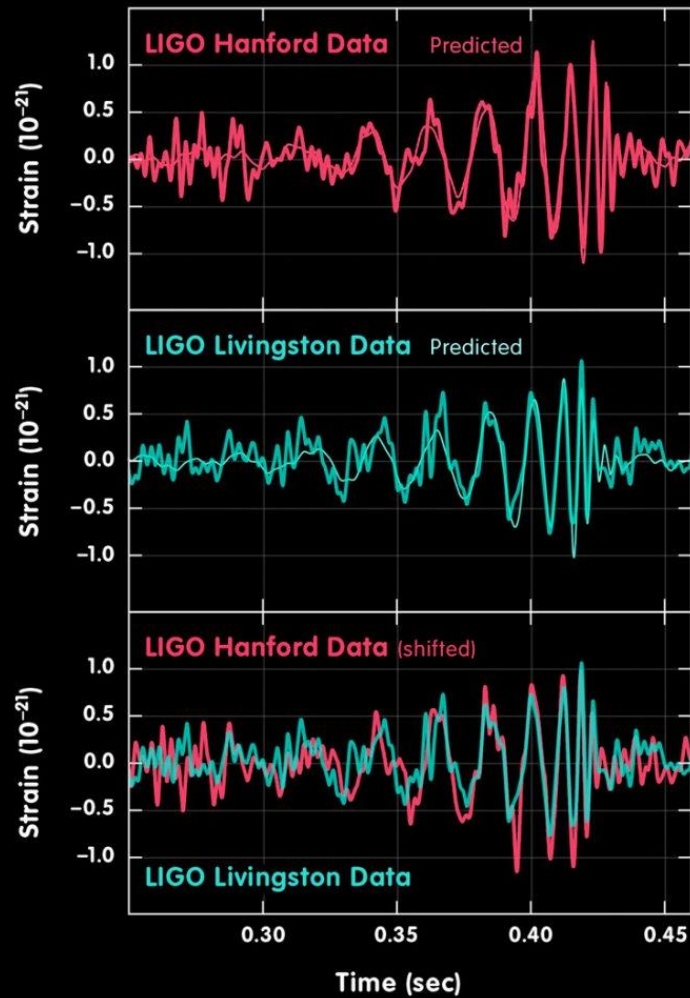
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Mentors: Richard Udall & Alan Weinstein

Caltech

Overview

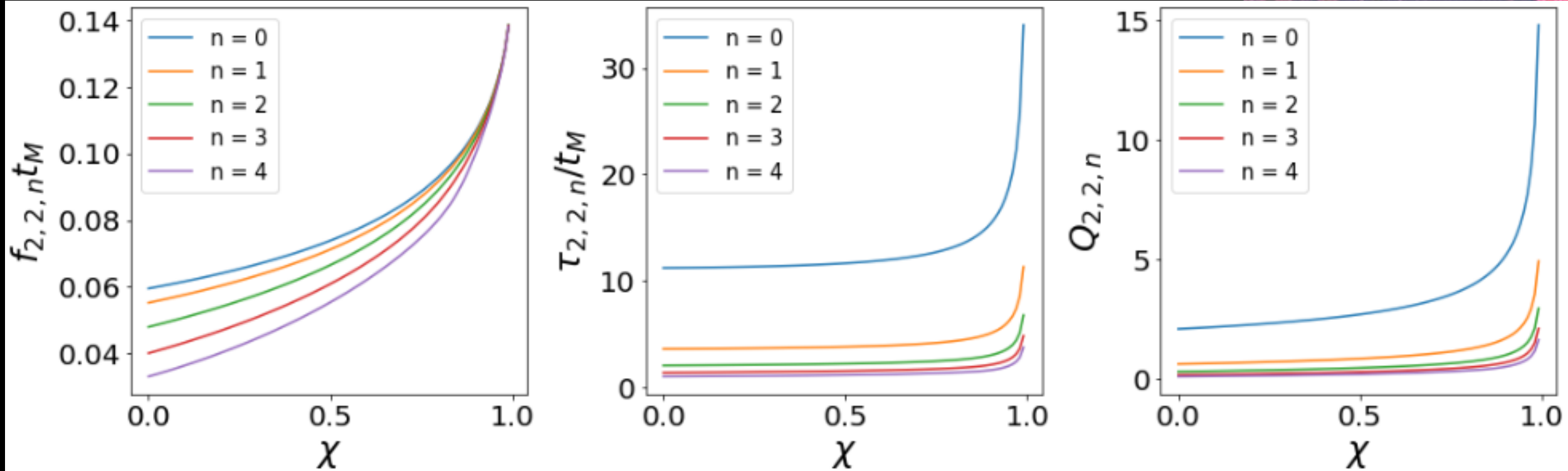


- BBH mergers
- Time domain ringdown analysis
- Quasinormal Modes (QNMs)
- Higher Order Modes (HOMs)
- No Hair Theorem (NHT)

$$t_M = \frac{GM}{c^3}$$

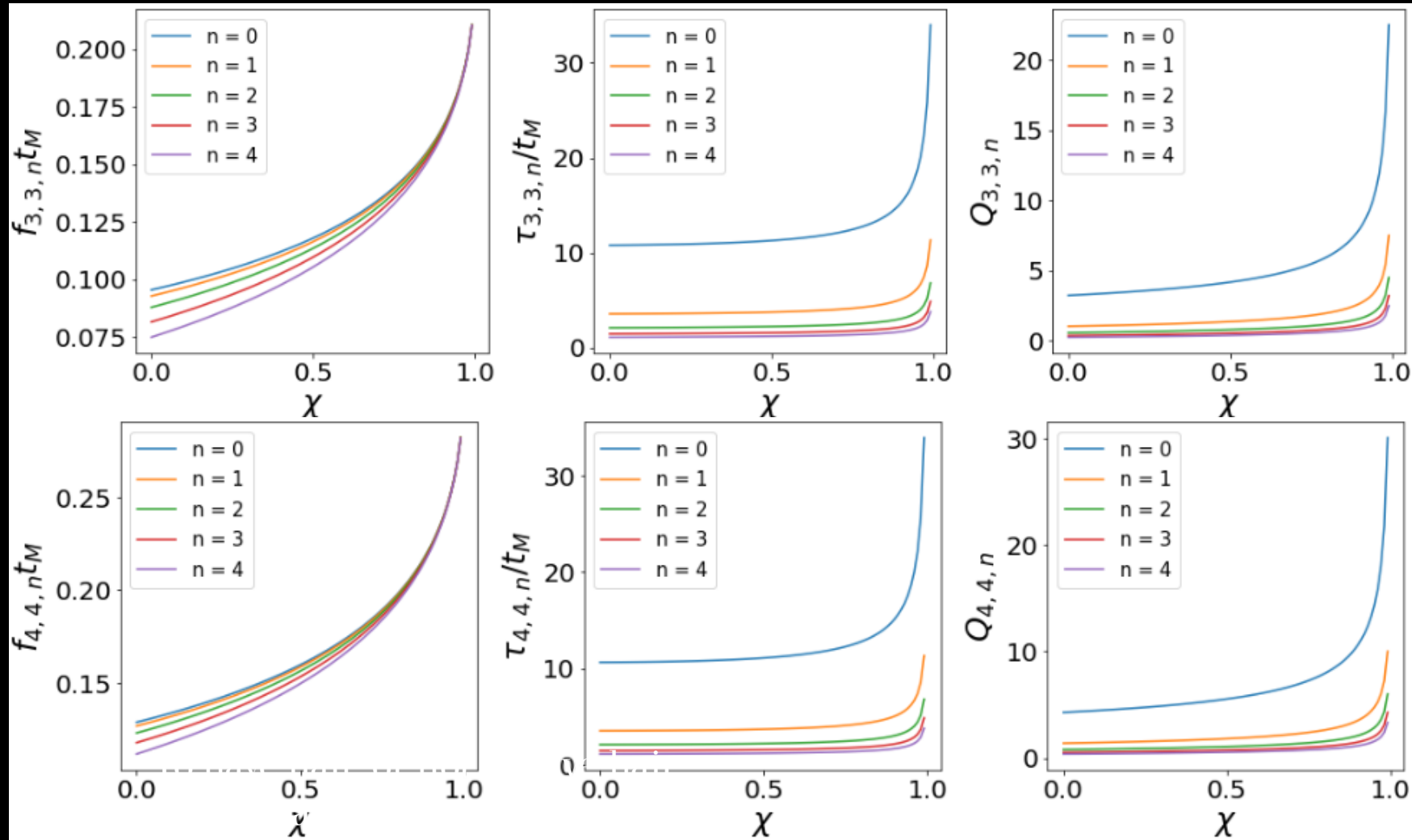
$$Q = \pi f \tau$$

Quasinormal Modes (QNMs)



$$Q = \pi f \tau$$

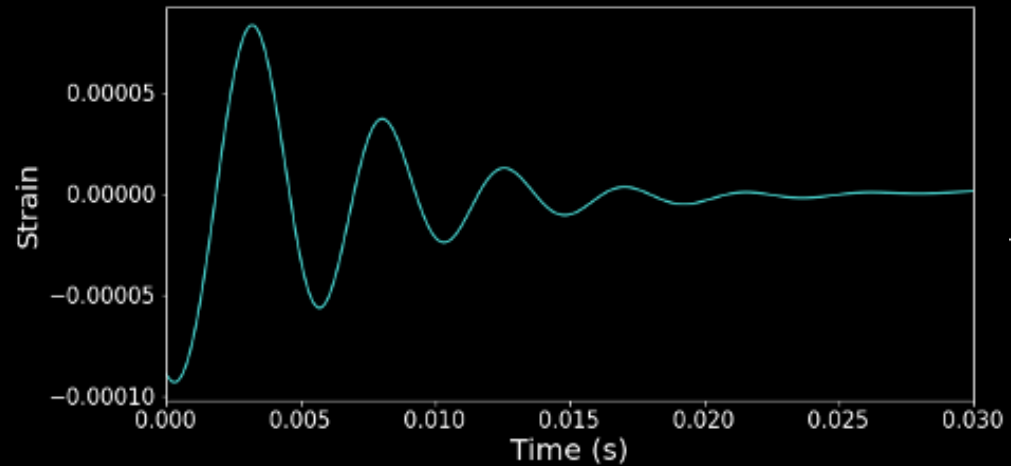
$$t_M = \frac{GM}{c^3}$$



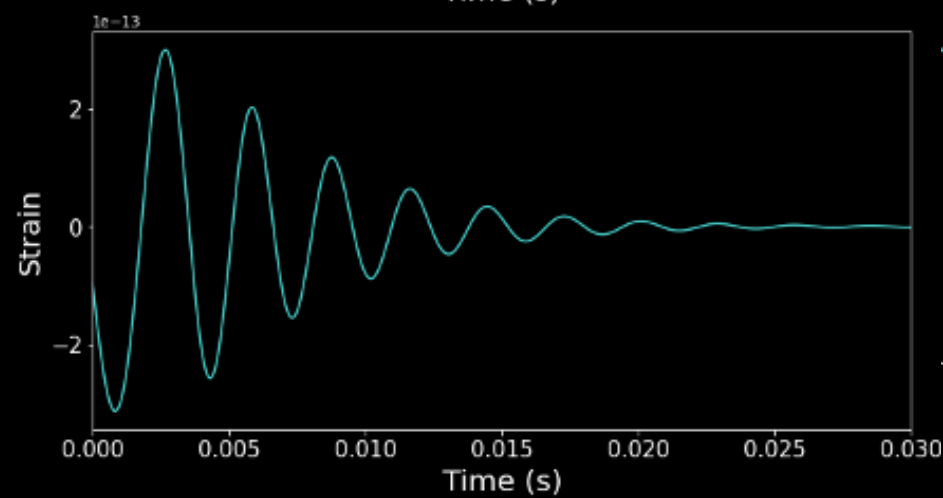
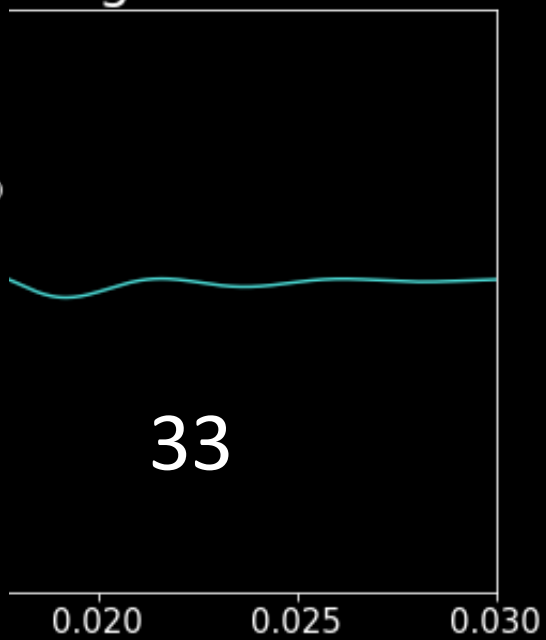
IMRPhenomXP(HM)

- Approximant
 - Combines inspiral, merger, ringdown
 - Phenomenological model
 - Precessing BBHs
 - QNM configuration
 - 21 (XPHM)
 - 22 (XP)
 - 32 (XPHM)
 - 33 (XPHM)
 - 44 (XPHM)
- $n = (0, 1, 2)$

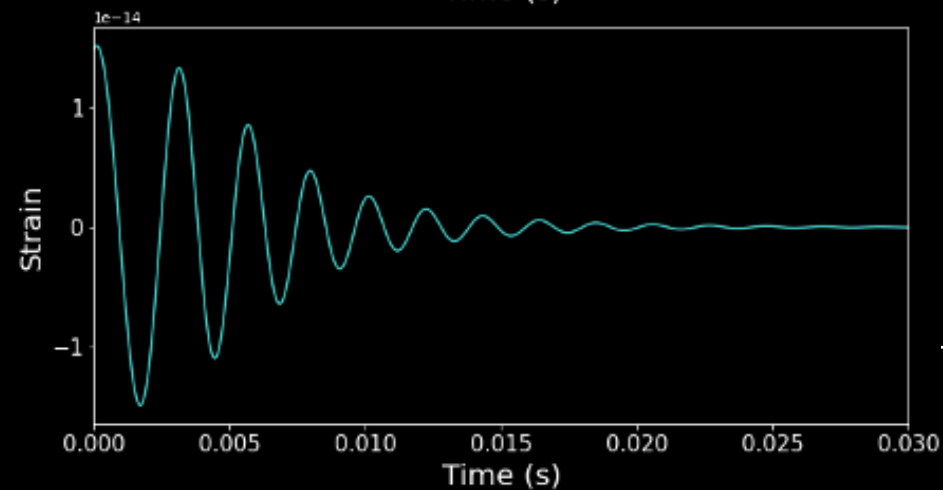




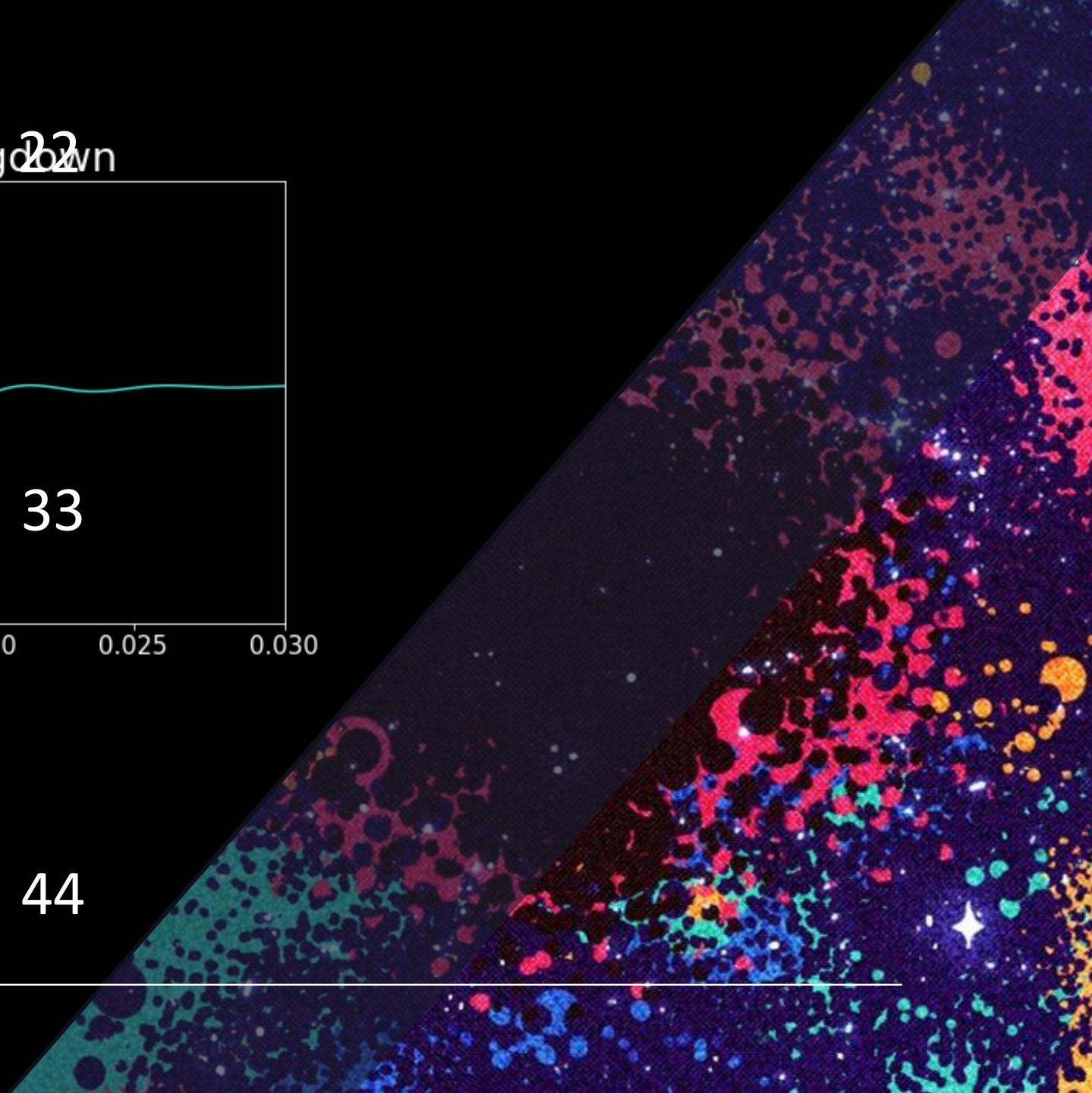
Ringdown 22



33



44



Recovery Methoddoes it do a good job?

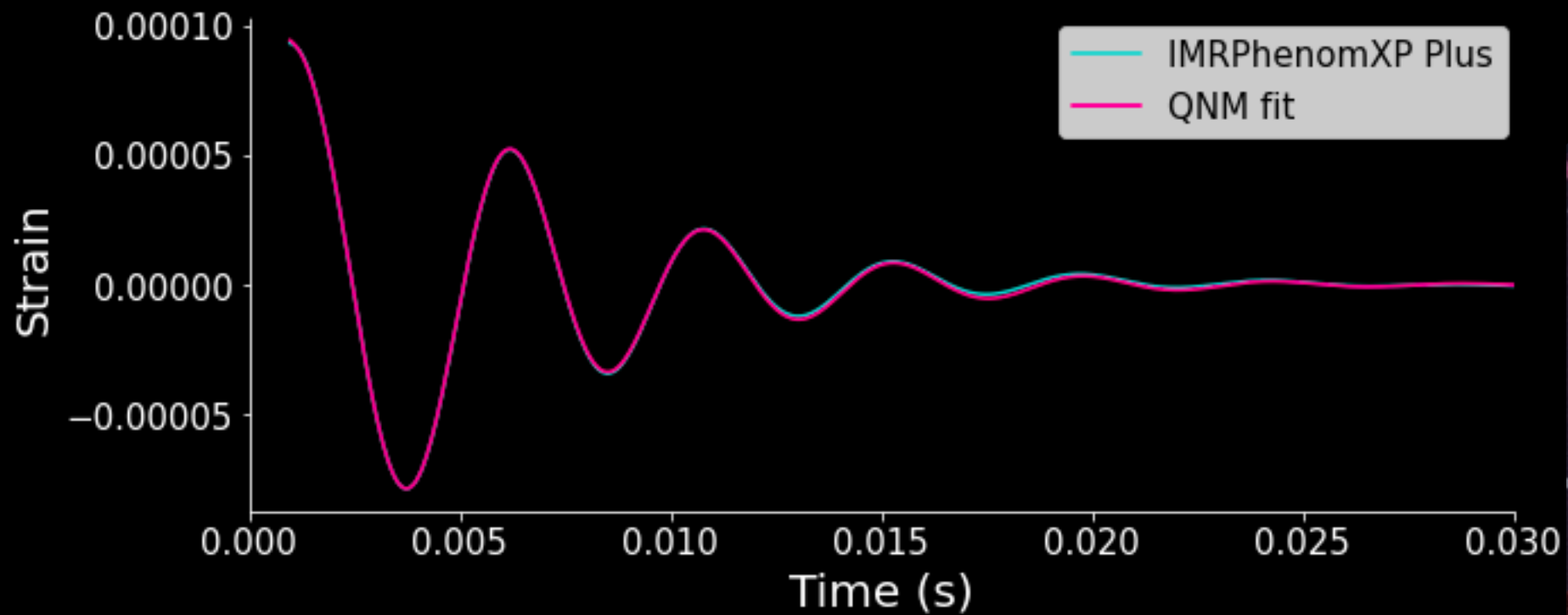
scipy.optimize.curve_fit

```
scipy.optimize.curve_fit(f, xdata, ydata, p0=None, sigma=None,  
absolute_sigma=False, check_finite=True, bounds=(- inf, inf), method=None,  
jac=None, **kwargs)
```

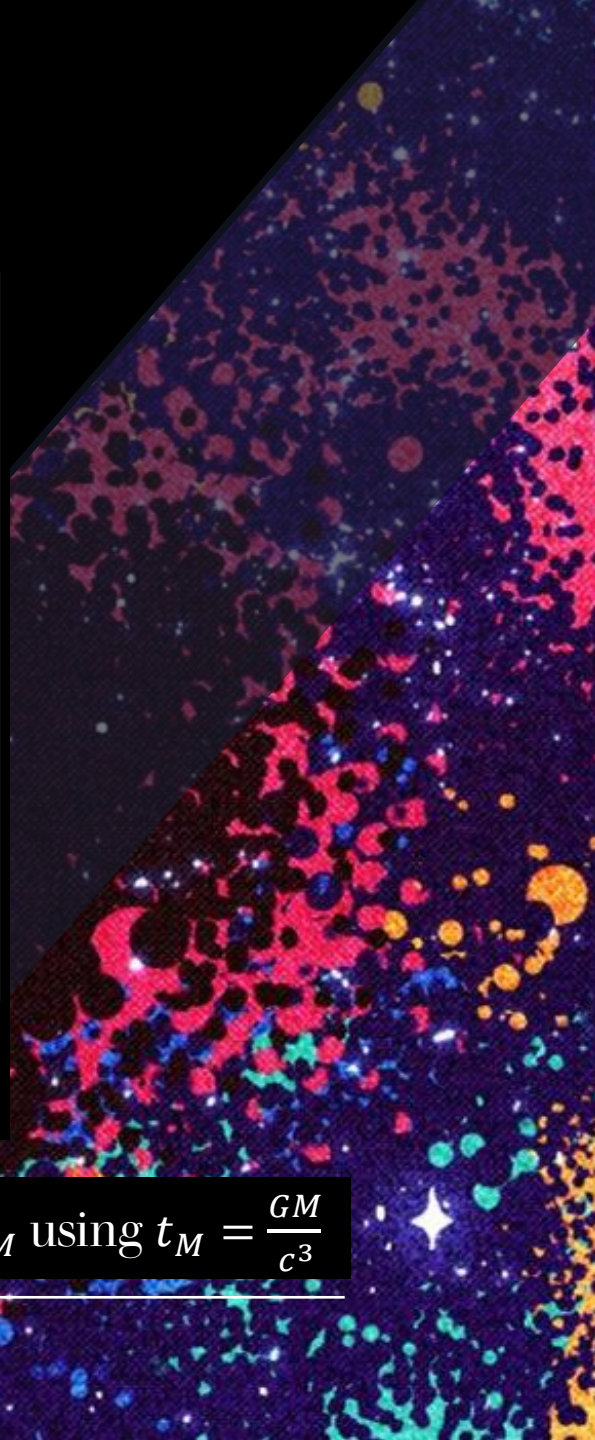
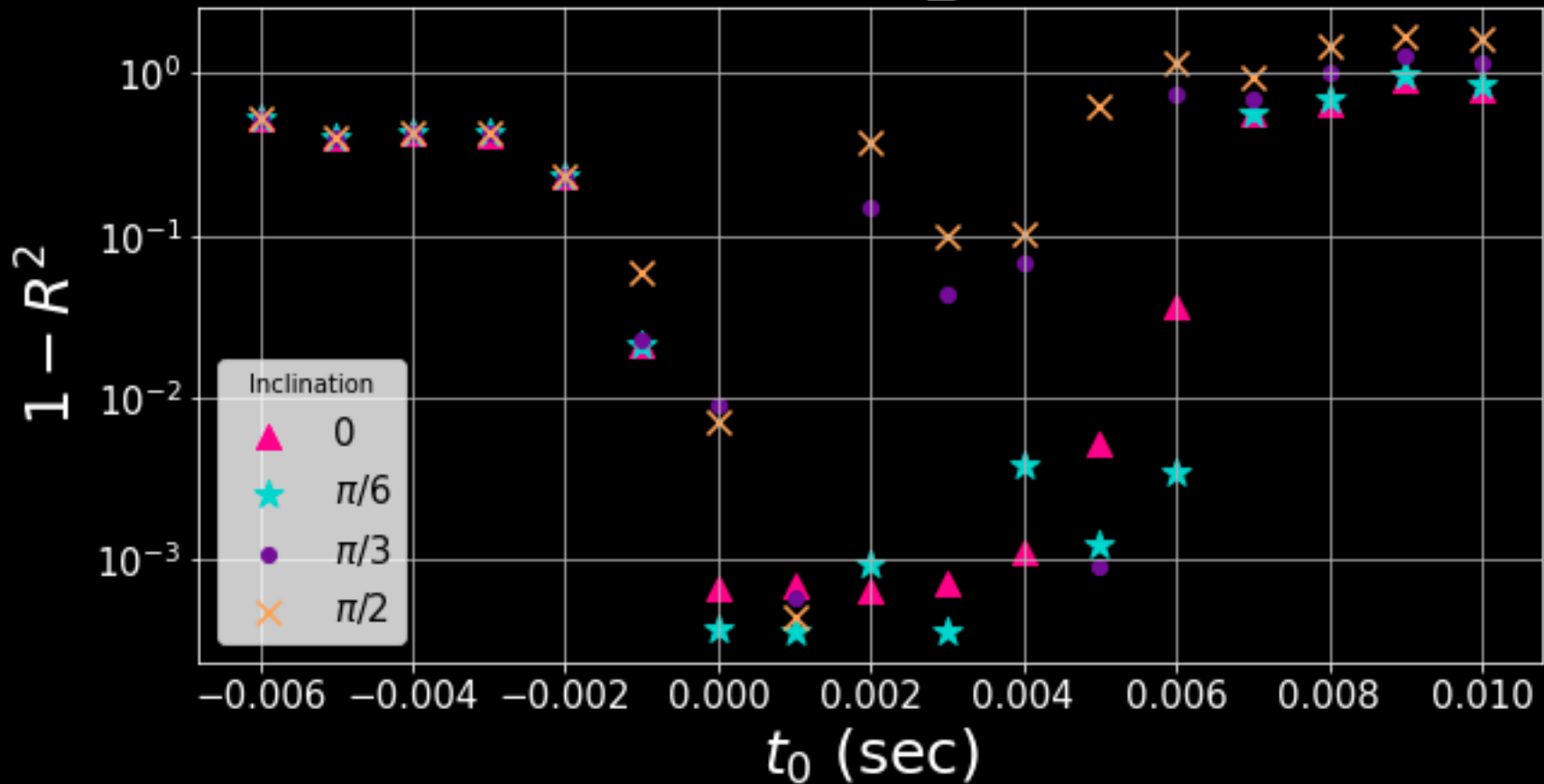
$$h \sim \sum_{lmn} A_{lmn} \sin(2\pi f_{lmn} t) e^{-t/\tau_{lmn}}$$

$$1 - R^2 = \frac{RSS}{TSS}$$

IMRPhenomXP [22]



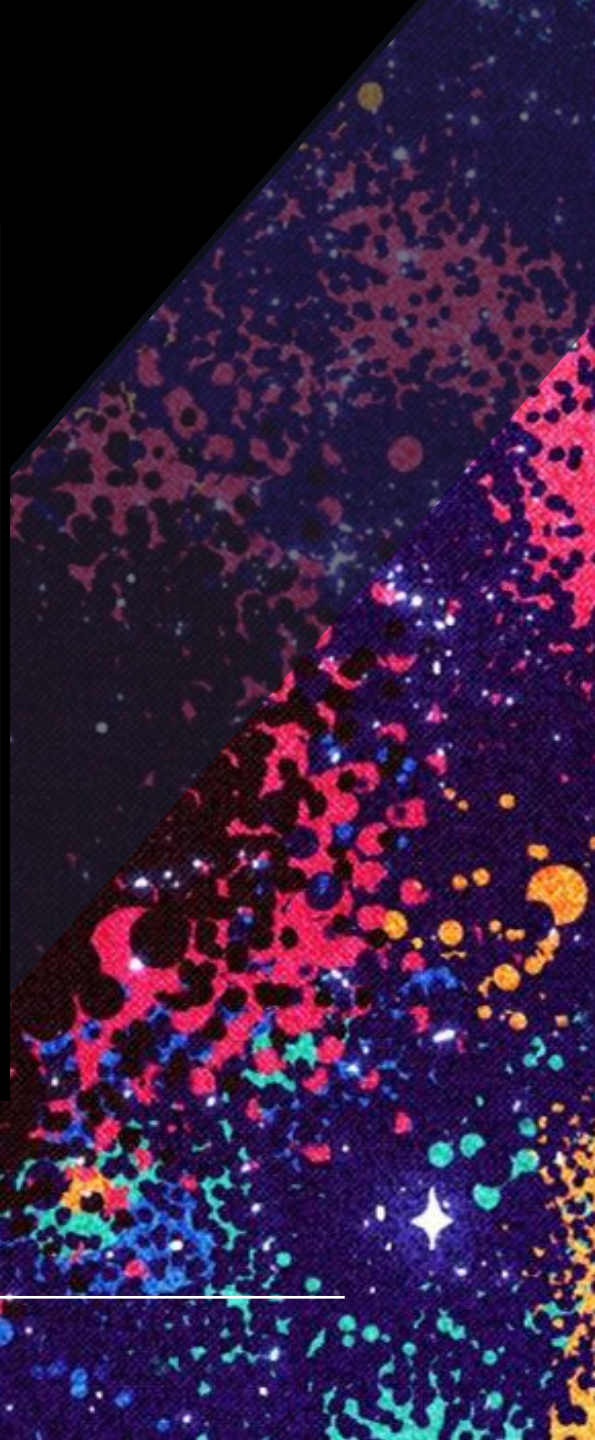
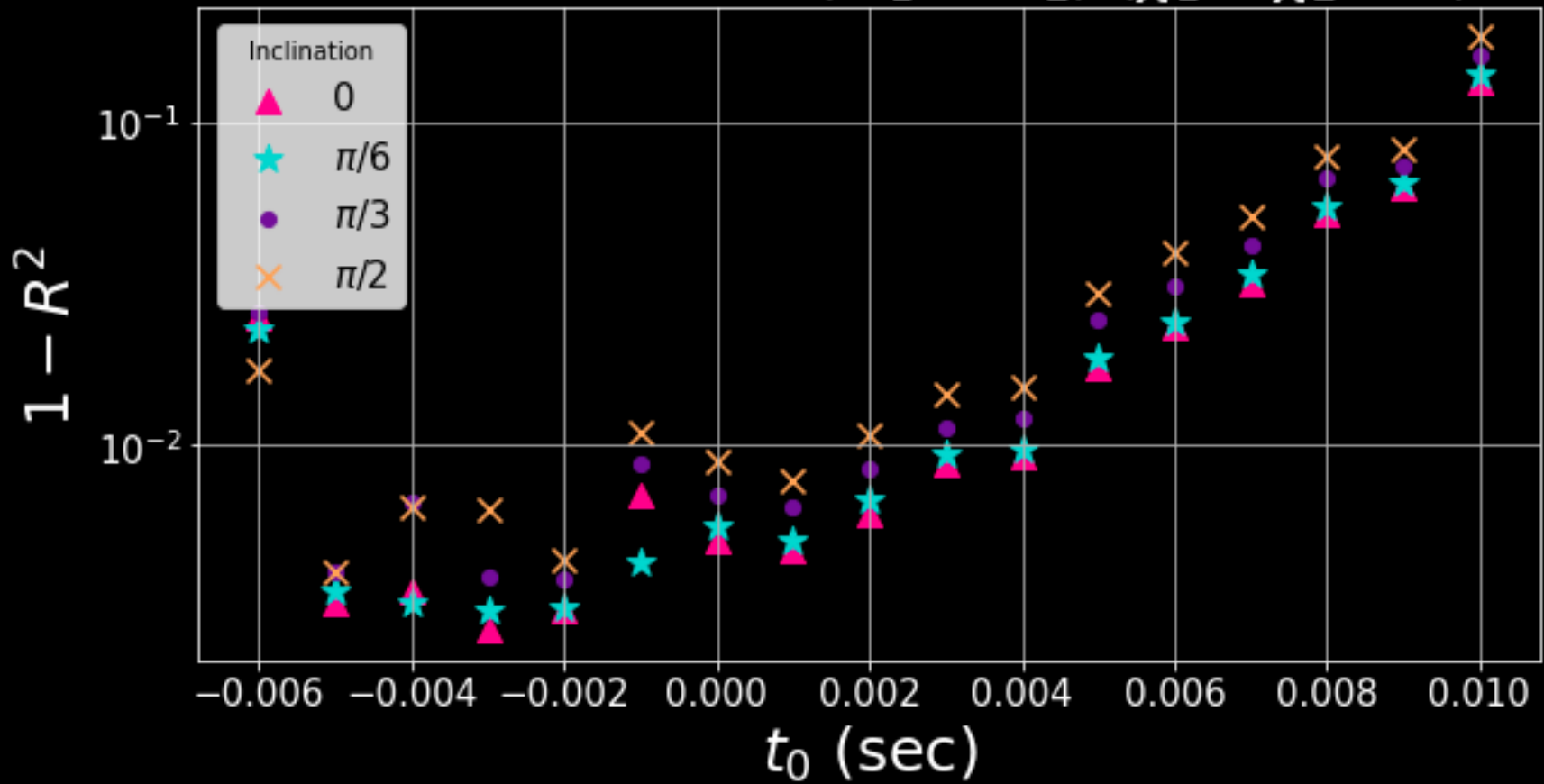
IMRPhenomXP ($M_1 = \frac{1}{2}M_2$) ($\chi_1 = \chi_2 = 0$)



IMRPhenomXP Modes: [22]

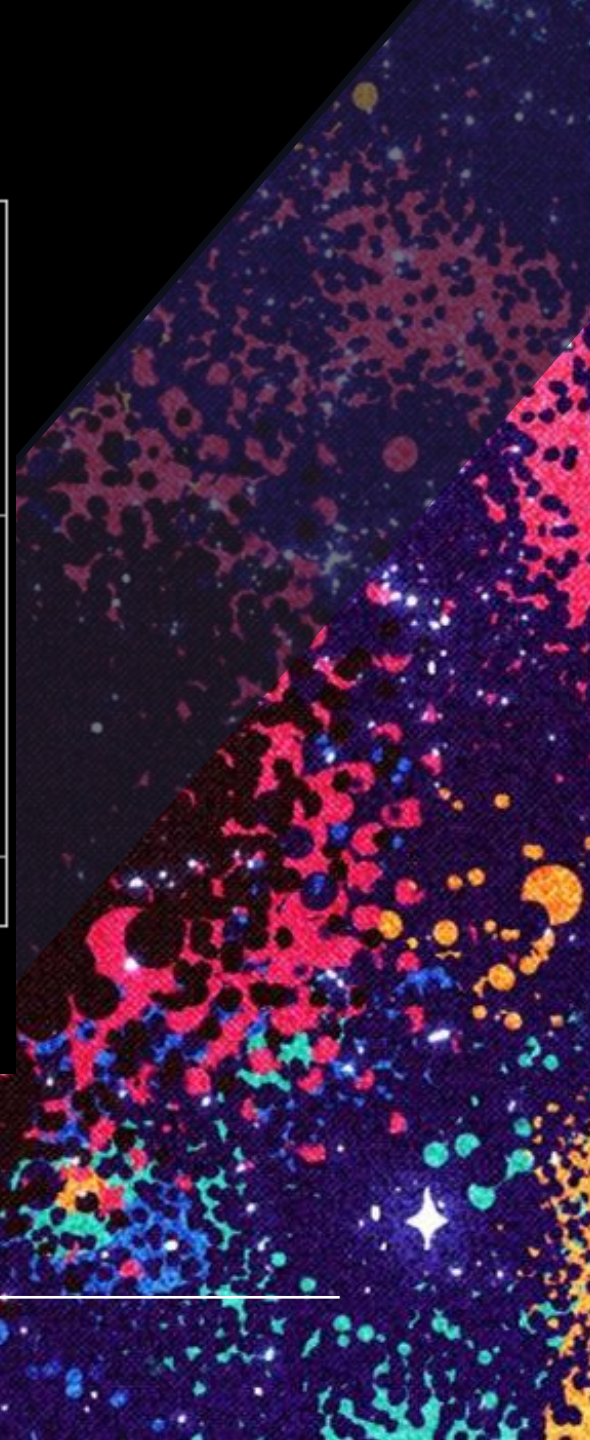
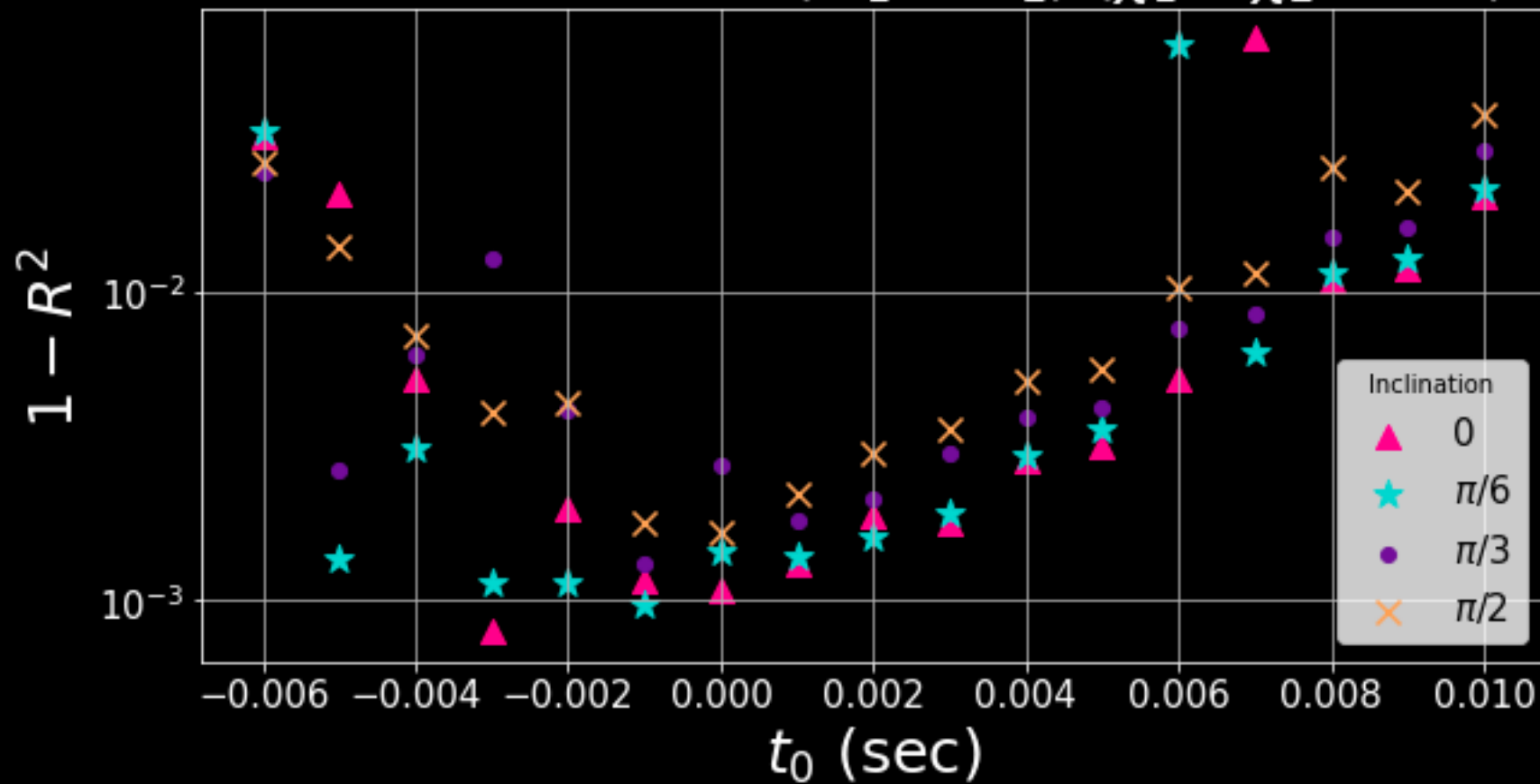
Note: t_0 can be in units of t_M using $t_M = \frac{GM}{c^3}$

IMRPhenomXPHM ($M_1 = M_2$) ($\chi_1 = \chi_2 = 0$)



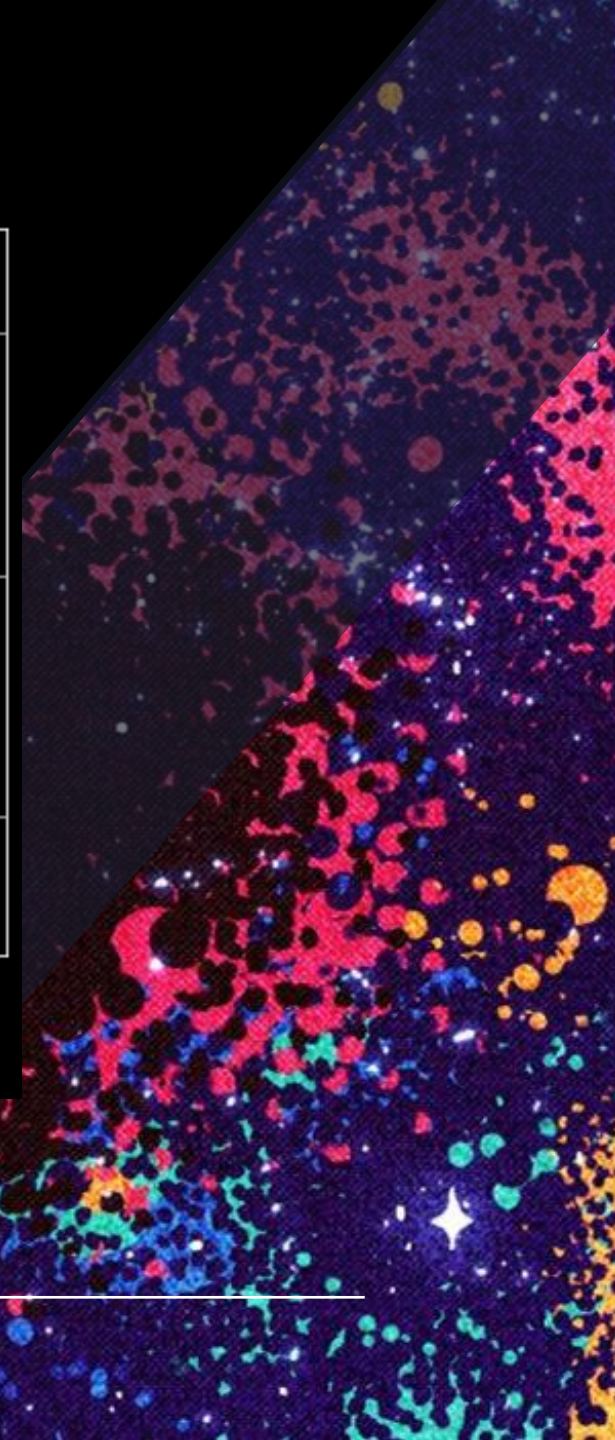
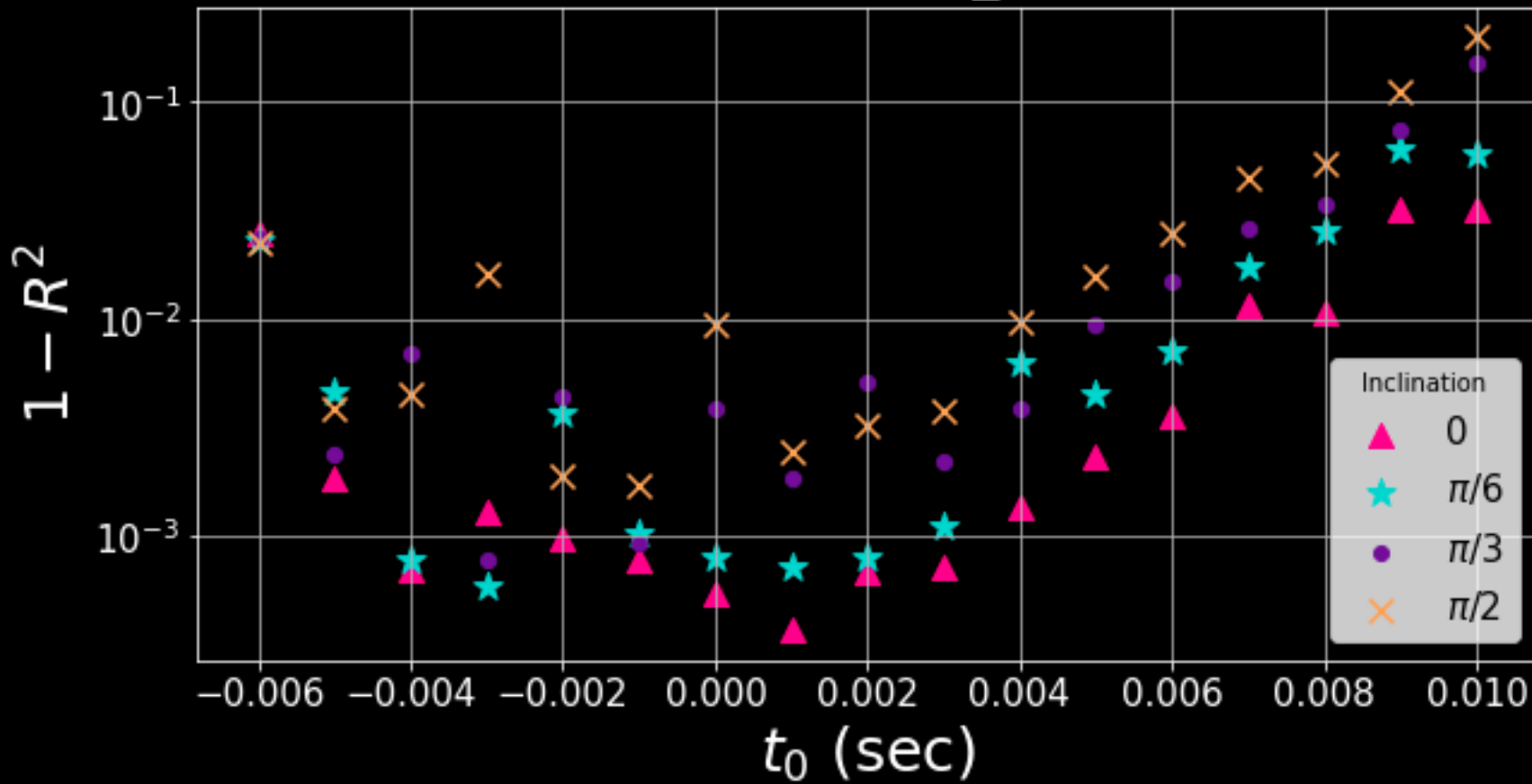
*IMRPhenomXPHM Modes: [21,22,32,33,44]

IMRPhenomXPHM ($M_1 = M_2$) ($\chi_1 = \chi_2 = 0.5$)



*IMRPhenomXPHM Modes: [21,22,32,33,44]

IMRPhenomXPHM ($M_1 = \frac{1}{2}M_2$) ($\chi_1 = \chi_2 = 0$)



*IMRPhenomXPHM Modes: [21,22,32,33,44]

Remnant BH Parameter Recovery

XPHM [21,22,32,33,44]

- SurfinBH

- returns χ and spin

- l-sigma

mass	chi
78.639717	0.870000
78.452861	0.870000
71.000252	0.793228
76.845981	0.860198
78.999563	0.840552
78.675252	0.860175
78.200119	0.853722
76.917871	0.845052

```
chi = 0.831245957632349  
mass = 74.61579536670621
```

To Summarize:

- IMRPhenomXP(HM)
 - Amplitude & phase
 - Remnant mass & spin
- Recovery is highly dependent on t_0 and inclination
- No violations of NHT

What's Next?

- Short-term
 - Compare ringdown analyses
 - Parameter estimation
- Long-term
 - Better understand waveform models
 - Real data analyses
 - Test NHT

References

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Thank You!

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